



UNIVERSITÀ  
DEGLI STUDI  
FIRENZE

## FLORE

# Repository istituzionale dell'Università degli Studi di Firenze

### **Building deformation assessment by means of Persistent Scatterer Interferometry analysis on a landslide-affected area: the Volterra**

Questa è la Versione finale referata (Post print/Accepted manuscript) della seguente pubblicazione:

*Original Citation:*

Building deformation assessment by means of Persistent Scatterer Interferometry analysis on a landslide-affected area: the Volterra (Italy) case study / Bianchini S.; Pratesi F.; Nolesini T.; Casagli N.. - In: REMOTE SENSING. - ISSN 2072-4292. - STAMPA. - 7(4):(2015), pp. 4678-4701. [10.3390/rs70404678]

*Availability:*

The webpage <https://hdl.handle.net/2158/1000608> of the repository was last updated on 2015-12-14T13:12:23Z

*Published version:*

DOI: 10.3390/rs70404678

*Terms of use:*

Open Access

La pubblicazione è resa disponibile sotto le norme e i termini della licenza di deposito, secondo quanto stabilito dalla Policy per l'accesso aperto dell'Università degli Studi di Firenze (<https://www.sba.unifi.it/upload/policy-oa-2016-1.pdf>)

*Publisher copyright claim:*

La data sopra indicata si riferisce all'ultimo aggiornamento della scheda del Repository FloRe - The above-mentioned date refers to the last update of the record in the Institutional Repository FloRe

(Article begins on next page)

Article

## Building Deformation Assessment by Means of Persistent Scatterer Interferometry Analysis on a Landslide-Affected Area: The Volterra (Italy) Case Study

Silvia Bianchini <sup>1,\*</sup>, Fabio Pratesi <sup>1,2</sup>, Teresa Nolesini <sup>1</sup> and Nicola Casagli <sup>1</sup>

<sup>1</sup> Department of Earth Sciences, University of Firenze, Via G. La Pira 4, 50121 Firenze, Italy; E-Mails: fabio.pratesi@unifi.it (F.P.); teresa.nolesini@unifi.it (T.N.); nicola.casagli@unifi.it (N.C.)

<sup>2</sup> Department of Civil and Environmental Engineering, University of Firenze, Via di S. Marta, 3, 50139 Firenze, Italy

\* Author to whom correspondence should be addressed; E-Mail: silvia.bianchini@unifi.it; Tel.: +39-55-275-7751; Fax: +39-55-275-6323.

Academic Editors: Richard Gloaguen and Prasad S. Thenkabail

Received: 19 January 2015 / Accepted: 8 April 2015 / Published: 17 April 2015

---

**Abstract:** In recent years, space-borne InSAR (interferometric synthetic aperture radar) techniques have shown their capabilities to provide precise measurements of Earth surface displacements for monitoring natural processes. Landslides threaten human lives and structures, especially in urbanized areas, where the density of elements at risk sensitive to ground movements is high. The methodology described in this paper aims at detecting terrain motions and building deformations at the local scale, by means of satellite radar data combined with *in situ* validation campaigns. The proposed approach consists of deriving maximum settlement directions of the investigated buildings from displacement data revealed by radar measurements and then in the cross-comparison of these values with background geological data, constructive features and on-field evidence. This validation permits better understanding whether or not the detected movements correspond to visible and effective damages to buildings. The method has been applied to the southwestern sector of Volterra (Tuscany region, Italy), which is a landslide-affected and partially urbanized area, through the use of COSMO-SkyMed satellite images as input data. Moreover, we discuss issues and possible misinterpretations when dealing with PSI (Persistent Scatterer Interferometry) data referring to single manufactures and the consequent difficulty of attributing the motion rate to ground displacements, rather than to structural failures.

**Keywords:** Persistent Scatterer Interferometry; building damages; angular distortion; landslide; Volterra

---

## 1. Introduction

In the last decade, satellite radar interferometry has been successfully applied as a remote-sensing tool to detect movements on the Earth's surface due to its accuracy, high spatial resolution, non-invasiveness and long-term temporal coverage and sampling [1,2]. In addition, displacement information obtained through processing of space-borne radar images covers wide areas, so that mapping and monitoring ground instability is feasible, even at a regional scale.

In particular, advanced multi-temporal interferometric techniques that generate radar benchmarks using a multi-interferogram analysis of SAR (synthetic aperture radar) images, *i.e.*, persistent scatterer interferometry [3], have been successfully used in the last few years for investigating active geological processes, such as landslides and subsidence [4–8]. Persistent Scatterer Interferometry (PSI) relies on temporally stable and highly reflective ground elements, called PS (Persistent Scatterer), in correspondence with which yearly terrain motion rates can be measured with high precision. These scatterers are typically man-made structures (*i.e.*, buildings, pylons, roadways, *etc.*) or natural elements (*i.e.*, rocks) with stable and strong backscattering and coherence characteristics [9]. As a consequence, PSI data are particularly effective for urbanized areas where many radar benchmarks can be retrieved [10]. Just on these populated and built-up areas, potential damages and losses caused by ground instability are stronger due to the higher value of the exposed elements at risk [11].

In past research, space-borne advanced SAR interferometry has been used to map and monitor movements and related building deformations on landslide-prone and -affected areas [11–13]. In particular, several works deal with the use of PS motion rates for detecting displacements in urbanized and cultural heritage sites [14–19], as well as for monitoring single urban structures [20,21].

In built-up areas, the effects of ground instability strongly redound on structures and infrastructures. The induced settlement and damage degree of buildings depend on their construction characteristics and on the geotechnical foundation ground properties. Therefore, some recent works combined InSAR tools with geotechnical features for identifying the potential occurrence of building damages [22–24].

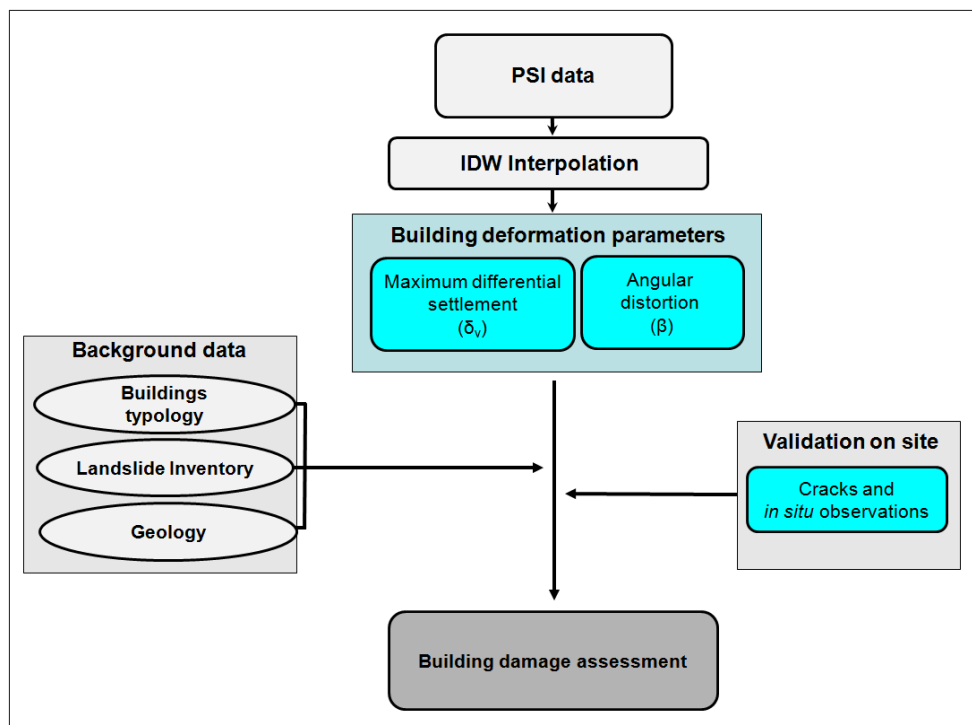
In particular, Sanabria *et al.* in [24] have proposed a method to develop a subsidence map by means of spatial interpolation of PSI displacement data acquired in the C-band, thus overcoming limitations related to the point-wise nature of PS information. This PSI-based methodology has been proven successful in identifying buildings susceptible to suffering subsidence-related damages in urban areas and estimating losses in terms of serviceability limit states.

Relying on the approach proposed by [24], we have applied a similar procedure on the southwestern sector of Volterra (Tuscany, Italy), a partially urbanized area where ground instability threatens the urban fabric and historical heritage, as presented in [25]. PSI data allowed us to locally detect the most unstable zones within the study area and consequently to identify the buildings subject to suffering terrain motions. The proposed PSI-based method allowed us to calculate the differential settlements of these buildings, overcoming the limitations due to the point-wise nature of PS information. The results were

then compared and validated with background data and *in situ* evidence to confirm the effectiveness of the proposed procedure.

## 2. Methodology

We propose an operative procedure to handle PSI displacement measurements combined with background data (building typology, landslide inventory, geological setting) and on-site evidence, finally leading to a building deformation assessment in the investigated area (Figure 1).

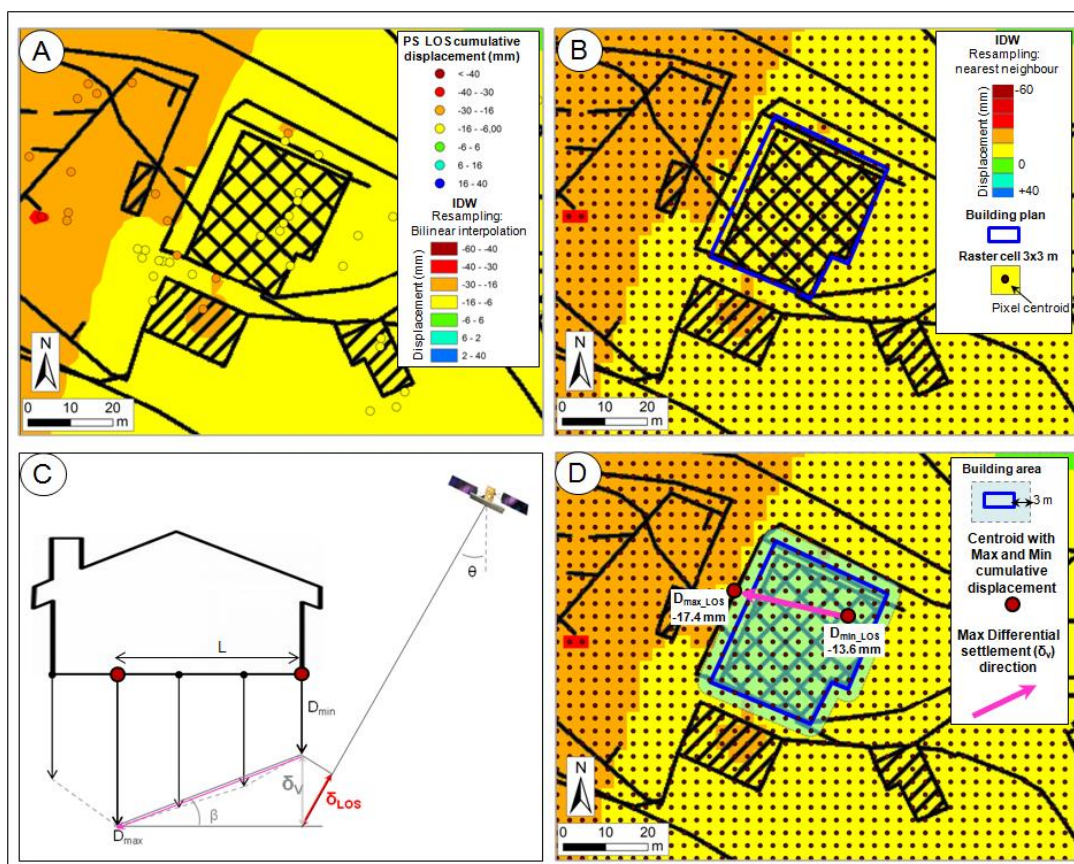


**Figure 1.** Methodology flowchart.

Mean yearly velocities and cumulative displacement provided by PSI data are measured along the satellite LOS (Line Of Sight) on a grid of point-like benchmarks on the ground. Since these measurements are characterized by a discrete point-sampling for certain locations, a surface interpolation of PS cumulative displacement rates is needed in order to obtain a displacement map of the whole area and, thus, to estimate ground motion displacements occurring in the monitoring period, even where no PS are available.

Following this facet, we have used the Inverse Distance Weighted (IDW) interpolation method to create a continuous displacement-surface from the sample set of PSI point locations (Figure 2a) [26].

IDW is a deterministic method for spatial interpolation based on the basic principle of geography, which defines that elements that are close to each other are more similar than elements farther away [27]. Using this principle, the IDW interpolator predicts a value for any unmeasured location by using the closest measured values and by assuming that each measured point has a local influence that diminishes with distance. Thus, IDW methods produce interpolated surfaces assuming that discrete values are mostly influenced by the nearby points and less by the more distant points. In the case of PSI datasets, the interpolating surface is a weighted average of the existing scatter points, and the weight assigned to each scatter point diminishes as the distance from the interpolation point to the scatter point increases.



**Figure 2.** Step by step procedure for building damage characterization and estimation: (A) PSI data and derived IDW surface displayed as bilinear interpolation layered on building boundaries; (B) IDW surface displayed as a nearest-neighbor discrete raster, with pixel centroids obtained for each raster cell; (C) schematic representation of differential settlement parameters used within the analysis; (D) computation of differential settlement direction within an appropriate buffer around the building.

The resolution of the IDW interpolation cell is to be set according to the resolution of the employed space-borne radar image. For instance, the pixel size of the resulting surface would be set as  $20 \times 20$  m if using medium-resolution C-band data (e.g., ERS 1/2 and ENVISAT) or as  $3 \times 3$  m if exploiting high ground resolution X-band data (e.g., COSMO-SkyMed data).

The raster re-sampling is firstly a bilinear interpolation for general-purpose smoothing and then converted into a nearest-neighbor re-sampling for getting a discrete center-to-center raster display.

As a result, a displacement value is assigned to each pixel centroid of the interpolated surface, thus obtaining a regular grid of distributed rates (Figure 2b).

Then, in order to detect movement directions and consequent expected damages on buildings, differential settlements of manufactures are calculated according to the criteria of serviceability limit states (SLS), which are those conditions that make the structure unsuitable for its projected use [28–30]. In particular, we used the maximum vertical differential settlement ( $\delta_v$ ) and the angular distortion ( $\beta$ ) calculated between the maximum and the minimum cumulative displacement (Figure 2c) [30–33].

The maximum vertical differential settlement ( $\delta_v$ ) is defined as the unequal settling of a building, and it is computed as the maximum difference of vertical displacement between two points of the foundation.

We chose these two points as the centroids with the maximum and the minimum cumulative displacement derived from PS time series. Thus, we calculated the  $\delta_v$  value by using the following equation:

$$\delta_v = \frac{|D_{\min\_LOS} - D_{\max\_LOS}|}{\cos \theta} = \frac{|\delta_{LOS}|}{\cos \theta} \quad (1)$$

where  $D_{\min\_LOS}$  and  $D_{\max\_LOS}$  are the minimum and maximum displacements measured on the building along the satellite LOS during the three-year (2010–2013) monitoring period,  $\delta_{LOS}$  is the maximum differential settlement between these two measurement points along the LOS and  $\theta$  is the satellite incidence angle. It is worth highlighting that the  $\delta_{LOS}$  value is divided by the cosine of the satellite incidence angle in order to obtain the maximum vertical differential settlement ( $\delta_v$ ) of a given structure [24].

The angular distortion ( $\beta$ ) we consider is related to the measured vertical settlement, and thus, it is computed as the ratio between  $\delta_v$  and the distance ( $L$ ) between the  $D_{\min\_LOS}$  and  $D_{\max\_LOS}$  measurement points:

$$\beta = \frac{\delta_v}{L} \quad (2)$$

The values  $D_{\min\_LOS}$  and  $D_{\max\_LOS}$ , used for the computation of  $\delta_v$ , the distance  $L$  and  $\beta$ , are set as the maximum and minimum displacements provided by PS time series, measured during the monitoring period (2010–2013) and assigned to the centroids of the pixel cells included within the “building area”. The “building area” is the buffer area drawn around the plain-edge of the analyzed building. The size of this tolerance area is dimensioned accordingly to the cell size resolution of the displacement raster surface and consequently to the spatial resolution of the radar images.

As observed in the case of “control areas” defined by [17], the use of a buffer allows taking into account even PS that do not lie within the building plain-edge, but that are the result of a backscattered signal mainly influenced by the structure itself, as a consequence of the metric resolution cell of SAR images. Moreover, the use of a buffer permits avoiding possible shifts in the georeferencing procedure of PSI data stacks, buildings and other cartographical layers.

The centroids of the two pixel cells included within the “building area” and selected for the calculation of  $D_{\min\_LOS}$  and  $D_{\max\_LOS}$  define the direction along which differential settlement is dominant (Figure 2d).

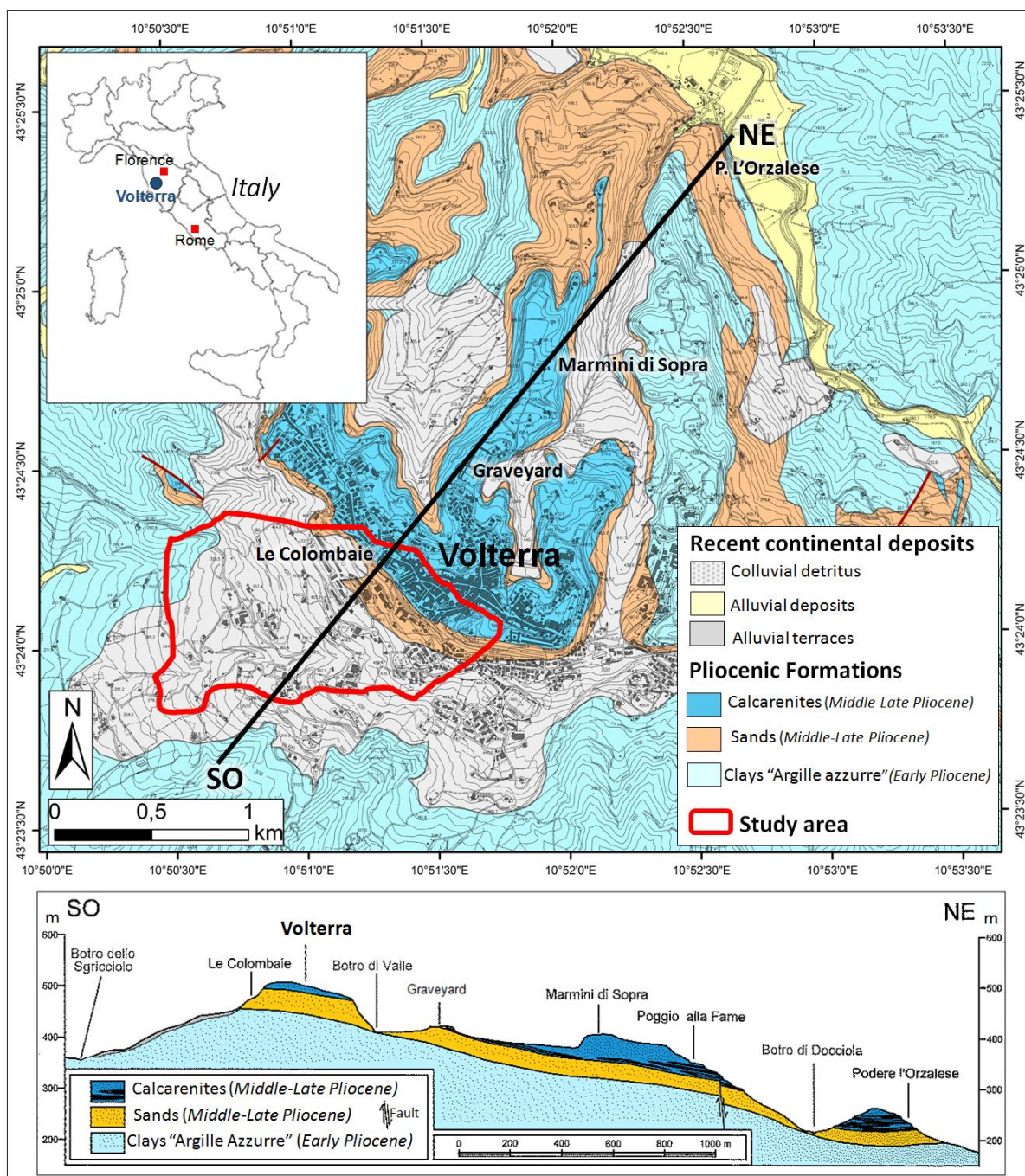
Since differential settlements and relative building damages depend on the movements of the foundation soil, as well as on the type of the structure itself, the amount and direction of the computed parameters  $\delta_v$  and  $\beta$  are cross-compared with background data, among which are the geological setting, the landslide inventory map and building typology information (Figure 1). Finally, validation and interpretation of the estimated PSI settlements are obtained by matching up  $\delta_v$  and  $\beta$  to local failures and building crack patterns recognized by *in situ* observations, the geological setting and constructive features.

### 3. Volterra Case Study

The above-mentioned methodology was applied on the southwestern sector of Volterra (Tuscany region, Italy). This area was chosen as the test site, since it is partially landslide affected and characterized by a middle urban fabric density between the city center and the rural area. Moreover, this test site, which extends up about 86,500 m<sup>2</sup>, includes different building typologies, such as masonry structures and concrete buildings realized either in the 19th century or in recent years, with different foundation types (e.g., direct foundations or bearing piles).

### 3.1. Geological Background

The town of Volterra is located on a tableland at 460–500 meters a.s.l. (above sea level) (Figure 3). The geological setting of the area consists of a Pliocene marine sedimentary succession. The bottom of the stratigraphic sequence is represented by a thickness of marine clays (“Argille Azzurre”) of Early-Middle Pliocene age, overlapped by cemented sandy deposits (“Villamagna sands”). The calcarenites named “Volterra limestones” close the sedimentary succession and lay at the top of the tableland, on which the Volterra city center was built. These three lithological units are stacked in horizontal or sub-horizontal layers, slightly dipping towards northeast, with an inclination that never exceeds 10 ° [34,35] (Figure 3).

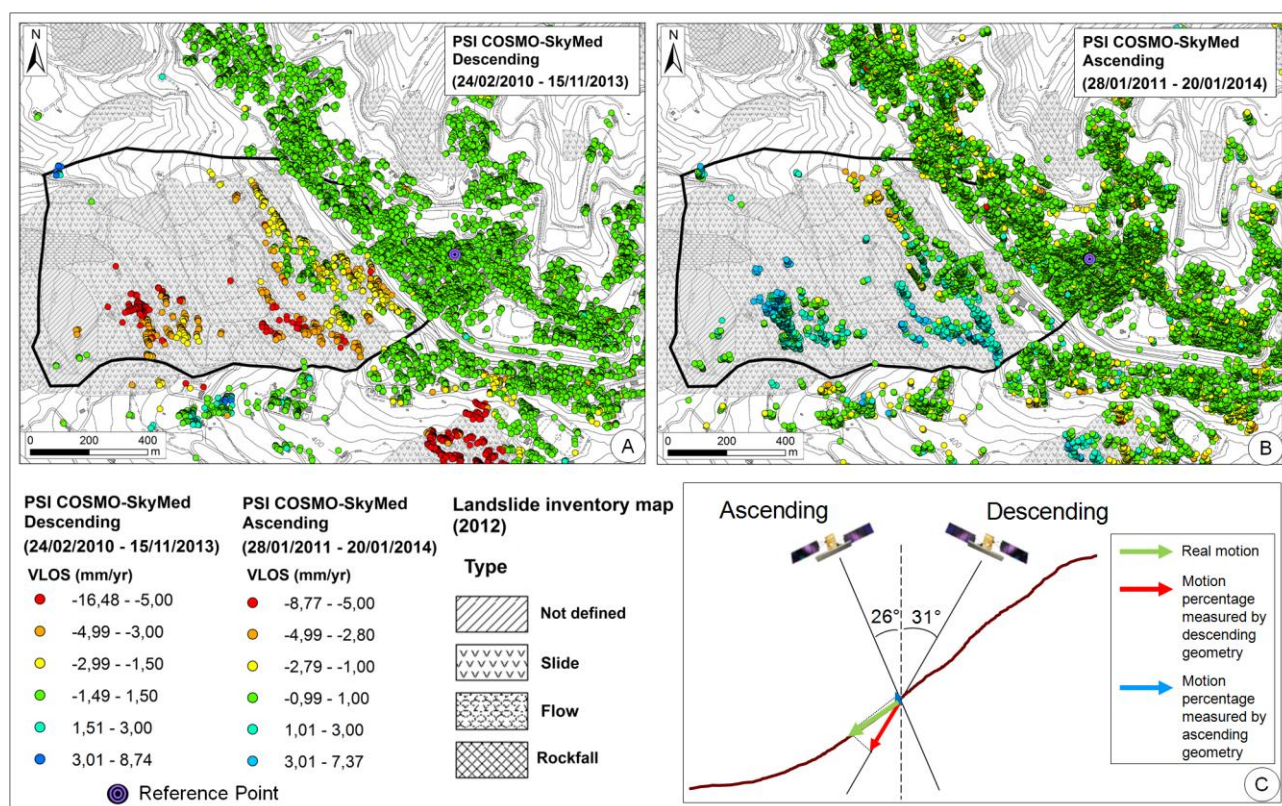


**Figure 3.** Volterra study area: geological map and section. In order to emphasize the morphology, a vertical exaggeration of 2× is applied to the section. Modified from [34].

The different geotechnical properties between the impermeable clays, the upper erodible Villamagna sands and well-cemented Volterra calcarenites determine the undermining of the clayey bases of the hill and consequent retrogressive slope failures that generate very steep, sub-vertical cliffs around the tableland.

Late Pliocene and Quaternary terrigenous debris lie upon the sandy-clay units, filling the valleys in the surrounding area. This extensive colluvial debris sheet, which lies on the sedimentary sequence, mainly derives from the gradual weathering of the upper sandy formations and calcarenites on which the city itself is built [34].

The geological structure and topography of the tableland influence the typology and the spatial distribution of mass movements. On the southwestern slope of the Volterra hill (red polygon in Figure 3), the Argille Azzurre mainly crops out, and the area turns out to be affected by gullies, typical of clayey soils. From an altitude of 450 m a.s.l., sands crop out, overlapped by calcarenites, where the Volterra city center is built. The main landslide typologies are represented by shallow translational slides and soil erosion, according to the available landslide inventory map provided by the Tuscany region and referring to 2012 (Figure 4a,b).



**Figure 4.** Velocity rates and spatial distribution of available PSI data overlapped on the landslide inventory map of Volterra area provided by the Tuscany region. The close-up study area is the black-contoured sector: (A) PSI COSMO-SkyMed in descending orbit; (B) PSI COSMO-SkyMed in ascending orbit; (C) sketch representing the two COSMO-SkyMed acquisition geometries combined with the local topography of the study area.

The shallow colluvial deposits, made up of chaotic detritus, reach up to a thickness of 20 meters in the study area and contribute to determining the ground instability. As a result, diffuse landsliding of the

area actually could result from shallow ground deformation related to the instability of the colluvial layer or to surface creep downslope, rather than to landslides.

### 3.2. PSI Data

Available satellite radar data over Volterra consist of 57 SAR images acquired in the X-band by the COSMO-SkyMed (CSK) satellite of ASI (Italian Space Agency) in the time spanning 2010–2014 and processed by means of the SqueeSAR™ approach, which is an evolution of PSInSAR™ [36]. The acquisition parameters of the available SAR images are reported in Table 1.

The SqueeSAR™ technique overcomes some limits of PSInSAR, the analysis of interferometric data-stacks, by extracting information not only from point-wise deterministic objects (*i.e.*, PS), but also from distributed scatterers (DS). DS are areas of moderate coherence in some interferometric pairs of stacks, where a sufficient high number of random small scatterers is present within a resolution cell with no dominant scatterer and follows the complex circular Gaussian distribution [37,38].

DS, which are widespread in rural areas, correspond to rangeland, pasture, shrubs, bare soils, *etc.*, that do not produce the same high signal-to-noise ratios of PS, but are, however, discernible from the background noise. Thus, the SqueeSAR™ technique jointly processes PS and DS, making the density of terrain benchmarks higher, especially in semi- and non-urban areas.

**Table 1.** Main features of the exploited PSI datasets in the Volterra area. CSK, COSMO-SkyMed.

Feature	CSK	CSK
Wavelength	X (~3.1 cm)	X (~3.1 cm)
Incidence angle $\theta$ (°)	26	31
Geometry	Descending	Ascending
Azimuth x range PS cell resolution (m × m)	3 × 3	3 × 3
Revisit time (day)	16	16
Temporal span (day/month/years)	24 February 2010– 15 November 2013	28 January 2011– 20 January 2014
Processing method	SqueeSAR™	SqueeSAR™
N° of used SAR images	25	41
N° of PSI within study area	1,623	2,484

In this work, PSI analysis was focused on the Volterra southwestern area, which is the most critical and unstable sector, as it is affected by extensive dormant mass movements and consequently characterized by the highest PSI ground motion rates (Figure 4b,c).

The spatial distributions of PSI LOS velocities are shown in Figure 4. The negative sign stands for an increasing distance of the benchmark from the satellite sensor, while a positive sign means a movement towards the satellite. Within the PSI velocity, stability thresholds are fixed at  $\pm 1.5$  mm/year and  $\pm 1.0$  mm/year in descending and ascending orbits, respectively, for distinguishing stable targets (displayed in a green color) from moving ones. Most of the published PSI landslide analyses have been performed on the C-band (4–8 GHz, 5.6-cm wavelength) and establish the stability LOS velocity threshold at  $\pm 2$  mm/year [13]. Since the LOS displacement sensitivity increases with the radar frequency, the stability thresholds in the X-band (8–12 GHz, 3.1-cm wavelength) have been set within a narrower range, at  $\pm 1.5$

mm/year or 1.0 mm/year, being compatible with one and 1.5 standard deviation values of CSK PS populations, respectively, for the ascending and descending dataset. These values are also in accordance with stable threshold choices already tested and accepted by the scientific community [5,10,14,39].

The reference point of PSI datasets is located within the city center, which is the stable part of Volterra, as confirmed by landslide inventories and the absence of ground motion evidence, while the highest mean annual LOS velocities reach up tens of mm/year within the southwestern study area (Figure 4).

When observing ground motions using satellite radar images, only the component of movement along the LOS is detected. Additionally, being that the satellite orbits polar and right-side looking, the same terrain movement can be measured with opposite signs and different modules from ascending and descending passes, thus making the slope dynamics interpretation not immediately intelligible [6,13]. Consequently, PSI-based displacement data depend on the combination of the sensor acquisition geometry (orbit and incidence angle) with the local topography (aspect and slope of the area) and with the real direction of movement [4,6]. Generally, radar data collected in ascending orbit are suitable for detecting E-facing slope movements, while descending geometry is more appropriate for W-facing slope movements. Therefore, given the west-facing orientation of the Volterra southwestern area, movements measured by the COSMO-SkyMed satellite in ascending geometry strongly underestimate the downslope motion, as they are minimized by the combination of slope topography and LOS, whereas movements recorded in descending orbit are a good approximation of the real displacements, as ground motion direction is nearly parallel to LOS direction (Figure 4c). Consequently, for the PSI analysis on the study area, only the CSK dataset in descending geometry was considered and analyzed within the study area.

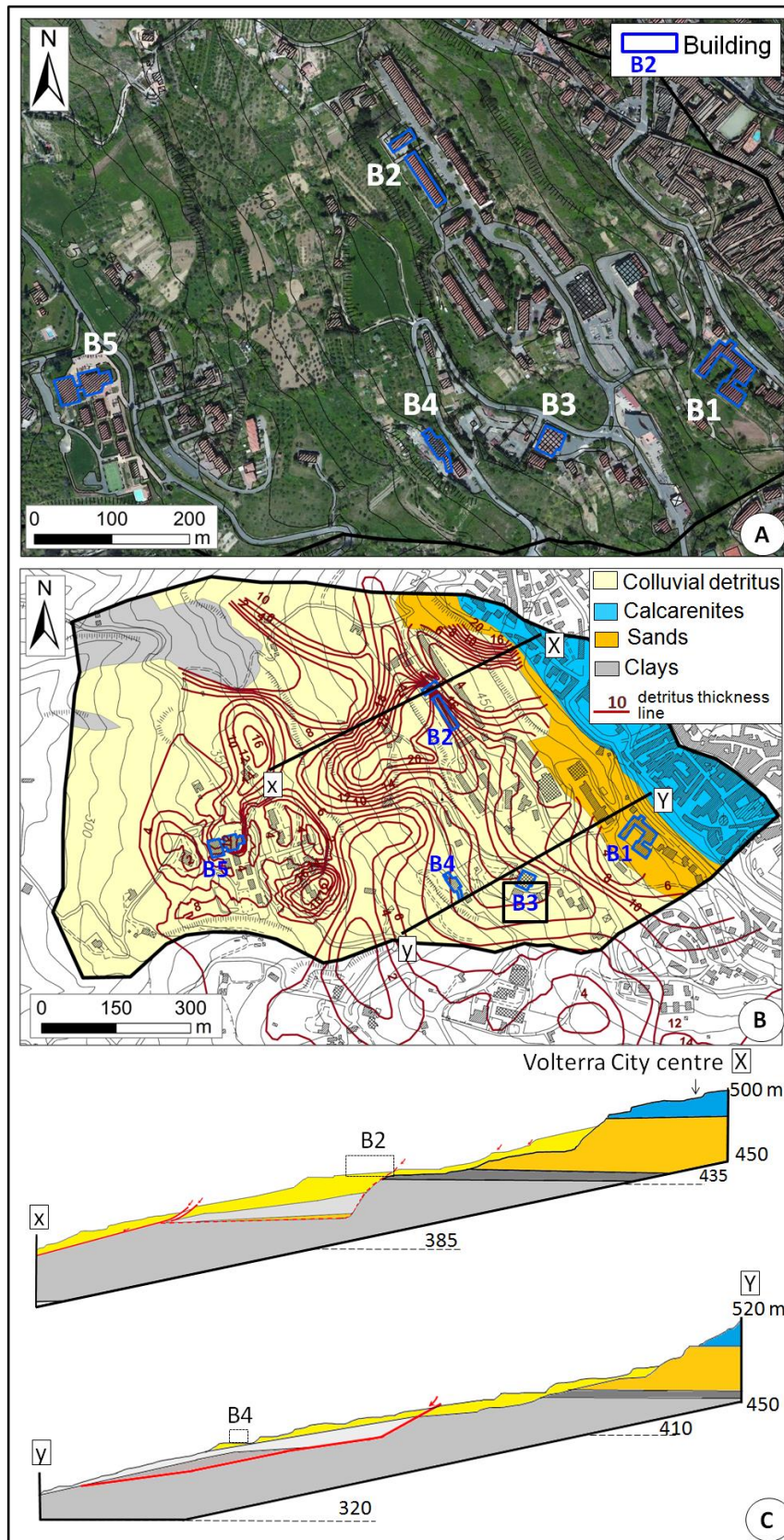
### 3.3. Analysis Results and Validation

We present results on five example buildings (B1–B5 in Figure 5) homogeneously distributed in the test area (Figure 5a) at different topographic elevations along the slope (from 340 m a.s.l. up to 470 m a.s.l.) (Figure 5b, Table 2). The selected structures are characterized by different construction typologies, age and foundations, as well as by different foundation ground, since they are located on sandy formations (B1) or clayey formations covered by colluvial deposits with very different thicknesses (B2 to B5).

On these buildings, we performed a deformation assessment throughout the PSI-based computation of differential settlement values. Then, we cross-compared these values with background data and crack pattern damages detected during a recent *in situ* survey, in order to validate the estimated building deformations.

The building damage assessment was performed considering descending CSK PSI data acquired in the recent three-year time interval 2010–2014 and analyzing their deformation time series. As during this acquisition period, no restoration activities were undertaken over the selected structures, the *in situ* surveys of building crack patterns, performed during 2014, can be considered reliable.

On the one hand, PS velocities detected on rocks and natural elements within a landslide phenomenon may reasonably be ascribed to the landslide itself; on the other hand, the measured displacement of PS on buildings represents the result of an interaction between the movement of the landslide and the mechanisms of the soil-structure system, and damages potentially derive from this interaction.



**Figure 5.** (A) Location of the five case studies; (B) geological map of the study area; and (C) two longitudinal sections.

The resolution of the IDW interpolation has been set as three meters, according to the  $3 \times 3$  m cell size of COSMO-SkyMed satellite images. By virtue of such a resolution, many PS show up on building facades and roofs, fitting the typical scale of constructive elements well.

**Table 2.** Values of minimum and maximum line of sight (LOS) displacement during the period 2011–2013 ( $D_{\min\_LOS}$  and  $D_{\max\_LOS}$ , respectively), distance L between  $D_{\min\_LOS}$  and  $D_{\max\_LOS}$ , maximum vertical differential settlement ( $\delta_v$ ) and the related angular distortion ( $\beta$ ) for each building (B1–B5) during the period 2011–2013.

Building	$D_{\min\_LOS}$ (mm)	$D_{\max\_LOS}$ (mm)	L (m)	$\delta_v$ (mm)	$\beta$ between $D_{\min\_LOS}$ and $D_{\max\_LOS}$	
B1	−4.87	−9.11	54.74	4.94	$9.03 \times 10^{-5}$	
B2	B2 <sub>i</sub>	−4.99	−22.96	34.71	20.96	$6.04 \times 10^{-4}$
	B2 <sub>ii</sub>	−7.86	−12.55	29.68	5.47	$1.84 \times 10^{-4}$
B3	−13.59	−17.38	27.70	4.42	$1.59 \times 10^{-4}$	
B4	−15.75	−41.35	66.06	29.86	$4.52 \times 10^{-4}$	
B5	−22.35	−39.34	36.24	19.82	$5.46 \times 10^{-4}$	

As background data, we used a topographic map at 1:10,000 scale, a geological map of the Volterra municipality, digital color orthophotos with 1m resolution and the landslide inventory map of the area provided by the Tuscany region.

### 3.3.1. Building B1

Building B1 is a public comprehensive school and consists of a U-shaped masonry structure (Figure 6). The edifice was built in 1933, and it is located on outcropping sands at an altitude of about 470 m a.s.l.

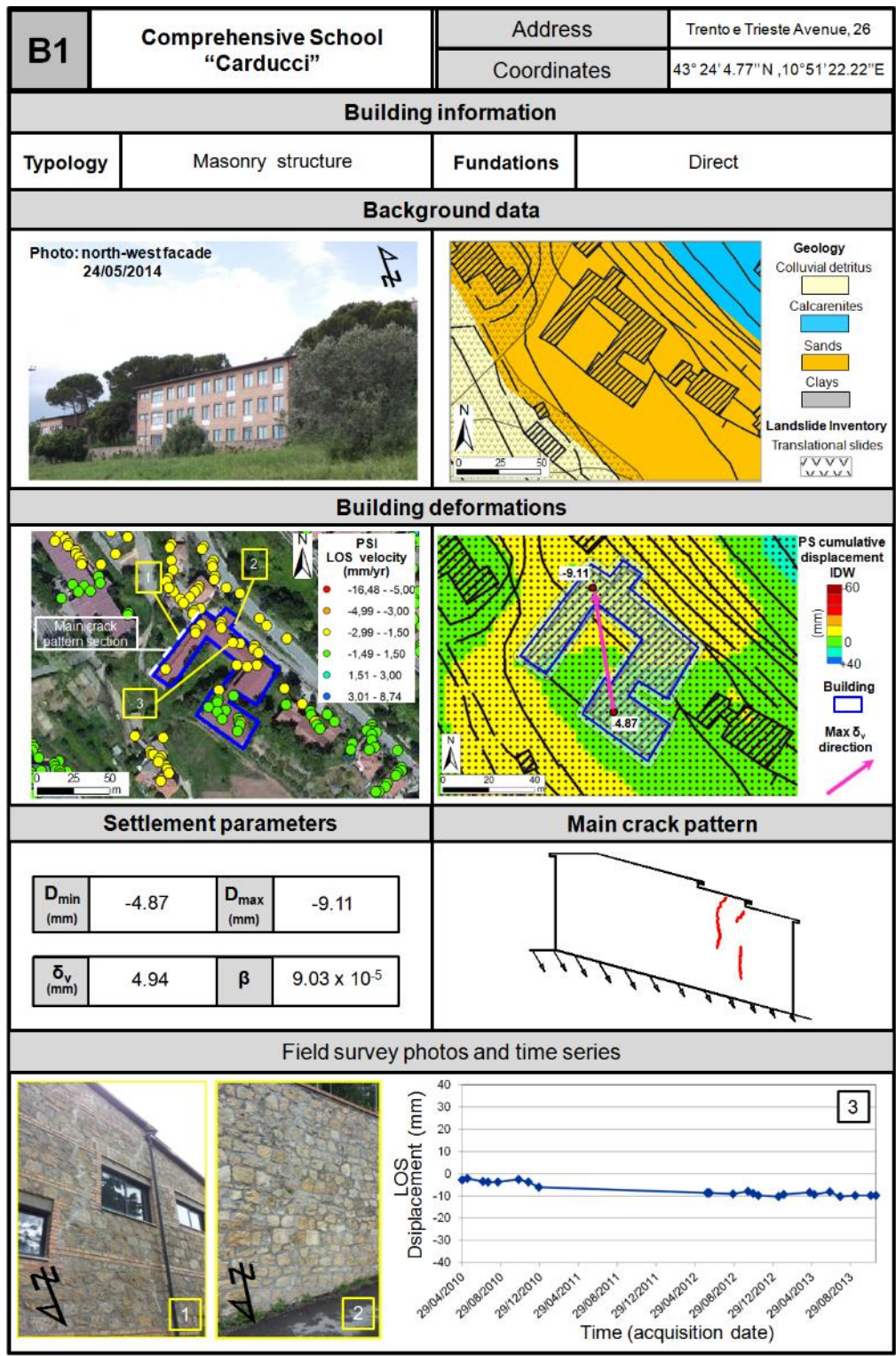
#### Deformation Assessment

PS motion rates show mean yearly velocity values of about 2–3 mm/year downslope during the monitoring period (2010–2013). PS cumulative displacements and their IDW interpolation show values up to 8–9 mm over the “building area” (Figure 6).

In particular, PS located on the southeastern portion of the building are stable, while the ones located on the northwestern portion show a slight tendency to move. Moreover, PSI deformation time series reveal a linear trend of displacement from April, 2012, until November, 2013 (Figure 6).

#### Validation

PSI data were validated with *in situ* checks performed in April–May, 2014. Although good overall conditions were recognized, some centimetric vertical cracks were detected in the external walls of the northwestern portion of the building. The position and the pattern of the cracks are compatible with the direction of the estimated maximum differential settlement (SE-NW-oriented vector). The low modules of both differential settlement ( $\delta_v$ ) and angular distortion ( $\beta$ ) (4.94 mm and  $9.03 \times 10^{-5}$ , respectively) are concordant with the geological setting, as the building is located on almost stable terrain, *i.e.*, sandy formation, within an area not affected by recorded landslides.



**Figure 6.** Analysis results of building B1: building information, background data, building deformations, settlement parameters, main crack pattern, some photos of the field survey and a PS time series (the gap during year 2011 is due to missing acquisitions).

### 3.3.2. Building B2

Building B2 is a private housing estate that includes two reinforced concrete structures (Figure 7). Both edifices (B2<sub>i</sub> and B2<sub>ii</sub>) are built on a clayey morphological sub-vertical scarp 30 meters high

completely covered by colluvial deposits and only recently detected [40]. The colluvial detritus derives from the weathering of the clays and upper sands, and its thickness reaches up values of 25–30 meters.

The buildings, initially built with direct foundations, were partially underpinned with 11 meter-long piles in 1997, since they were affected by important settlements and suffered consequent damages. These remedial actions did not effectively strengthen the foundations, and further settlements occurred because the bearing micropiles were not sufficiently long with respect to the detritus thickness; thus, they did not reach the bedrock, but were within the thick colluvial layer.

In particular, the uphill portion of the building B2<sub>ii</sub> is directly built on the bedrock, since the bearing piles reach it, while the downhill portion of the building is completely pinned within the soft colluvial deposits (Figure 7). The same occurs on the southwestern and northeastern portions of B2<sub>i</sub>, the first being underpinned in the bedrock of the edge scarp and the second in the colluvial detritus above the scarp. As a result, the scarp influences the deformations of the buildings of the area, as also confirmed by the edifices uphill that appear to be stable.

### Deformation Assessment

On building B2<sub>i</sub>, average LOS velocities of about 2–4 mm/year and cumulative displacements up to 20–22 mm are recorded within the acquisition period, while on building B2<sub>ii</sub>, no PS were detected, even if IDW interpolation provides a displacement surface over the whole area.

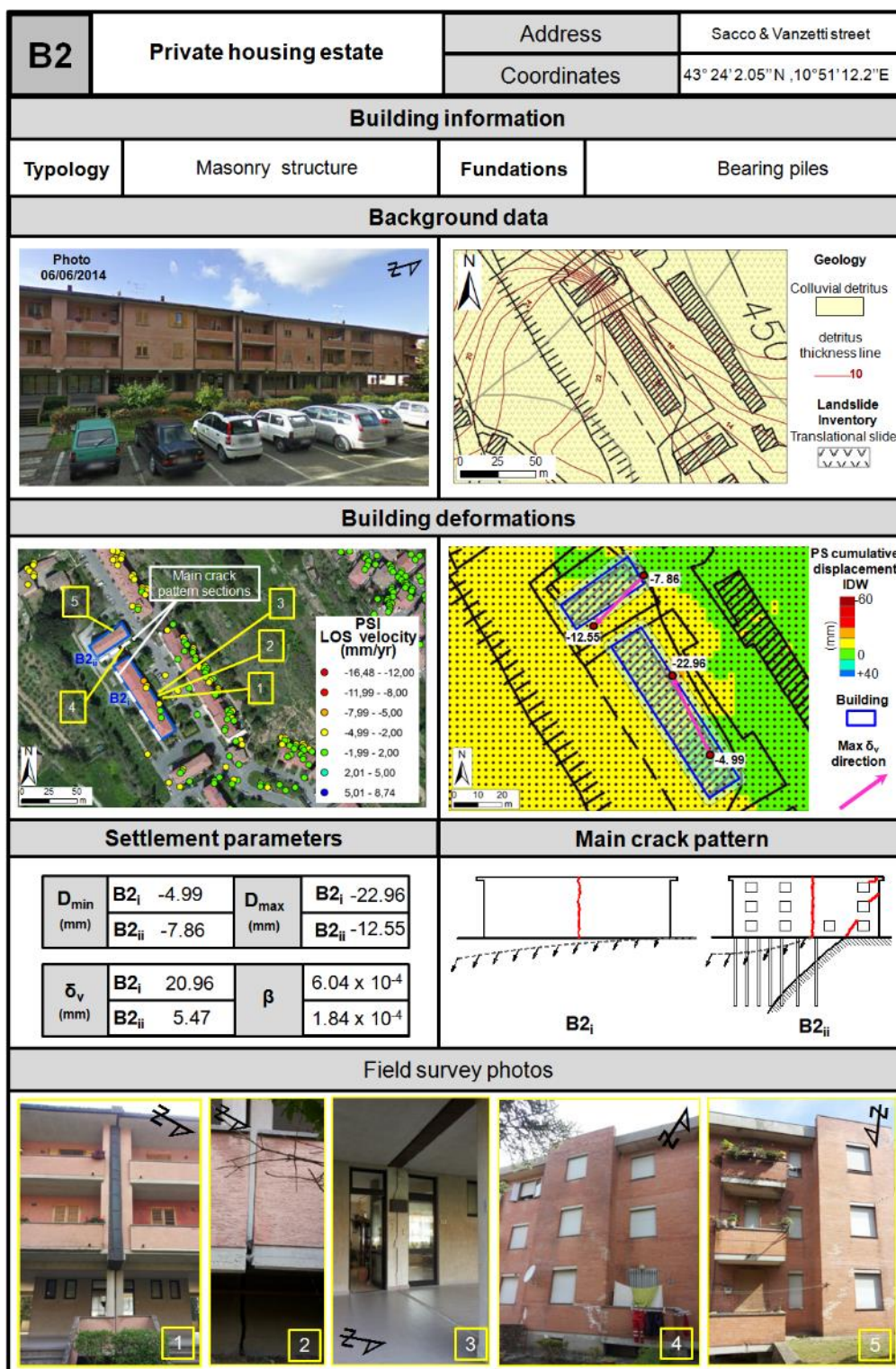
Settlement parameters were calculated for both buildings B2<sub>i</sub> and B2<sub>ii</sub>. Building B2<sub>i</sub> shows a high  $\delta_v$  value of 20.96 mm, SE-NW directed. Building B2<sub>ii</sub> shows a  $\delta_v$  value of 5.47 mm E-W oriented, which could be not completely reliable, since it is merely based on IDW interpolation values. Both edifices show high angular distortions ( $\beta$ ), with values of  $6.04 \times 10^{-4}$  and  $1.84 \times 10^{-4}$  (Figure 7).

Both buildings are located on an area affected by shallow translational slides, according to the available landslide inventory map. Moreover, the buildings are sited on the above-mentioned scarp, thus standing at the stratigraphic contact between geotechnically different lithotypes, *i.e.*, the clayey bedrock and the upper colluvial sediments.

### Validation

Field checks confirmed and validated the critical instability conditions revealed by deformation parameters and background data. In fact, both buildings are affected by intense damages resulting in centimetric cracks on the external facades (Figure 7). In particular, building B2<sub>ii</sub> shows 45° fissures with a centimetric width on the facades, mainly coinciding with weaker wall areas, *e.g.*, window corners. Building B2<sub>i</sub> is cracked into two portions, as confirmed by vertical centimetric fissures at mid-length.

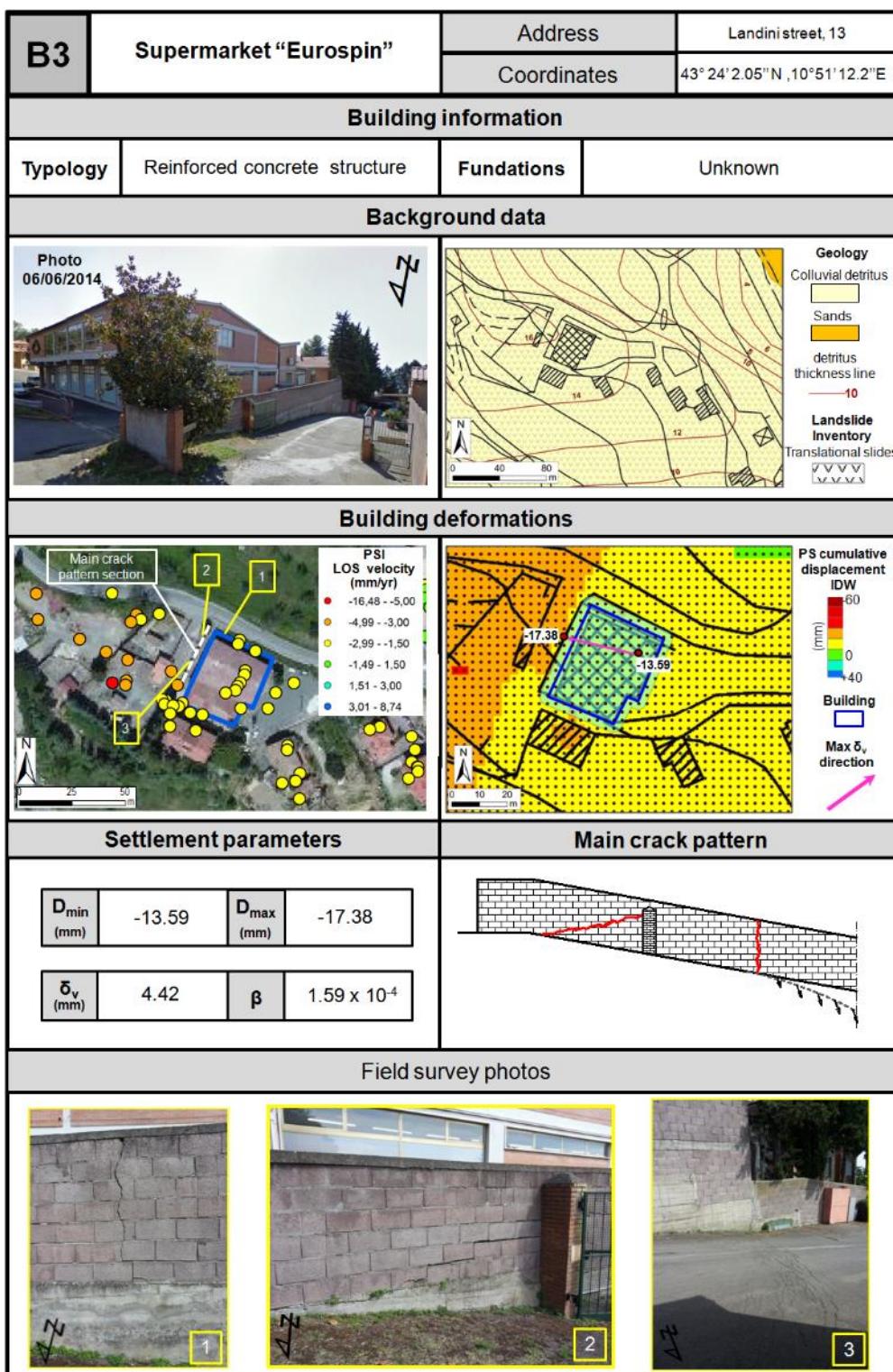
These crack patterns are clear effects of differential settlements, and their directions are consistent with  $\delta_v$  orientation, as well as with the direction of the morphological scarp. The recorded motions are potentially due to the building loading on the colluvial layer on the scarp and also to the downslope creep of the shallowest portion of this layer.



**Figure 7.** Analysis results of building B3: building information, background data, building deformations, settlement parameters, main crack pattern and photos of field survey.

### 3.3.3. Building B3

Building B3 is a reinforced concrete structure that houses a supermarket (Figure 8). It is located at an altitude of about 430 m a.s.l., on a 16–14 m-thick colluvial layer that lays on the clayey unit. The area is affected by a dormant translational landslide, which is extended uphill to an altitude of 440 m a.s.l.



**Figure 8.** Analysis results of building B3: building information, background data, building deformations, settlement parameters, main crack pattern and photos of field survey.

Deformation Assessment

CSK PSI data retrieved on building B3 reveal movements characterized by mean yearly velocities of about 4 mm/year and cumulative displacements of about 16 mm at the last acquisition date, while radar benchmarks located W-NW the building show higher motion rates up to 6 mm/year and displacement of

18–19 mm. Thus, minimum cumulative displacement is retrieved on the building roof (−13.59 mm), whereas the maximum one (−17.38 mm) is estimated on the passageway westward. Comparing these values with the soil thickness map, it can be observed that the direction of maximum differential settlement  $\delta_v$  is dipping NW towards the thickest compressible colluvial sediments (Figure 8).

#### Validation

Field campaign results reveal no evident damages on the supermarket structure. Conversely, on the passageway, scarps and cracks on the road pavement, as well as significant centimetric fissures on the walls show clear landslide evidence and are in agreement with the SW downslope movement.

As a result, PSI data, differential settlement parameters and field checks confirm that the whole area is unstable and landsliding, and the higher movements detected towards W-NW of the building B3 within the landslide body could be determined by the higher thickness of the colluvial deposits, which increases the creeping and slope instability.

#### 3.3.4. Building B4

Building B4 is an alabaster warehouse that consists of a reinforced concrete structure located at an altitude of 410 m a.s.l. The area is characterized by a 12 m-thick colluvial layer that lays on the clayey unit, and it is affected by the dormant translational landslide that also includes building B3. The landslide slip surface is at an 18-m depth between upper geotechnically poor clays characterized by low shear strength and lower clays with better geotechnical properties, *i.e.*, a higher shear strength [39]. The structure has direct foundations consisting of a grade beam placed directly on the ground (Figure 9).

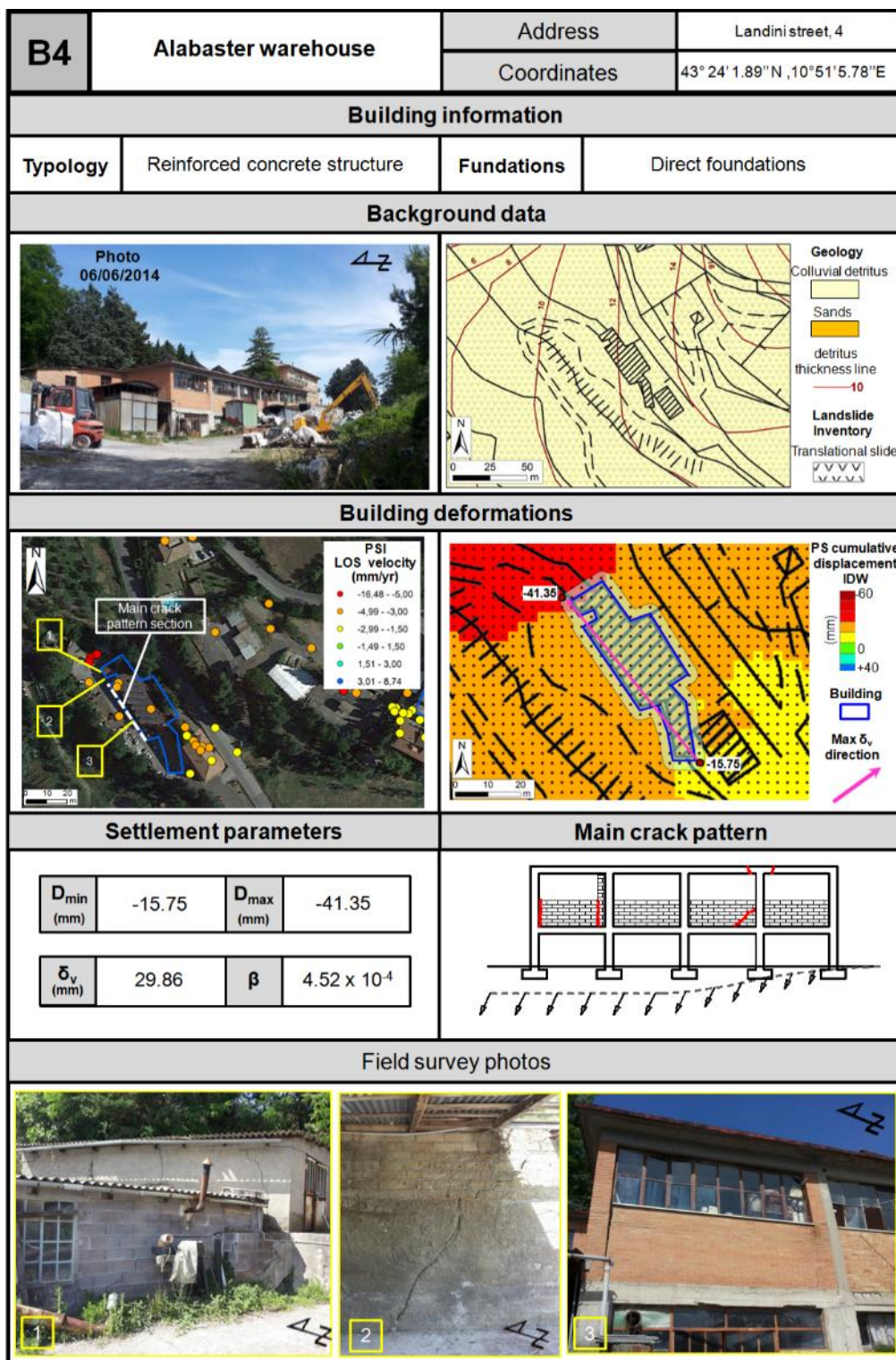
#### Deformation Assessment

The IDW interpolation of PS data exhibits high cumulative displacements up to about 40 mm, with spatially increasing values from SE to NW. Accordingly, the maximum differential settlement  $\delta_v$  for B4, with a SE-NW vector orientation, shows a considerable value (29.86 mm).

#### Validation

The PS data spatial pattern, as well as  $\delta_v$  and  $\beta$  directions were compared and validated with *in situ* observations. Intense damages were surveyed on the building, resulting in millimetric–centimetric cracks on external walls, as shown in Figure 9.

The location and pattern of damages, normal to tension stresses, resulted in agreement with the orientation of the  $\delta_v$  vector.

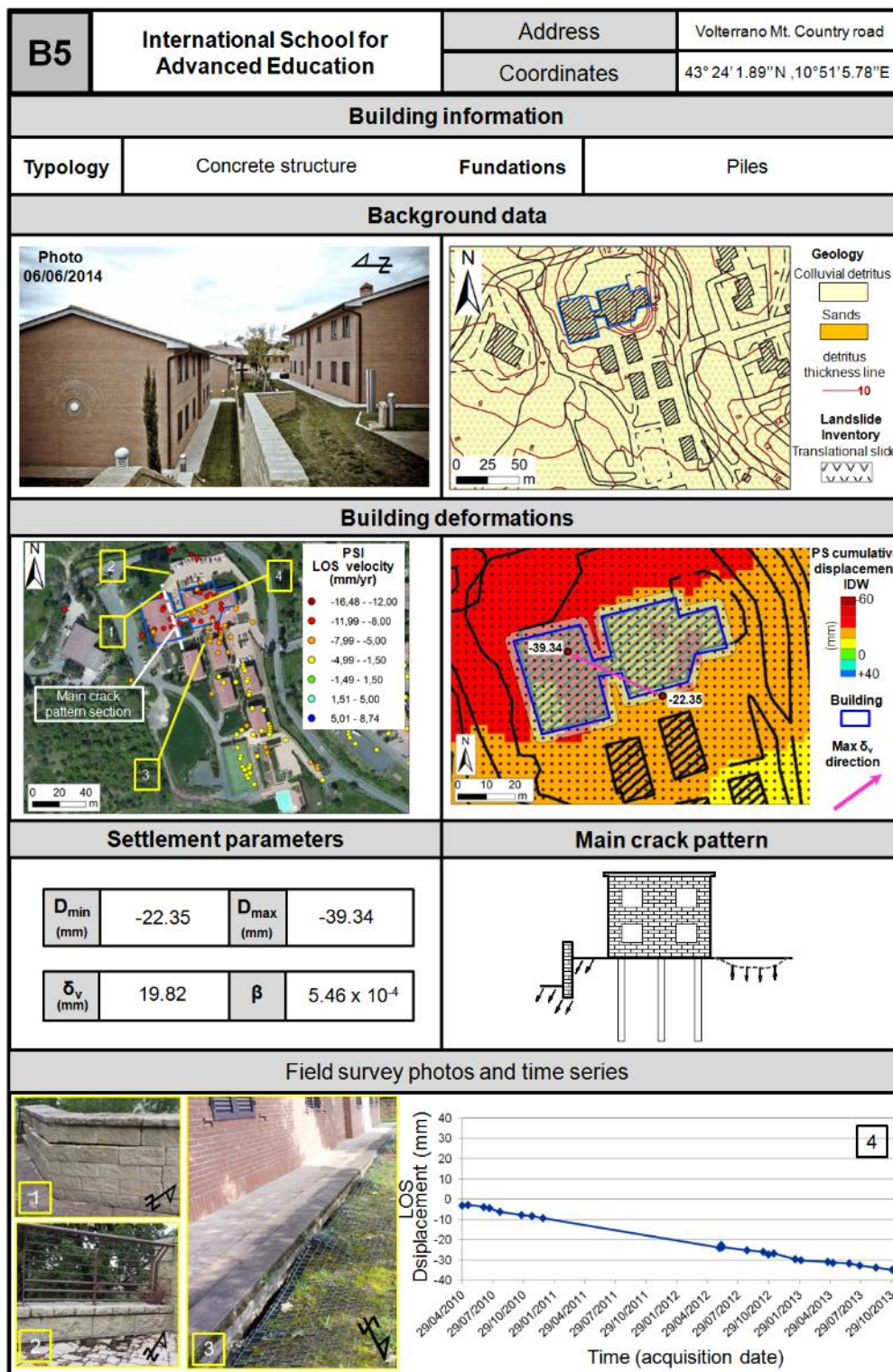


**Figure 9.** Analysis results of building B4: building information, background data, building deformations, settlement parameters, main crack pattern and photos of the field survey.

### 3.3.5. Building B5

Building B5 is the main structure of the modern residential campus owned by the International School for Advanced Education funded by St. Anna School of Advanced Studies of Pisa. The reinforced concrete structure was realized in 2003 using bearing piles for the foundations. It is located at an altitude

of about 330–340 m a.s.l. on colluvial layer, whose thickness is very variable in this area, from 4 m up to 12 m (Figure 10).



**Figure 10.** Analysis results of building B5: building information, background data, building deformations, settlement parameters, main crack pattern, some photos of the field survey and a PS time series (the gap during year 2011 is due to missing acquisitions).

## Deformation Assessment

PSI analysis shows high mean annual motion rates (up to  $-10$  mm/year) and cumulative displacements up to  $-39.34$  mm over the building complex (Figure 10), with an increasing spatial trend from the swimming pool towards SE to NW, where the main building of the campus is located.

## Validation

The estimated maximum  $\delta_v$  is 19.82 mm, and its orientation traces the PSI spatial pattern. *In situ* observations revealed that ground movements mainly correspond to compaction of the soil fill (Figure 9), rather than to structural damages. The more damaged areas are the northward ones, coincident with PS showing highest velocities and maximum cumulative displacements.

## 4. Discussion

We performed a PSI-based methodology exploiting the IDW interpolation to calculate differential settlement parameters of buildings in the southwestern portion of Volterra (Tuscany region, Italy). The analysis of magnitude and direction of movements combined with on-field surveys and observed damages, as well as with background data (*i.e.*, structural typologies, geological setting and landslide inventory) allowed us to better detect and interpret the ground instabilities of the investigated area and how they influence building deformations.

The use of COSMO-SkyMed X-band data significantly improved the level of detail of the analysis on built-up areas and man-made infrastructure, since many targets show up on roofs and facades [11,41,42]. IDW interpolation was confirmed to be a step forward in the PSI data radar interpretation procedure, firstly introduced by [43] and then widely used by the scientific community, extending the point-like information stored in the PS benchmarks.

The five example buildings described in this paper (B1 to B5) are representative of the whole southwestern area of Volterra and characterized by different geological conditions and structural typologies (Table 2).

Within the Volterra sedimentary sequence, the upper calcarenites and sands, which outcrop at altitudes higher than 450 m in the study area, are stable with respect to lower clays and to the colluvial layer that covers the sequence. This was confirmed by the results obtained for the public school (building B1) that is built on a stable sandy formation through direct foundations and shows low values of differential settlement ( $\delta_v = 4.94$  mm and  $\beta = 9.03 \times 10^{-5}$ ), which is consistent with the overall good conditions revealed by on-site surveys.

Conversely, slow-moving landslide phenomena involving clays and colluvial detritus can cause intense damages and differential settlement on buildings. Moreover, the choice of a suitable type of foundation combined with the terrain morphology can play an important role in the occurrence of movements and consequent damages on buildings.

This clearly emerged during the analysis of building B2, which is a private housing estate consisting of two edifices, B2<sub>i</sub> and B2<sub>ii</sub>. Both edifices show high values of angular distortion ( $\beta = 6.04 \times 10^{-4}$  and  $1.84 \times 10^{-4}$ ) and B2<sub>i</sub> also a high  $\delta_v$  value of 20.96 mm, in accordance with the extensive cracks on the facades of building B2<sub>ii</sub> and the vertical split at the mid-length of B2<sub>i</sub>. The structural failures are mainly

due to the very thick colluvial layer that overlaps the clayey basement, covering a morphological scarp, where bearing piles are not effective.

Building B3 and building B4, respectively the supermarket and the alabaster warehouse, are located within a landslide area. This downslope translational ground movement is confirmed by the high mean PSI velocities that reach up to rates of about 6–8 mm/year. In particular, building B4 shows the highest  $\delta_v$  (29.86 mm) and high  $\beta$  value ( $4.52 \times 10^{-4}$ ) due to the significant spatial trend of the movement. On the other hand, building B3 shows the lowest  $\delta_v$  value (4.42 mm), since the highest motion rates are located westwards of the “building area”. The cross-comparison of PSI data,  $\delta_v$  and  $\beta$  values and directions and *in situ* observations revealed that the crack patterns surveyed on both buildings are compatible with ground motion rates due to the slow-moving landslide phenomenon.

Movements detected on the surface by PSI data can also be related to unstable fill soil or embankments allocated for building construction. This is the case of building B5, which is a recently built structure that houses the International School for Advanced Education. PSI data show the highest motion rates of the whole study area, reaching up to mean velocity values of 10–12 mm/year and cumulative displacements of about 35–40 mm at the last acquisition date (15 November 2013). *In situ* checks performed in April–May, 2014, have shown that damages occurred only on the external areas of the structure and clearly evidenced problems with the sediment earthwork.

These examples illustrate well that PSI-based deformation assessment performed at the desk, prior to *in situ* investigations, need to be validated by background data and field survey, in order to better assess the causes of movements and whether the detected motions correspond to visible and effective damages on buildings.

A wide number of limiting criteria for maximum settlement and angular distortion values are available in the geotechnical literature [29–31] and technical standards [28,32]. The maximum allowable settlement and angular distortion can be defined in relation to the type of structure (*i.e.*, stiffness and use), foundation soil and foundation type (piles or direct foundations). For instance, a maximum angular distortion value of  $3 \times 10^{-4}$  can be broadly defined for civil buildings on sandy and clayey terrain [24,29]. As a future outlook for the proposed methodological procedure, a rating system for the admissibility of differential settlement values could be tackled more specifically, according to the criterion of the serviceability limit states and to the temporal coverage of input radar datasets.

## 5. Conclusions

In this paper, we presented a method that effectively exploits COSMO-SkyMed PSI data combined with *in situ* validation campaigns for a single building-scale analysis of differential settlement related to instability. The analysis was performed over the southwestern sector of Volterra in the Tuscany region (Italy), which is a medium built-up area affected by diffuse landslide phenomena. The proposed approach mainly consists of deriving the direction and values of building settlements (differential settlement  $\delta_v$  and angular distortion values  $\beta$ ) from PSI motion rates and then in their cross-comparison with background geological data, constructive features and on-field surveys. A good accordance between the estimated building deformations and on-field damage evidence was found on the five example buildings within the study area. In particular, the lowest vertical differential settlement and angular distortion values ( $4.94$  and  $9.03 \times 10^{-5}$ , respectively) were measured on building B1, which turns out to

lay on stable sandy terrain and is only characterized by good overall conditions. Conversely, high values of  $\delta_v$  and  $\beta$  were computed on buildings B2<sub>i</sub> and B4 ( $\delta_v = 20.96$ ,  $\beta = 6.04 \times 10^{-4}$ , and  $\delta_v = 29.86$ ,  $\beta = 4.52 \times 10^{-4}$ ), in agreement with local geo-morphological conditions and with the directions and width of the extensive cracks observed on those edifice facades.

## Acknowledgments

The authors would like to thank GEOPROGETTI-Studio associato (geologists Francesca Franchi and Emilio Pistilli) for making the geological and geotechnical data on Volterra available.

All of the COSMO-SkyMed SAR images were processed by Telerilevamento Europa by means of the SqueeSAR technique.

The landslide inventory map was provided by the Tuscany region (“Research and Innovation in the environmental field”, 2009) within the DIANA (Dati Interferometrici per l’ANalisi Ambientale) Italian project.

Further data and information on the investigated area of the Volterra site are available on the City Council website: <http://www.comune.volterra.pi.it>.

## Author Contributions

Silvia Bianchini designed research, carried out data interpretation and wrote the manuscript. Fabio Pratesi and Teresa Nolesini improved the quality of the work and contributed to write the paper under the scientific coordination of and with the contribution of Nicola Casagli. All authors contributed to the field survey.

## Conflicts of Interest

The authors declare no conflict of interest.

## References

1. Massonnet, D.; Feigl, K.L. Radar interferometry and its application to changes in the Earth’s surface. *Rev. Geophys.* **1998**, *36*, 441–500.
2. Rosen, P.A.; Hensley, S.; Joughin, I.R.; Li, F.K.; Madsen, S.N.; Rodriguez, E.; Goldstein, R.M. Synthetic aperture radar interferometry. *Proc. IEEE* **2000**, *88*, 333–382.
3. Ferretti, A.; Prati, C.; Rocca, F. Permanent scatterers in SAR interferometry. *IEEE Trans. Geosci. Remote Sens.* **2001**, *39*, 8–20.
4. Colesanti, C.; Wasowski, J. Investigating landslides with space-borne Synthetic Aperture Radar (SAR) interferometry. *Eng. Geol.* **2006**, *88*, 173–199.
5. Cigna, F.; Bianchini, S.; Casagli, N. How to assess landslide activity and intensity with Persistent Scatterer Interferometry (PSI): The PSI-based matrix approach. *Landslides* **2013**, *10*, 267–283, doi:10.1007/s10346-012-0335-7.
6. Notti, D.; Herrera, G.; Bianchini, S.; Meisina, C.; García-Davalillo, J.C.; Zucca, F. A methodology for improving landslide PSI data analysis. *Int. J. Remote Sens.* **2014**, *35*, doi:10.1080/01431161.2014.889864.

7. Tomás, R.; Romero, R.; Mulas, J.; Marturià J.J.; Mallorquí J.J.; Lopez-Sanchez, J.M.; Herrera, G.; Gutiérrez, F.; González, P.J.; Fernández, J.; *et al.* Radar interferometry techniques for the study of ground subsidence phenomena: A review of practical issues through cases in Spain. *Environ. Earth Sci.* **2014**, *71*, 163–181.
8. Heleno, S.I.N.; Oliveira L.G.S.; Henriques, M.J.; Falcão, A.P.; Lima, J.N.P.; Cooksley, G.; Ferretti, A.; Fonseca, A.M.; Lobo-Ferreira, J.P.; Fonseca, J.F.B.D. Persistent scatterers interferometry detects and measures ground subsidence in Lisbon. *Remote Sens Environ.* **2011**, *115*, 2152–2167.
9. Crosetto, M.; Monserrat, O.; Junger, A.; Crippa, B. Persistent scatterer interferometry: Potential and limits. In Proceedings of the 2009 ISPRS Workshop on High-Resolution Earth Imaging for Geospatial Information, Hannover, Germany, 2–5 June 2009.
10. Bianchini, S.; Cigna, F.; Righini, G.; Proietti, C.; Casagli, N. Landslide HotSpot Mapping by means of Persistent Scatterer Interferometry. *Environ. Earth Sci.* **2012**, *67*, 1155–1172.
11. Bianchini, S.; Ciampalini, A.; Raspini, F.; Bardi, F.; di Traglia, F.; Moretti, S.; Casagli N. Multi-temporal evaluation of landslide movements and impacts on buildings in San Fratello (Italy) by means of C- and X-band PSI data. *Pure Appl. Geophys.* **2014**, doi:10.1007/s00024-014-0839-2.
12. Ciampalini, A.; Bardi, F.; Bianchini, S.; del Ventisette, C.; Moretti, S.; Casagli, N. Analysis of building deformation in landslide area using multi-sensor PSInSARTM technique. *Int. J. Appl. Earth Obs. Geoinf.* **2014**, *33*, 166–180.
13. Bianchini, S.; Herrera, G.; Mateos, R.M.; Notti, D.; Garcia, I.; Mora, O.; Moretti, S. Landslide activity maps generation by means of persistent Scatterer Interferometry. *Remote Sens.* **2013**, *5*, 6198–6222.
14. Herrera, G.; Tomás, R.; Monells, D.; Centolanza, G.; Mallorquí J.J.; Vicente, F.; Navarro, V.D.; Lopez-Sanchez, J.M.; Sanabria, M.; Cano, M.; *et al.* Analysis of subsidence using TerraSAR-X data: Murcia case study. *Eng. Geol.* **2010**, *116*, 284–295.
15. Parcharidis, I.; Fomelis, M.; Pavlopoulos, K.; Kourkouli, P. Ground deformation monitoring in cultural heritage areas by time series SAR interferometry: The case of ancient Olympia site (Western Greece). In Proceedings of the 2010 Fringe Conference, ESA, Noordwijk, The Netherlands, 4–7 May 2010.
16. Tapete, D.; Fanti, R.; Cecchi, R.; Petrangeli, P.; Casagli, N. Satellite radar interferometry for monitoring and early-stage warning of structural instability in archaeological sites. *J. Geophys. Eng.* **2012**, *9*, S10–S25.
17. Pratesi, F.; Tapete, D.; Terenzi, G.; del Ventisette, C.; Moretti, S. Structural assessment of case study historical and modern buildings in the florentine area based on a PSI-driven seismic and hydrogeological risk analysis. In *Engineering Geology for Society and Territory*, Proceedings of 2015 IAEG, Turin, Italy, 5–8 September 2014. Lollino, G., Giordan, D., Thuro, K., Carranza-Torres, C., Wu, F., Marinis, P., Delgado, C.; pp. 345–349.
18. Karila, K.; Karjalainen, M.; Hyypä J. Urban land subsidence studies in Finland using Synthetic Aperture Radar images and coherent targets. *Photogramm. J. Finland* **2005**, *19*, 43–53.
19. Bru, G.; Herrera, G.; Tomás, R.; Duro, J.; de la Vega, R.; Mulas J. Control of deformation of buildings affected by subsidence using persistent scatterer interferometry. *Struct. Infrastruct. Eng.* **2010**, *9*, 188–200.

20. Arangio, S.; Calò, F.; Di Mauro, M.; Bonano, M.; Marsella, M.; Manunta, M. An application of the SBAS-DInSAR technique for the Assessment of structural damage in the city of Rome. *Struct. Infrastruct. Eng.* **2014**, *10*, 1469–1483
21. Sousa, J.J.; Bastos, L. Multi-temporal SAR interferometry reveals acceleration of bridge sinking before collapse. *Nat. Hazards Earth Syst. Sci.* **2013**, *13*, 659–667.
22. Tomás, R.; García-Barba, J.; Cano, M.; Sanabria, M.P.; Ivorra, S.; Duro, J.; Herrera, G. Subsidence damage assessment of a gothic church using Differential Interferometry and field data. *Struct. Health Monit.* **2012**, *11*, 751–762.
23. Cascini, L.; Peduto, D.; Pisciotta, G.; Arena, L.; Ferlisi, S.; Fornaro, G. The combination of DInSAR and facility damage data for the updating of slow-moving landslide inventory maps at medium scale. *Nat. Hazards Earth Syst. Sci.* **2013**, *13*, 1527–1549.
24. Sanabria, M.P.; Guardiola-Albert, C.; Tomás, R.; Herrera, G.; Prieto, A.; Sánchez, H.; Tessitore, S. Subsidence activity maps derived from DInSAR data: Orihuela case study. *Nat. Hazards Earth Syst. Sci.* **2014**, *14*, 1341–1360.
25. Pratesi, F.; Nolesini, T.; Bianchini, S.; Leva, D.; Lombardi, L.; Fanti, R.; Casagli, N. Early warning GBInSAR-based method for monitoring Volterra (Tuscany, Italy) city walls. *IEEE J. Sel. Top. Appl. Earth Obs. Remote Sens.* **2015**, doi:10.1109/JSTARS.2015.2402290.
26. Shepard, D. A two-dimensional interpolation function for irregularly-spaced data. In Proceedings of the 1968 ACM National Conference, New York, NY, USA, 27–29 August 1968.
27. Tobler, W. A computer movie simulating urban growth in the Detroit region. *Econ. Geogr.* **1970**, *46*, 234–240.
28. Eurocode—Basis of Structural Design. Available online: [http://www.unirc.it/documentazione/materiale\\_didattico/599\\_2010\\_260\\_7481.pdf](http://www.unirc.it/documentazione/materiale_didattico/599_2010_260_7481.pdf) (accessed on 12 October 2014).
29. Ricceri, G.; Soranzo, M. An analysis on allowable settlement of structures. *Riv. Ital. Geotec.* **1985**, *4*, 177–188.
30. Skempton, A.W.; McDonalds, D.H. Allowable settlements of buildings. *Proc. ICE.* **1956**, *5*, 727–768.
31. Bjerrum, L. Allowable settlement of structures. In Proceedings of the 3rd European Conference on Soil Mechanics and Foundation Engineering, Wiesbaden, Germany, 15–18 October 1963.
32. EC 1994—Eurocode 7, 1994. Geotechnical Design. Available online: <https://law.resource.org/pub/eur/ibr/en.1997.1.2004.pdf> (accessed on 10 October 2014).
33. Bowles, J.E. *Foundation Analysis and Design*; Mc Graw Hill Publications: New York, NY, USA, 1977.
34. Sabelli, R.; Cecchi, G.; Esposito, A.M. *Mura etrusche di Volterra. Conservazione e Valorizzazione*; Bientina, Ita.: La Grafica Pisana, Italy, 2012.
35. Terrenato, N. The romanization of Volaterrae (Volterra). *J. Roman Stud.* **1998**, *88*, 94–114.
36. Ferretti, A.; Fumagalli, A.; Novali, F.; Prati, C.; Rocca, F.; Rucci, A. A new algorithm for processing interferometric data stacks: SqueeSAR™. *IEEE Trans. Geosci. Remote Sens.* **2011**, *49*, 3460–3470.
37. Bamler, R.; Hartl, P. Synthetic aperture radar interferometry. *Inverse Problems* **1998**, *14*, R1–R54.
38. Zhang, Y.; Xie, C.; Shao, Y.; Yuan, M. Adaptive spatial filtering of interferometric data stack oriented to distributed scatterers. *Int. Arch. Photogramm. Remote Sens. Spat. Inf. Sci.* **2013**, *XL-7/W1*, 173–178.

39. Righini, G.; Pancioli, V.; Casagli, N. Updating landslide inventory maps using Persistent Scatterer Interferometry (PSI). *Int. J. Remote Sens.* **2012**, *33*, 2068–2096.
40. AAVV. Indagini Geognostiche e Sismiche per L'analisi Dell'assetto Geologico e Geomorfologico del Versante sud di Volterra, 2010. Available online: <http://www.comune.volterra.pi.it> (accessed on 10 October 2014).
41. Gernhardt, S.; Adam, N.; Eineder, M.; Bamler, R. Potential of very high resolution SAR for persistent scatterer interferometry in urban areas. *Ann. GIS* **2010**, *16*, 103–111.
42. Roth, A. TerraSAR-X: A new perspective for scientific use of high resolution spaceborne SAR data. In Proceedings of the 2nd GRSS/ISPRS Joint Workshop on Remote Sensing and Data Fusion on Urban Areas, Berlin, Germany, 22–23 May 2003.
43. Farina, P.; Casagli, N.; Ferretti, A. Radar-interpretation of InSAR measurements for landslide investigations in civil protection practices. In Proceedings of the 1st North American Landslide Conference, Vail, CO, USA, 3–8 June 2007.

© 2015 by the authors; licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution license (<http://creativecommons.org/licenses/by/4.0/>).