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Comparison of the efficiencies of class D and class E rectifiers **Proceedings of 36th Midwest Symposium on Circuits and**

Questa è la Versione finale referata (Post print/Accepted manuscript) della seguente pubblicazione:

Original Citation:

Comparison of the efficiencies of class D and class E rectifiers Proceedings of 36th Midwest Symposium on Circuits and Systems / A. Reatti; M.K. Kazimierczuk. - ELETTRONICO. - (1993), pp. 871-874. (Intervento presentato al convegno This paper appears in: Circuits and Systems, 1993., Proceedings of the 36th Midwest Symposium on) [10.1109/MWSCAS.1993.343206].

Availability:

This version is available at: 2158/645173 since:

Published version:

DOI: 10.1109/MWSCAS.1993.343206

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Comparison of the Efficiencies of Class D and Class E Rectifiers

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Abstract - The efficiencies of the Class D and Class E rectifiers are compared considering power losses in the parasitic resistances of capacitors, inductors and transformer windings, and conduction losses in the diodes. Equations for efficiency are plotted as functions of the output current with an output voltage $V_O = 5$ V and a maximum output power $P_O = 100$ W. It is shown that center-tapped rectifiers are the most suitable for low-voltage applications. Class E rectifier efficiency is higher than that of Class D circuit in the higher range of the output current. The Class E circuit is more suitable for low-current high-frequency applications. The results of this paper can be used by designers in selecting circuits with a better efficiency with respect to their specific load requirements.

I. INTRODUCTION

Resonant dc-dc converters represent the most promising solution to the problem of size and weight reduction of off-line power supplies. The inverter section of the converter contains a resonant circuit at the output, operated as a sinusoidal current or voltage source [1]-[5]. The dc-dc power conversion is achieved by rectifying these waveforms. Power supplies for VLSI circuits must operate at a high-efficiency with a low-voltage, high-current output, e.g., 3.3 V or 5 V and 10 A. If off-line power supplies are used, the inverter section has a high-efficiency, e.g., 95 % [2]-[5]. Therefore, the total efficiency of the converter is mostly affected by the rectifier, where high currents flow through the circuit components. Because of this, one of the major problems facing designers is the rectifier topology which optimizes the converter efficiency.

The purpose of this paper is to compare the efficiencies of Class D rectifiers [2]-[4] [6] and Class E rectifiers [7]-[9] and determine which circuits are more suitable for applications in converters for VLSI circuits. The equations of rectifier efficiencies were determined as functions of the output current taking into account the parasitic resistances of diodes, capacitors, inductors, transformer windings, as well as diode offset voltages. The significance of the paper is that the presented method allows the designers to select the rectifier circuit which can be operated with higher efficiency, once specific applications in are given.

II. DETERMINATION OF THE RECTIFIER EFFICIENCIES

The analyses of rectifiers are carried out under the following assumptions:

1) The diode in the ON state is modelled by a series combination of a constant-voltage battery V_F and a constant resistance R_F , where V_F represents the diode threshold voltage and R_F diode forward resistance. The diode in the OFF state is modelled by an open switch. According to this assumption, the conduction loss in a diode is expressed as follows

$$P_D = V_F I_{D(AV)} + R_F I_{Drms}^2 \quad (1)$$

where $I_{D(AV)}$ and I_{Drms} are the average and rms values of the current through the diode, respectively.

2) The voltage-driven rectifiers are driven by an ideal sinusoidal voltage source and the amplitude of the input voltage V_{Rim} is much higher than V_F . The current-driven rectifiers are driven by an ideal sinusoidal current source.

4) Filter inductance L_f in the voltage-driven rectifiers is large enough that the current ripple is negligible with respect to the dc output current I_O . Inductor L_f equivalent resistance is r_f .

5) Core losses in the transformer are assumed to be much smaller than copper losses. Copper losses are evaluated considering the equivalent resistance of the windings as it is seen at the terminals of the secondary winding r_{Cu} .

6) Losses in the capacitors are evaluated considering their equivalent series resistances. The equivalent series resistance of the filter capacitor is R_{ESRf} and equivalent series resistance of the parallel capacitor in the Class E rectifier is R_{ESR} .

Fig. 1 shows the Class D current-driven rectifier circuits, including the insulation transformer. In the half-wave rectifier, the average and the rms values of the current through each diode are $I_{D(AV)} = I_O$ and $I_{Drms} = \pi I_O / 2$, respectively. The rms value of the current through the filter capacitor is $I_{C(AV)} = I_O$ and $I_{Crms} = \pi I_O / 2$. The rms value of the current through the secondary winding of the transformer and blocking capacitor C_c is $I_{Curms} = \pi I_O / \sqrt{2}$. Since the output power delivered to load resistance R_L is $P_O = R_L I_O^2$, the rectifier efficiency is

$$\eta_{DCHW} = \left[1 + \frac{2V_F}{V_O} + \frac{\pi^2 R_F}{2R_L} + \frac{r_{ESRf}}{R_L} \left(\frac{\pi^2}{4} - 1 \right) + \frac{\pi^2 r_{Cu}}{2R_L} + \frac{\pi^2 r_{ESR1}}{2R_L} \right]^{-1} \quad (2)$$

In the Class D, current-driven, center-tapped rectifier, the average and rms values of the current through each diode modify as $I_{D(AV)} = I_O / 2$ and $I_{Drms} = \pi I_O / 4$, respectively. Moreover, the rms current through the filter capacitor is

This work was supported by National Science Foundation under Grant ECS-8922695 and by Magnetek S.p.A. - Italian Division

$I_{Cfrms} = I_O(\pi^2/8-1)^{1/2}$ and through the transformer secondary winding is $I_{Curms} = \pi I_O/4$. Since an equivalent resistance $r_{Cu}/2$ in series with each secondary winding has been considered, the final expression for the efficiency of the Class D, current-driven rectifier is

$$\eta_{DCCT} = \left[1 + \frac{V_F}{V_o} + \frac{\pi^2 R_F}{8 R_L} + \frac{r_{ESRf}}{R_L} \left(\frac{\pi^2}{8} - 1 \right) + \frac{\pi^2 r_{Cu}}{16 R_L} \right]^{-1} \quad (3)$$

Fig. 1. Current-driven Class D rectifiers: (a) Half-wave circuit. (b) Center-tapped circuit. (c) Full Bridge circuit.

In the Class D, current-driven, full-bridge rectifier, conduction losses in each diode and in the filter capacitor are the same as in center-tapped rectifier. Since two diodes conduct simultaneously, the overall power loss in diode parasitics is doubled. The transformer power loss is twice that in the center-tapped rectifier. As a result, the expression for the full-bridge rectifier efficiency becomes

$$\eta_{DCFB} = \left[1 + \frac{2V_F}{V_o} + \frac{\pi^2 R_F}{4 R_L} + \frac{r_{ESRf}}{R_L} \left(\frac{\pi^2}{8} - 1 \right) + \frac{\pi^2 r_{Cu}}{8 R_L} \right]^{-1} \quad (4)$$

The circuits of the Class D, voltage-driven rectifiers are shown in Fig. 2. According to assumption (4), the input current of the Class D, voltage-driven rectifiers is a square wave, varying from $-I_O/2$ and $I_O/2$. Because of this, the average value of the current through each diode is $I_{D(AV)} = I_O/2$ and its rms value is $I_{Drms} = I_O/\sqrt{2}$. The rms value of the current through inductor L_f and the transformer secondary winding are $I_{Lfrms} = I_O$ and $I_{Curms} = I_O/2$, respectively. The rms value of the current in the filter capacitor ESR is $I_{Cfrms} = 0.2346 I_O R_L / f L_f$. As

a result, the expression for the efficiency of the Class D, voltage-driven, half-wave rectifier is given by

$$\eta_{DVCT} = \left[1 + \frac{V_F}{V_o} + \frac{R_F}{R_L} + \frac{r_f}{R_L} + \frac{0.2346^2 r_{ESRf} R_L}{f^2 L_f^2} + \frac{r_{Cu}}{4 R_L} \right]^{-1} \quad (5)$$

Fig. 2. Voltage-driven Class D rectifiers: (a) Half-wave circuit. (b) Center-tapped circuit. (c) Full-bridge circuit.

In the Class D, voltage-driven, center-tapped rectifier of Fig. 2(b), the output current I_O flows through diodes D_1 and D_2 for half a period. Consequently, the average and rms values of the current through each diode are as in the half-wave rectifier. The rms current through the filter capacitor is $I_{Cfrms} = 0.0337 I_O R_L / f L_f$. The rms value of the current through the secondary winding is equal to the output current I_O . Because of this, the efficiency of the Class D, center-tapped, voltage-driven rectifier is expressed as

$$\eta_{DVCT} = \left[1 + \frac{V_F}{V_o} + \frac{R_F}{R_L} + \frac{r_f}{R_L} + \frac{0.0337^2 r_{ESRf} R_L}{f^2 L_f^2} + \frac{r_{Cu}}{R_L} \right]^{-1} \quad (6)$$

The rms values of the currents through the Class D, full-bridge, voltage-driven rectifier of Fig. 2(c) are the same as those evaluated for the center-tapped, voltage-driven rectifier. Since two diodes conduct simultaneously in the full-bridge rectifier, the expression for its efficiency is as follows

$$\eta_{DVFB} = \left[1 + \frac{2V_F}{V_o} + \frac{2R_F}{R_L} + \frac{r_f}{R_L} + \frac{0.0337^2 r_{ESRf} R_L}{f^2 L_f^2} + \frac{r_{Cu}}{R_L} \right]^{-1} \quad (7)$$

Fig. 3(a) shows the circuits of the Class E, current-driven, half-wave rectifier. The rms value of the current through diodes D_1 is given by

$$I_{D_{rms}} = I_o \left[D + \frac{2\pi D + \sin\phi \cos\phi}{4\pi \sin^2(\phi + 2\pi D)} + \frac{3}{4\pi \tan(\phi + 2\pi D)} - \frac{\cos\phi}{\pi \sin(\phi + 2\pi D)} \right]^{1/2} \quad (8)$$

where ϕ is the turn-on delay angle of diode D_1 and D is its on-duty cycle. The relationships among delay angle ϕ , load resistance R_L , and duty cycle D are given in [9]. Similarly, the rms value of the current through the parallel capacitor C_f is

$$I_{C_{rms}} = I_o \left[1 - D + \frac{2\pi(1-D) - \sin\phi \cos\phi}{4\pi \sin^2(\phi + 2\pi D)} - \frac{3}{4\pi \tan(\phi + 2\pi D)} + \frac{\cos\phi}{\pi \sin(\phi + 2\pi D)} \right]^{1/2} \quad (9)$$

The current through the secondary winding of the transformer and filter capacitor C_f is equal to the current of the source, that is, the ac component of ni . As a result, we have

$$I_{C_{rms}} = I_{C_{fms}} = \frac{I_o}{\sqrt{2} \sin(\phi + 2\pi D)} \quad (10)$$

Considering an equivalent resistance $r_{Cu}/2$ in series with each secondary winding, the efficiency of the Class E, current-driven, half-wave rectifier is determined as follows

$$\eta_{ECHW} = \left\{ 1 + \frac{V_F}{V_o} + \frac{R_F}{R_L} \left[D + \frac{2\pi D + \sin\phi \cos\phi}{4\pi \sin^2(\phi + 2\pi D)} + \frac{3}{4\pi \tan(\phi + 2\pi D)} - \frac{\cos\phi}{\pi \sin(\phi + 2\pi D)} \right] + \frac{r_{ESR}}{R_L} \left[1 - D + \frac{2\pi(1-D) - \sin\phi \cos\phi}{4\pi \sin^2(\phi + 2\pi D)} - \frac{3}{4\pi \tan(\phi + 2\pi D)} + \frac{\cos\phi}{\pi \sin(\phi + 2\pi D)} \right] + \frac{r_{Cu}}{2R_L \sin^2(\phi + 2\pi D)} + \frac{r_{ESRf}}{2R_L \sin^2(\phi + 2\pi D)} \right\}^{-1} \quad (11)$$

In the Class E, current-driven, center-tapped rectifier of Fig. 3(b), the amplitude of the current through each diode is one half of that flowing through the diode of the half-wave rectifier. Therefore, the conduction losses in each diode due to the forward voltage drop V_F are one half and the loss due to the forward resistance r_F is four times lower than that in the diode of the Class E half-wave rectifier. Also the power losses in parallel capacitors C_1 and C_2 and in the transformer windings are reduced by a factor of four. Moreover, in the Class E center-tapped rectifier, the current through filter capacitor C_f is nearly zero. This results in no loss operation of capacitor C_f . Because all of this, the efficiency of the Class E, current-driven, center-tapped rectifier is expressed as

$$\eta_{ECT} = \left\{ 1 + \frac{V_F}{V_o} + \frac{R_F}{2R_L} \left[D + \frac{2\pi D + \sin\phi \cos\phi}{4\pi \sin^2(\phi + 2\pi D)} + \frac{3}{4\pi \tan(\phi + 2\pi D)} - \frac{\cos\phi}{\pi \sin(\phi + 2\pi D)} \right] + \frac{r_{ESR}}{2R_L} \left[1 - D + \frac{2\pi(1-D) - \sin\phi \cos\phi}{4\pi \sin^2(\phi + 2\pi D)} - \frac{3}{4\pi \tan(\phi + 2\pi D)} + \frac{\cos\phi}{\pi \sin(\phi + 2\pi D)} \right] + \frac{r_{Cu}}{8R_L \sin^2(\phi + 2\pi D)} \right\}^{-1} \quad (12)$$

Fig. 3. Current-driven Class E rectifiers: (a) Half-wave circuit. (b) Center-tapped circuit.

The efficiencies of the Class D and Class E rectifiers are plotted in Fig. 4 as functions of the output current assuming a 5 V constant output voltage operation. According to the data measured while testing a 1 MHz, 100 W, Class E, center-tapped rectifier, the values of the components were chosen as follows: $V_F = 0.3$ V, $R_F = 0.033$ Ω , $R_{ESRf} = 0.04$ Ω , $r_f = 0.125$ Ω , $L_F = 5$ μ H, $r_{Cu} = 0.01$ Ω , and $D_{MAX} = 0.45$. The efficiencies of the Class E rectifiers are plotted for $r_{ESR} = 0.01$ Ω and $r_{ESR} = 0.04$ Ω . All Class D rectifiers have high efficiencies at low loads while the Class E, half-wave circuit has a poor efficiency over the entire load range even if r_{ESR} is low. Since only the current-driven, center-tapped Class D and Class E rectifiers have an efficiency greater than 78 % over the entire load range, they result suitable for low output voltage applications. The efficiency of Class D rectifier decreases from 94 % to 85 % for an output current increasing from 0 to 12 A and decreases to 78 % at the full load. The Class E circuit efficiency slightly decreases from 88 % to 83 % for I_o increasing from 10 % to 100 % of the maximum value.

As shown in Fig. 5, Class D rectifier has a better performance in low current applications, i.e., $I_o < 10$ A. The experimental waveform of the diode voltage depicted in Fig. 6 demonstrates that the Class E rectifier is not affected by switching losses and parasitic oscillations occurring at high-frequencies. Therefore, it represents an appropriate solution for high-power density, high-output current applications in the megahertz range.

III. CONCLUSIONS

The efficiencies of Class D, current-driven and voltage-driven rectifiers, along with those of Class E current-driven rectifiers have been analytically evaluated and plotted

versus the dc load current I_O , assuming a constant output voltage $V_O = 5$ V operation of the rectifiers. Circuit parameters have been chosen according to those measured in experimentally testing a 100 W, 1 MHz Class E, current-driven, center-tapped rectifier with an output voltage $V_O = 5$ V. Only the Class D and Class E, current-driven, center-tapped rectifiers operate with high efficiencies over the entire load range. The Class E rectifier has a higher efficiency for a high load current and has zero switching losses. Therefore, it is suitable for high-frequency, and high output current applications. The presented method can be applied to other rectifier circuits to select the rectifier operating with the higher efficiency for any given application. Because of this, this paper represents a helpful tool in the optimization of the efficiency of power converters.

Fig. 4. Efficiency of Class D and Class E rectifiers as functions of the output current I_O . (a) Efficiency of Class D, current-driven rectifiers. (b) Efficiency of Class D, voltage-driven rectifiers. (c) Efficiency of Class E, current-driven rectifiers.

Fig. 5. Efficiency of Class D current-driven, center-tapped rectifier η_{DCCT} and efficiency of Class E, current-driven, center-tapped rectifier η_{ECCT} as functions of output current I_O .

Fig. 6. Experimental waveform of the voltage across one diode of Class E, current-driven, center-tapped rectifier measured at the frequency $f = 1$ MHz, with an output voltage $V_O = 5$ V, and an output current $I_O = 5$ A.

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