# Mitigating baryonic effects with a theoretical error covariance

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# ABSTRACT

One of the primary sources of uncertainties in modelling the cosmic-shear power spectrum on small scales is the effect of baryonic physics. Accurate cosmology for stage-IV surveys requires knowledge of the matter power spectrum deep in the non-linear regime at the per cent level. Therefore, it is important to develop reliable mitigation techniques to take into account baryonic uncertainties if information from small scales is to be considered in the cosmological analysis. In this work, we develop a new mitigation method for dealing with baryonic physics for the case of the shear angular power spectrum. The method is based on an augmented covariance matrix that incorporates baryonic uncertainties informed by hydrodynamical simulations. We use the results from 13 hydrodynamical simulations and the residual errors arising from a fit to a  $\Lambda$ CDM model using the extended halo model code HMCODE to account for baryonic physics. These residual errors are used to model a so-called theoretical error covariance matrix that is added to the original covariance matrix. In order to assess the performance of the method, we use the 2D tomographic shear from four hydrodynamical simulations that have different extremes of baryonic parameters as mock data and run a likelihood analysis comparing the residual bias on  $\Omega_m$  and  $\sigma_8$  of our method and the HMCODE for an LSST-like survey. We use different modelling of the theoretical error covariance matrix to test the robustness of the method. We show that it is possible to reduce the bias in the determination of the tested cosmological parameters at the price of a modest decrease in the precision.

Key words: cosmology: observations – large-scale structure of Universe.

# **1 INTRODUCTION**

One of the goals of modern cosmology is to uncover the nature of dark matter and dark energy. Current and new instruments aim at obtaining data with increasing quality and quantity. Surveys of galaxies such as the *Extended Baryon Oscillation Spectroscopic Survey* (eBOSS;<sup>1</sup> eBOSS Collaboration 2021) and the previous phases of the *Sloan Digital Sky Survey* (SDSS; Eisenstein et al. 2011; Blanton et al. 2017), the *Hyper Suprime-Cam Subaru Strategic Program* (HSC-SSP;<sup>2</sup> Hikage et al. 2019), the *Kilo-Degree Survey* (KiDS;<sup>3</sup> Hildebrandt et al. 2017; Heymans et al. 2021), and the *Dark Energy Survey* (DES;<sup>4</sup> Abbott et al. 2018) have already delivered an outstanding amount of results. And future surveys such as the *Dark Energy Spectroscopic Instrument* (DESI;<sup>5</sup> DESI Collaboration 2016), the *Vera C. Rubin Observatory Legacy Survey of Space and* 

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<sup>1</sup>www.sdss.org/surveys/eboss <sup>2</sup>hsc.mtk.nao.ac.jp/ssp <sup>3</sup>kids.strw.leidenuniv.nl <sup>4</sup>www.darkenergysurvey.org <sup>5</sup>www.desi.lbl.gov *Time* (LSST;<sup>6</sup> Ivezić et al. 2019), *Euclid*<sup>7</sup> (Laureijs et al. 2011), and the *Nancy Grace Roman Space Telescope*<sup>8</sup> (Spergel et al. 2015) will provide even more accurate information.

In order to extract cosmological information from these data, it is important to have an accurate theoretical modelling of the measured observables. One of the key obstacles in the interpretation of weak lensing measurements is the modelling of baryonic feedback at small scales. For a recent review of the challenges of baryonic feedback and relevant references see, e.g. Chisari et al. (2019).

State-of-the-art hydrodynamical simulations allow the study of the impact of baryonic feedback galaxy formation dynamics on the matter power spectrum. However, these simulations cannot predict the behaviour of feedback processes from first principles and several phenomenological parameters must be assumed. Therefore, there are uncertainties in the predictions of baryonic feedback from these simulations since there is a range of different values for these parameters that can be used.

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The main methods used for mitigating baryonic uncertainties consist on using the information from current cosmological hydrodynamical simulations to:

(i) Choose a scale ('scale-cut') below which one cannot trust the theoretical modelling of the power spectrum (Krause et al. 2017);

(ii) Use principal component analysis to find the modes that are the most significant in describing baryonic impacts and marginalize over them (Eifler et al. 2015; Huang et al. 2019);

(iii) Construct self-calibrated phenomenological models that mimic the baryonic effects in the structure of dark matter haloes (Mead et al. 2015).

DES and HSC have chosen to mitigate baryonic uncertainties using scale cuts to eliminate the impact of baryonic physics as modelled by either the Over Whelmingly Large Simulations (OWLS) hydrodynamical simulations (van Daalen et al. 2011) in the case of DES (Krause et al. 2017), or by a modification of the dark matter power spectrum due to the active galactic nucleus (AGN) feedback modelled by a fitting function in the case of HSC (Hikage et al. 2019; Hamana et al. 2020). KiDS, on the other hand, uses in their fiducial analysis a baryon feedback parameter (Asgari et al. 2021).

In a recent study, Huang et al. (2019) showed that in the case of weak lensing for the LSST there are still residual errors using these mitigation methods. In this paper, we aim to mitigate these residual errors, particularly the ones arising from a likelihood analysis using hydrodynamical simulations as input data and a theoretical model using HMCODE (Mead et al. 2015).

In order to develop a new mitigation method for the residual errors in an LSST-like tomographic weak lensing survey, we adapt the general statistical approach developed by Baldauf et al. (2016; see also Audren et al. 2013). This method incorporates the effects of nonnegligible theoretical uncertainties in the covariance matrix, leading to a smooth suppression of modes where these uncertainties are larger. This method was recently applied for the case of unknown non-linear corrections in the matter and galaxy power spectra in Chudaykin, Ivanov & Simonovic (2021).

This paper is organized as follows. In Section 2 we review the theoretical modelling of the convergence power spectrum and its Gaussian covariance matrix. Section 3 presents the main ingredients of a general proposal to include theoretical errors in a covariance matrix proposed in Baldauf et al. (2016). In Section 4 we adapt this method to construct covariance matrices aimed at mitigating residual baryonic uncertainties using a set of hydrodynamical simulations and their best fits from a likelihood analysis that employed HMCODE to model baryonic effects. In Section 5 we perform a simulated likelihood analysis for an LSST-like weak lensing survey with different covariance matrices and find that the augmented covariance matrices in fact result in an increased accuracy (less biased inferred cosmological parameters) at the expense of a modest decrease in the precision (larger error bars). We discuss our findings in Section 6 and present our conclusions in Section 7.

# 2 CONVERGENCE POWER SPECTRUM AND ITS GAUSSIAN COVARIANCE MATRIX

Here we are interested in the convergence angular power spectrum between two tomographic bins *i* and *j*,  $C_{\kappa\kappa}^{ij}(\ell)$  given in the Limber approximation by

$$C_{\kappa\kappa}^{ij}(\ell) = \int_0^{\chi_h} \mathrm{d}\chi \, \frac{g^i(\chi)g^j(\chi)}{\chi^2} \, P_m\left(\frac{\ell+1/2}{\chi}, z(\chi)\right),\tag{1}$$

where  $\chi$  is the comoving radial distance between the observer and the object, the lens efficiency  $g^i(\chi)$ , in a flat cosmology, is written for source galaxies with redshift distribution  $n^i(z)$  as

Mitigation baryonic effects

$$g^{i}(\chi) \equiv \frac{3\Omega_{m}H_{0}^{2}}{2c^{2}a(\chi)} \int_{0}^{\chi_{h}} dz \, n^{i}(z) \frac{(\chi'(z) - \chi)\chi}{\chi'(z)} \,\Theta(\chi'(z) - \chi), \qquad (2)$$

with  $\Omega_{\rm m}$  the matter density parameter, *c* the speed of light,  $a(\chi)$  is the expansion scale factor as a function of  $\chi$ ,  $H_0$  the Hubble constant taken at the present day and  $\Theta(\chi'(z)-\chi)$  is the heavyside step function. In this preliminary analysis, we will not consider effects such as bias corrections to shear and intrinsic alignments.

The Gaussian covariance of projected convergence power spectra can be expressed as (Hu & Jain 2004)

$$\operatorname{Cov}_{G}(C^{ij}_{\kappa\kappa}(\ell), C^{pq}_{\kappa\kappa}(\ell')) = \left\langle \Delta C^{ij}_{\kappa\kappa}(\ell) \Delta C^{pq}_{\kappa\kappa}(\ell') \right\rangle = \frac{2\pi \, \delta_{\ell\ell'}}{A \, \ell \, \Delta \ell} \left[ \bar{C}^{ip}_{\kappa\kappa}(\ell) \bar{C}^{jq}_{\kappa\kappa}(\ell') + \bar{C}^{iq}_{\kappa\kappa}(\ell) \bar{C}^{jp}_{\kappa\kappa}(\ell') \right], \tag{3}$$

with

$$\bar{C}^{ij}_{\kappa\kappa}(\ell) = C^{ij}_{\kappa\kappa}(\ell) + \delta_{ij} \frac{(\sigma^i)^2}{n^i_{\Omega}},\tag{4}$$

where  $\Omega$  is the angular survey area,  $\Delta \ell$  is the angular bin width (as described in Section 2),  $n_{\Omega}^{i}$  is the area density of galaxies in redshift bin *i* and  $\sigma^{i}$  is the Gaussian shape noise per component. For LSST Y10, we adopt the requirements of The LSST Dark Energy Science Collaboration (2018) with a survey area  $\Omega$  of 14 300 deg<sup>2</sup>, shape noise of  $\sigma^{i} = 0.26$  and  $n_{\Omega}^{i} = 5.4$  arcmin<sup>-2</sup> for all bins. Furthermore, we use a gravity-only model for the non-linear two-point function from Takahashi et al. (2012) in CosmoLike (Krause & Eifler 2017), in order to generate the analytical Gaussian covariance matrix.

The covariance matrix has contributions from a Gaussian part and a non-Gaussian part composed of the connected four-point (trispectrum) contributions and supersample covariance (Hu & Jain 2004; Krause et al. 2017; Barreira, Krause & Schmidt 2018). The Gaussian contribution is the dominant one as seen in a  $\chi^2$  analysis for DES-Y3 set-up (Friedrich et al. 2020) and for stage-IV experiments (Barreira et al. 2018). As an initial test of our mitigation method, we will be interested in incorporating errors from residual baryon effects in the Gaussian covariance matrix.

# **3 MITIGATING UNCERTAINTIES WITH MODIFIED COVARIANCES**

In this section, we briefly review the strategy described in Baldauf et al. (2016) to model a general residual error as a Gaussian random variable that can be marginalized over resulting in an additional contribution to the covariance matrix.

Let **x** be the data vector, and **t** the theoretical vector. The error vector **e** being the residual between the data vector and its corresponding best-fitting theory, with mean value  $\bar{\mathbf{e}}$ . We assume **e** to follow a Gaussian distribution

$$P_{e} \propto \exp\left[-\frac{1}{2}(\mathbf{e}-\bar{\mathbf{e}})C_{e}^{-1}(\mathbf{e}-\bar{\mathbf{e}})\right],$$
(5)

with a covariance matrix  $C_e$  given by

$$C_e^{ab} = \left\langle e^a \, e^b \right\rangle - \bar{e}^a \, \bar{e}^b. \tag{6}$$

In this section, for simplicity, we will use *a* and *b* as the indexes for the angular bins. We parametrize  $\langle e^a e^b \rangle$  as

$$\left\langle e^a \, e^b \right\rangle \equiv E_a \, \rho_{ab} \, E_b, \tag{7}$$

where we introduced a quantity we call the envelope  $E_a = E(\ell_a)$  and assume that the correlation coefficient  $\rho_{ab}$  is Gaussian and it depends only on the distance between two bins centred at  $\ell_a$  and  $\ell_b$ . Thus,

$$\rho_{ab} \equiv \exp\left[-\frac{(\ell_a - \ell_b)^2}{2L^2}\right].$$
(8)

Hence, we can fully describe this mitigation approach by the smooth envelope  $E(\ell)$  and the correlation  $\ell$ -scale L, which specifies the minimal scale of variation of the theoretical model. Note that including the correlation coefficient is one important difference compared to the method of Audren et al. (2013), where fluctuations due to theoretical uncertainties in all bins are treated as independent.

Assuming a Gaussian likelihood, we can include the theoretical error as

$$\mathcal{L}_e \propto \exp\left\{-\frac{1}{2}\left[(\mathbf{x}-\mathbf{t}-\mathbf{e})\,C_d^{-1}(\mathbf{x}-\mathbf{t}-\mathbf{e})+(\mathbf{e}-\bar{\mathbf{e}})\,C_e^{-1}(\mathbf{e}-\bar{\mathbf{e}})\right]\right\},\tag{9}$$

where  $C_d$  is the usual data covariance matrix and  $C_e$  the error covariance matrix. We can marginalize the likelihood over the errors **e** to obtain:

$$\mathcal{L} \propto \exp\left[-\frac{1}{2}(\mathbf{x} - \mathbf{t} - \bar{\mathbf{e}})C^{-1}(\mathbf{x} - \mathbf{t} - \bar{\mathbf{e}})\right],\tag{10}$$

with the augmented covariance matrix C given by

$$C = C_d + C_e. (11)$$

In the next section, we will present our ansatz for the error covariance matrix in the case of uncertainties arising from the modelling of baryon physics.

# 4 MODELLING THE THEORETICAL ERROR COVARIANCE

In this section, we use 13 hydrodynamical simulations<sup>9</sup> to model the residual baryonic error from HMCODE on the convergence angular power spectrum of an LSST-like survey with the introduction of a baryonic error covariance matrix, which we will denote in the following by Cov<sup>Bar</sup>. The 13 hydrodynamical simulations considered in this work are: Illustris (Vogelsberger et al. 2014), Eagle (Schaye et al. 2015), MassiveBlack-II (MB-II; Khandai et al. 2015), Horizon-AGN (Dubois et al. 2014), and the nine different baryonic scenarios from the OWLS simulation set (Schaye et al. 2010; van Daalen et al. 2011).

We compute the tomographic convergence angular power spectrum from equation (1) with an upper limit of  $\ell_{max} \sim 3000$ . Following the Dark Energy Science Collaboration (DESC) requirements for the LSST Y10 weak lensing analysis (Mandelbaum et al. 2018), we consider 20 equally spaced logarithmic angular  $\ell$  bins ranging from 20 to 3000 for each tomographic spectra.

The matter power spectrum that enters equation (1) includes baryons and non-linear effects that we must account for. One widely used method to take include these effects in the matter power spectrum is to use a phenomenological halo model based approach implemented in HMCODE (Mead et al. 2015). This variant of the halo model uses two physically motivated additional parameters: the halo bloating parameter,  $\eta_0$ , and the minimum halo concentration, *A*. Calibration with the Cosmic Emu emulator obtained from the high-resolution gravity only (G) *N*-body simulations Coyote suite (Lawrence et al. 2010) yields A = 3.13 and  $\eta_0 = 0.604$ . When varying the *A* and  $\eta_0$  parameters, one controls the halo-profile in a

**Table 1.** Parameters of the flat- $\Lambda$  CDM + HMCODE parameters adopted in this work. Massless neutrinos were assumed.

Parameter	Fiducial	Prior		
$\Omega_m$	0.3156	flat(0.2998-0.3314)		
σ8	0.831	flat(0.789-0.873)		
$h_0$	0.6727	fixed		
$\Omega_b$	0.049 1685	fixed		
ns	0.9645	fixed		
w	-1.0	fixed		
τ	0.08	fixed		
Α	0.08	flat(1.0-8.0)		
$\eta_0$	0.08	flat(0.3-1.6)		

mass-dependent way that reproduces different feedback processes from various baryonic scenarios.

The HMCODE can be used to reproduce the results from hydrodynamical simulations. However, the results from best-fitting parameters arising from a Markov Chain Monte Carlo (MCMC) analysis show residual errors between the HMCODE-generated power spectra and the power spectra from simulations (Huang et al. 2019). We will mitigate these residual errors, modelling them as Gaussian variables that can be marginalized, generating an augmented covariance matrix as reviewed in Section 3.

There are several hydrodynamical simulations that include the effects of baryons, but they all depend on certain assumptions, such as the intensity of baryonic feedback processes. We use the results from Huang et al. (2019), who studied the spread in the predictions of the 3D power spectrum from different hydrodynamical simulations to assess the residual errors. We denote  $P_{hydro}^{\delta}$  the 3D power spectrum output from a given hydrodynamical simulation.

One difficulty in comparing different simulations is that they do not have the same input cosmology defined by the parameters that we denote  $\mathbf{p}_{co}$ . In order to compare results for the same cosmology, one adopts the following definition for the baryonic power spectra,  $P_{hydro}^{\delta}$ :

$$P_{\text{hydro}}^{\delta}(k, z | \mathbf{p}_{\text{co}}) = \frac{P_{\text{hydro, sim}}^{\delta}(k, z | \mathbf{p}_{\text{co,sim}})}{P_{\delta}^{G, \text{sim}}(k, z | \mathbf{p}_{\text{co,sim}})} P_{\text{HMcode, G}}^{\delta}(k, z | \mathbf{p}_{\text{co}}).$$
(12)

where  $P_{hydro, sim}^{\delta}$  is the outcome from a given baryonic simulation at some cosmology  $p_{co,sim}$  and  $P_{G,sim}^{\delta}$  denotes the corresponding gravity-only *N*-body simulation. Finally,  $P_{HMcode, G}^{\delta}(k, z | \mathbf{p}_{co})$ , is the power spectrum calculated from the HMcode calibrated by gravity only simulations. Thus we are assuming that the baryonic physics contribution to the power spectrum is independent of the input cosmologies  $p_{co,sim}$ . This was shown to be a good approximation in van Daalen, McCarthy & Schaye (2020) by running hydrosimulations given the span of cosmology from Wilkinson Microwave Anisotropy Probe (WMAP) 2009 (Hinshaw et al. 2013) to Planck 2015 (Planck Collaboration XIII 2016). Schneider et al. (2020) also showed that ignoring the coupling between baryon and cosmology would be valid for future stage-IV weak lensing experiments. We adopt the fiducial flat- $\Lambda$ CDM cosmology shown in Table 1.

In order to compute the convergence angular power spectrum one needs to project the 3D power spectrum into different tomographic redshift bins. For the galaxy number distribution, we again DESC requirements for the LSST Y10 weak lensing analysis (Mandelbaum et al. 2018). Hence, we use the following parametric form for the source redshift distribution n(z):

<sup>&</sup>lt;sup>9</sup>In some cases, such as CMB lensing, one can also use analytical prescriptions to estimate the impact of baryonic physics on the matter power spectrum (Bragança et al. 2020).



**Figure 1.** The redshift distribution of source galaxies for LSST Y10 weak lensing measurements (Mandelbaum et al. 2018). Dashed line: the true underlying galaxy distribution following equation (13) normalized to  $n_{\Omega} = 27 \operatorname{arcmin}^{-2}$ . Shaded areas: the redshift distribution of galaxies split into five tomographic bins normalized to  $n_{\Omega}^{i} = 5.4 \operatorname{arcmin}^{-2}$ . The shades of blue are darker for lower redshifts and lighter for higher redshifts.

where we set  $(z_0, \alpha) = (0.11, 0.68)$  for Y10. Furthermore, the total number density of galaxies is normalized as  $n_{\Omega} = 27 \text{ arcmin}^{-2}$ .

We take into account uncertainties in the photometric redshift measurements by considering a Gaussian probability distribution for a true redshift given a point measurement of a photometric redshift  $z_{phot}$ :

$$P(z_{\rm phot}|z) \propto \exp\left[-(z_{\rm phot} - z)^2 / 2\sigma_z^2\right],\tag{14}$$

with a photometric redshift error of  $\sigma_z = 0.05(1 + z)$ . The redshift distribution in each photometric redshift bin  $n_i(z)$  is then given by

$$n_i(z) = \int_{z_{\text{phot}}^{(i+1)}}^{z_{\text{phot}}^{(i+1)}} \mathrm{d}z_{\text{phot}} n(z) P(z_{\text{phot}}|z),$$

where the minimum redshift of the *i*th tomographic bin,  $z_{\text{phot}}^{(i)}$ , is constructed such that each one contains an equal number density of galaxies,  $n_{\Omega}^{i} = 5.4 \text{ arcmin}^{-2}$ . Furthermore the number of galaxies per steradian in the *i*th bin,  $n_{\Omega}^{i}$  is given by

$$n_{\Omega}^{i} = \int_{0}^{\infty} \mathrm{d}z \, n^{i}(z).$$

The resulting five  $n^i(z)$  tomographic distributions for the LSST source samples are shown in Fig. 1. By construction, the sum of the individual distributions equals the total  $\sum_i n_{\Omega}^i \equiv n_{\Omega}$ .

With the galaxy redshift distributions in the five tomographic bins, we can proceed to model the residual errors of baryonic effects on the convergence angular power spectrum. We compare the convergence angular power spectra as obtained from a given hydrodynamical simulation with the best-fitting HMCODE results for that particular simulation. An example of these residual errors for 13 different simulations is shown in Fig. 2 for the autocorrelations of redshift bins 0 and 4 in the same angular binning and scale-cut as the datavector. One can see that the spread of the errors decreases at higher redshifts, where baryonic effects are less important.

In this work, we use the best-fitting models generated by Huang et al. (2019). These models are characterized by the best-fitting values of *A* and  $\eta_0$ , and were obtained from MCMC runs, fitting the HMCODE baryonic parameters to the 2D convergence power spectra of the hydrodynamical simulations (considering the 3D power spectrum

of equation 12). We will now use these results to model the two ingredients that enter the additional covariance matrix due to the marginalization of the baryonic residual error: the envelope and the correlation.

#### 4.1 Modelling the envelope

Based on the residual errors for the angular power spectra and on the assumption that the true angular power spectrum spectra (i.e. the one directly obtained from observations) lies among the range of the hydrodynamical models, we decided to test three different parametrizations for the envelope shown in Fig. 2 that we call the Mirror, 2Mirror, and the Variance envelopes.

The Mirror envelope is a conservative definition. It takes the most extreme deviations of the HMcode best-fitting models and mirrors them about the horizontal axis, hence the name Mirror envelope. This approach overestimates the error amplitude, but guarantees that we are taking all the possible deviations the baryonic error may present. Also, this definition ensures the residual error,  $\mathbf{e}$ , to have zero mean,  $\mathbf{\bar{e}} = 0$ , which leads to the additional baryonic covariance matrix:

$$\operatorname{Cov}_{\operatorname{Bar}}(C^{ij}_{\kappa\kappa}(\ell), C^{pq}_{\kappa\kappa}(\ell')) = E^{ij}_{\operatorname{Mirror}}(\ell) \ \rho^{ij,pq}(\ell, \ell') \ E^{pq}_{\operatorname{Mirror}}(\ell'),$$
(15)

with

$$E_{\text{Mirror}}^{ij}(\ell) \equiv C_{\kappa\kappa}^{ij}(\ell) \max_{\text{model}} \left| 1 - \frac{C_{\text{HMcode}}^{ij}(\ell)}{C_{\text{Sim}}^{ij}(\ell)} \right|, \tag{16}$$

the *i*, *j* indexes labels the tomographic bins pairs from Fig. 1,  $C_{\kappa\kappa}^{ij}(\ell)$  on the right-hand side follows a gravity only model, just like the one used to compute the Gaussian covariance in equation (3). We choose the boundaries of the envelope to be at the model that presents the maximum deviation at that  $\ell$ . The absolute value makes it explicit that the Mirror envelope is a symmetric function about the  $\ell$ -axis. An even more conservative envelope, used to stress-test our approach with only our two most extreme baryonic data-vectors (ILLUSTRIS and MB-II), is the 2Mirror envelope which consists in simply doubling the Mirror envelope, as it follows

$$E_{2\text{Mirror}}^{ij}(\ell) \equiv 2 \times E_{\text{Mirror}}^{ij}(\ell).$$
(17)

The Variance envelope, on the other hand, is a less conservative approach which defines the envelope as the variance of the random vector  $\mathbf{e}$ . In this approach, we interpret the residual error from each hydrosimulation as a realization of the random variable  $\mathbf{e}$ . Hence, we simply take the variance between the 13 error curves and define it as our envelope, as follows:

$$E_{\text{Var}}^{ij}(\ell) = C_{\kappa\kappa}^{ij}(\ell) \sqrt{\frac{1}{N} \sum_{\text{model}}^{N} \left[ 1 - \frac{C_{\text{HMcode model}}^{ij}(\ell)}{C_{\text{Sims model}}^{ij}(\ell)} - \bar{e}^{ij}(\ell) \right]}, \quad (18)$$

where N = 13 stands for the total number baryonic models being considered here. In contrast with the mirror envelope, this definition does not impose a symmetric envelope; in other words, the Variance approach admits a non-zero mean value for the theoretical error,  $\bar{e}^{ij}(\ell) \equiv \langle 1 - \frac{C_{\text{HMCde}}^{ij}(\ell)}{C_{\text{Sim}}^{ij}(\ell)} \rangle$  and the baryonic error contribution to the covariance matrix has to be changed accordingly:

$$\operatorname{Cov}_{\operatorname{Bar}}(C^{ij}_{\kappa\kappa}(\ell), C^{pq}_{\kappa\kappa}(\ell')) = E^{ij}_{\operatorname{Var}}(\ell) \ \rho^{ij,pq}(\ell, \ell') \ E^{pq}_{\operatorname{Var}}(\ell') - \bar{e}^{ij}(\ell) \ \bar{e}^{pq}(\ell'),$$
(19)

Fig. 2 shows the different envelopes for two redshift bins: the first and the last ones. As expected, larger redshifts result in larger physical scales for the same angular scale leading to a decrease in the baryonic



**Figure 2.** The figures show the envelope's behaviour at redshift bins i, j = 0, 0 (low-redshift, on the left) and i, j = 4, 4 (high-redshift, on the right), with respect to the set of 13 baryonic models (solid lines). The lighter shaded area presents the 2Mirror envelope definition; which doubles the size of the most extreme scenarios and reflect them into the *x*-axis, ensuring a zero mean to the error variable. The intermediate grey area shows the coverage of the Mirror envelope. In this definition, the covariance amplitude is assumed to follow the size of the most extreme scenario. Finally, the darkest area shows the Variance envelope. For this definition, we take the standard deviation between all scenarios as the amplitude.

effects for a given angular scale. Notice that, as opposed to the mirror model, the Variance envelope underestimates the covariance amplitude for the most extreme scenarios. For instance, the Illustris simulation residual errors (red line) are left outside of the Variance envelope for  $\ell \gtrsim 100$ .

#### 4.2 Modelling the correlation

The last ingredient to model is the correlation coefficient  $\rho^{ij, pq}(\ell, \ell')$  that relates different redshift bins and Fourier modes of the error covariance. We adopt the ansatz

$$\rho^{ij,pq}(\ell,\ell') \equiv R^{ij,pq} \exp\left[-(\ell-\ell')^2/2L^{ij}L^{pq}\right],$$
(20)

which separates the redshift bin correlations  $R^{ij, pq}$  from the correlation of Fourier modes.

In this work we will model the effect on the covariance within the same redshift bin pairs, neglecting cross-covariances induced by baryonic effects in different redshift bin pairs, i.e. we assume:

$$R^{ij,pq} = \delta^{ip}\delta^{jq}.$$
(21)

With this major assumption, we are including tomographic power spectra that can fluctuate independently from other tomographic pairs as possible baryonic models. We will show that this ansatz is sufficient to mitigate the baryonic uncertainties.

With a diagonal  $R^{ij, pq}$ , the only parameter left to fully define the theoretical error covariance is the correlation scale of the baryonic errors,  $L^{ij}$ . We adopt

$$L^{ij} = k_{\text{halo}} \langle \chi \rangle^{ij} = k_{\text{halo}} \frac{\int d\chi \ \chi \ g^i(\chi) g^j(\chi)}{\int d\chi \ g^i(\chi) g^j(\chi)}, \tag{22}$$

with  $k_{\rm halo} = 1.0 h \,{\rm Mpc}^{-1}$  being a typical halo scale for  $\rho_{\rm virial} = \rho_{200}$ and  $M_{200} \approx 10^{13.5} \,{\rm M}_{\odot}$ . The chosen halo mass input,  $M_{200} \approx 10^{13.5} \,{\rm M}_{\odot}$ was motivated by Takada & Bridle (2007). In their fig. 3, they show that, at non-linear scales, an expressive fraction of the 1-halo term contributions for the lensing effects comes from haloes with masses of  $\approx 10^{13.5} \,{\rm M}_{\odot}$ . The calculated values of  $L^{ij}$  using equation (22) are shown in Table 2.

**Table 2.** Evaluated tomographic values of the characteristic  $\ell$ -scale for residual baryonic errors,  $L^{ij}$ , calculated in equation (22).

1 \ J	0	1	2	3	4
0	491	600	637	653	665
1	_	806	912	959	987
2	_	-	1120	1241	1308
3	_	-	-	1483	1655
4	-	-	_	-	2112

# 4.3 Full covariance

Finally, the full covariance is given by

$$\operatorname{Cov}(C_{\kappa\kappa}^{ij}(\ell), C_{\kappa\kappa}^{pq}(\ell')) = \operatorname{Cov}_{G}(C_{\kappa\kappa}^{ij}(\ell), C_{\kappa\kappa}^{pq}(\ell'))\delta_{\ell}^{\ell'} + \operatorname{Cov}_{\operatorname{Bar}}(C_{\kappa\kappa}^{ij}(\ell), C_{\kappa\kappa}^{pq}(\ell')),$$
(23)

where the Gaussian covariance matrix is given by equation (3) and is analytically generated using CosmoLike (Krause & Eifler 2017) with the LSST survey characteristics already discussed.

It is important to mention that shape noise starts to dominate the Gaussian covariance matrix, that is  $(\sigma^i)^2/2n_A^i > C_{\kappa\kappa}^{ii}(\ell)$  in equation (4), for  $\ell \geq 600$ , in the last redshift bin. For closer redshift bins, the shape noise is dominating for even smaller values of  $\ell$ .

In Fig. 3 we show the fractional difference between the Gaussian covariance matrix and the augmented covariance matrix (Gaussian plus baryonic theoretical errors). For large  $\ell$  (small scales), the theoretical errors term has larger relative values and dominates the uncertainties. In the following section, we study the impact of the augmented covariance matrix on parameter estimation using a simulated likelihood analysis.

#### **5 LIKELIHOOD ANALYSIS**

In this section we present our analysis choices used to assess the effectiveness of the proposed mitigation approach. In general lines, the analysis methodology consists in the following steps:



Figure 3. Fractional change in the diagonal elements of the covariance matrix ( $\ell = \ell'$ ) due to the inclusion the baryonic terms from the Mirror (left) and Variance (right) envelopes.

(i) Take the lensing spectra predicted by one of the four hydrodynamical simulations (Eagle, Illustris, MB-II, and Horizon-AGN) as mock data for our fiducial cosmology. These four simulations are representatives of the different baryonic effects.

(ii) Use the nested sampling algorithm MULTINEST (Feroz, Hobson & Bridges 2009) to fit the mock data to the HMCODE model by varying two cosmological ( $\Omega_m, \sigma_8$ ) and two nuisance parameters (A,  $\eta_0$ ) and determine the statistical errors from the Gaussian covariance on the cosmological parameters. This analysis does not include the residual effects of the model.

(iii) Determine the HMCODE bias with respect to the input cosmological parameters before the mitigation technique is applied.

(iv) Use MULTINEST to fit the mock data again to a model with those same two cosmological and two nuisance parameters but with the augmented covariance matrix proposed in the previous section.

(v) Determine the final residual bias as the difference between this second fit and the true values of the cosmological parameters used in the mock data (specified in Table 1).

(vi) Compare the statistical degradation of the methods from the size of the error bars in both cases.

In our analysis, we consider three sets of results for baryonic mitigation: HMCODE + Gaussian covariance matrix, HMCODE + Mirror covariance mitigation, and <math>HMCODE + Variance covariance mitigation. The 2Mirror covariance mitigation is used as a stress test of the method for the Illustris and MB-II simulations.

We assume a Gaussian likelihood for the tomographic two-point measurements. The model predictions are computed with HMCODE and the final posterior distribution on cosmological parameters is obtained with MULTINEST, implemented in COSMOSIS<sup>10</sup> (Zuntz et al. 2015). We use  $n_{\text{live}} = 100$  live points, efficiency of 0.01 and tolerance of 0.01. We sample over the parameters { $\Omega_m$ ,  $\sigma_8$ , A,  $\eta_0$ } since we want to concentrate on the cosmological parameters mostly affected by baryonic effects.

The results of the posterior distributions for the four different covariance matrices are shown in Fig. 4(a) and (b) for the Illustris and MB-II simulations. The dashed lines show the input cosmological parameters ( $\Omega_m$ ,  $\sigma_8$ ) together with the HMCODE parameters (A,  $\eta_0$ ) determined from the best-fitting analysis for a given simulation.

<sup>10</sup>https://bitbucket.org/joezuntz/cosmosis/wiki/Home

For the Illustris simulations, one cannotice a significant decrease in the bias for the cosmological parameters, whereas for the MB-II simulations there is a less significant improvement. This is probably due to the fact that Illustris has a stronger baryonic feedback than MB-II. It is also interesting to notice the effect of 'saturation' of the theoretical covariance matrix by comparing the results from the Mirror to the 2Mirror matrices: by becoming very conservative one stops losing statistical power and hence the areas of the ellipses do not change significantly. This is due to the fact that the affected modes are already suppressed and further suppression does not remove information. However, it is important to point out that there is a slight difference between different choices of the covariance matrix. This can be the most easily seen looking at the 2D posteriors for degenerate parameters, such as  $\Omega_m - \sigma_8$  panel in Fig. 4(a). In this case the true cosmology for the most aggressive  $1\sigma$  envelope is slightly outside the  $1\sigma$  contour. On the other hand, using the more conservative Mirror covariance leads to unbiased results for both cosmological parameters as well as for the best constrained principal component. This is important to keep in mind, particularly for combination with external data which have different degeneracy directions.

The results for the 1D marginalized 68 per cent error bars for the cosmological parameters ( $\Omega_m$ ,  $\sigma_8$ ) are shown in Fig. 5 for the four simulations using three different covariance matrices for the analyses (four for Illustris and MB-II simulations). One can see that by using improved covariance matrices modelling baryonic uncertainties can help in reducing the bias on the determination of cosmological parameters at a modest increase of the uncertainties.

# 6 DISCUSSION

Our final results are summarized in Table 3, where we show the 68 per cent error bars on the parameters  $\Omega_m$ ,  $\sigma_8$ , A, and  $\eta_0$  for four simulations and different covariance matrices and the amount of bias in the cosmological parameters  $\Omega_m$  and  $\sigma_8$  measured in units of the standard deviation. For Illustris and MB-II, representatives of extreme cases of baryonic parameters, we also present results with the very conservative case of the 2Mirror envelope. We can think of these augmented covariances from the Mirror and Variance envelopes acting in the data vector as a soft scale-cut. They gradually reduce the weight of a data point for the overall analysis as we move to scales with larger theoretical uncertainties.





**Figure 4.** Comparison of the posterior distributions for the cosmological  $(\Omega_m, \sigma_8)$  and nuisance parameters  $(A, \eta_0)$  among different mitigation covariances. The colours represent different covariance matrix model: Gaussian contributions only (blue), Mirror envelope (grey), 2Mirror (green), and Variance envelope (red) taking the Illustris (left) and MB-II (right) simulations as the input data vector. The dashed lines show the input cosmological parameters  $(\Omega_m, \sigma_8)$  together with the HMCode parameters  $(A, \eta_0)$  determined from the best-fitting analysis for the simulations. (a) Posterior distributions for an Illustris data vector. (b) Posterior distributions for a MB-II data vector.



Figure 5. Results for the 68 per cent error bars for the cosmological parameters  $\Omega_m$  and  $\sigma_8$  for different data vectors from four hydrodynamical simulation using three different covariance matrices (four in the case of Illustris and MB-II) in a nested sampling analysis of the posterior. Dashed lines are the input parameters.

**Table 3.** Summary of the results from simulated likelihood accuracy tests. In columns 3–6, we give the best-fitting posterior values as well as the 68 per cent confidence interval for two  $\Lambda$ CDM cosmological and nuisance parameters of the HMCODE ( $\Omega_m$  and  $\sigma_8$ ; *A* and  $\eta_0$ ). Columns 7–8 presents the offset between the best-fitting values and the fiducial ones. This offset is quantified in terms of the 68 per cent confidence interval, i.e. the 1 $\sigma$  interval size of that constraint.

Baryonic	Covariance	68 per cent limits				Bias	
data vector	matrix	$\Omega_m$	$\sigma_8$	$\eta_0$	A	$\Omega_m$	$\sigma_8$
Horizon-AGN	Gaussian	$0.3192 \pm 0.0018$	$0.8267 \pm 0.0024$	$0.601^{+0.015}_{-0.018}$	$2.54^{+0.13}_{-0.16}$	2.00σ	1.79σ
	Gauss. + Mirror	$0.3154 \pm 0.0026$	$0.8316^{+0.0040}_{-0.0036}$	$0.587 \pm 0.033$	$2.51 \pm 0.32$	$0.08\sigma$	$0.16\sigma$
	Gauss. + Variance	$0.3164 \pm 0.0024$	$0.8304 \pm 0.0034$	$0.600\pm0.021$	$2.64\pm0.19$	$0.33\sigma$	$0.18\sigma$
ILLUSTRIS	Gaussian	$0.3082 \pm 0.0019$	$0.8382 \pm 0.0027$	$0.764 \pm 0.017$	$2.14\pm0.13$	3.89σ	$2.66\sigma$
	Gauss. + 2Mirror	$0.3139 \pm 0.0027$	$0.8326 \pm 0.0036$	$0.816 \pm 0.046$	$2.33^{+0.36}_{-0.42}$	$0.63\sigma$	$0.45\sigma$
	Gauss. + Mirror	$0.3137 \pm 0.0025$	$0.8321 \pm 0.0036$	$0.819 \pm 0.036$	$2.40_{-0.34}^{+0.29}$	$0.76\sigma$	$0.31\sigma$
	Gauss. + Variance	$0.3122 \pm 0.0023$	$0.8334 \pm 0.0033$	$0.780 \pm 0.022$	$2.11 \pm 0.16$	$1.50\sigma$	$0.73\sigma$
EAGLE	Gaussian	$0.3175 \pm 0.0024$	$0.8279 \pm 0.0031$	$0.570^{+0.016}_{-0.015}$	$2.52^{+0.13}_{-0.15}$	0.79σ	$1.00\sigma$
	Gauss. + Mirror	$0.3148 \pm 0.0025$	$0.8317 \pm 0.0037$	$0.569 \pm 0.034$	$2.56 \pm 0.33$	$0.32\sigma$	$0.19\sigma$
	Gauss. + Variance	$0.3153 \pm 0.0022$	$0.8308 \pm 0.0032$	$0.572 \pm 0.020$	$2.63^{+0.16}_{-0.18}$	$0.13\sigma$	$0.06\sigma$
MB-II	Gaussian	$0.3150 \pm 0.0019$	$0.8308 \pm 0.0026$	$0.620\pm0.016$	$3.56\pm0.18$	$0.32\sigma$	$0.07\sigma$
	Gauss. + 2Mirror	$0.3147^{+0.0033}_{-0.0031}$	$0.8314_{-0.0043}^{+0.0045}$	$0.631^{+0.057}_{-0.052}$	$3.63^{+0.72}_{-0.62}$	$0.28\sigma$	$0.09\sigma$
	Gauss. + Mirror	$0.3148 \pm 0.0026$	$0.8313 \pm 0.0038$	$0.630 \pm 0.032$	$3.66 \pm 0.39$	$0.31\sigma$	$0.08\sigma$
	Gauss. + Variance	$0.3149^{+0.0021}_{-0.0025}$	$0.8312 \pm 0.0033$	$0.612\pm0.018$	$3.37\pm0.19$	0.30σ	$0.06\sigma$

Whereas the Mirror method performs a more conservative cut by accounting for unrealistically strong feedback models in its error amplitude, the Variance envelope considers the uncertainties on modelling more realistic AGN suppression leading to a softer cut. Figs 4(a),(b) and 5 show the 2D and 1D constraints obtained through these two approaches. We now discuss our results for the different simulations according to the strength of AGN feedback.

# 6.1 Weak AGN model

We begin by discussing the performance of the HMCODE-only analysis without the mitigation of its residuals (named as 'Gaussian'). For the MB-II data vector, the halo-bloating ( $\eta_0$ ) and concentration parameters (*A*) alone successfully recover the true cosmology. Even with only two free cosmological parameters, which may increase the bias since the other parameters are kept fixed, the best-fitting values for both  $\Omega_m$  and  $\sigma_8$  are below the ~0.4 $\sigma$  offset shift. This result is not unexpected if we recall MB-II's response function shown in Fig. 1 from Huang et al. (2019). Consequently, applying the 2Mirror, Mirror, and Variance methods to this well-modelled scenario does not significantly affect the residual biases, which remains below the ~0.4 $\sigma$  deviation.

# 6.2 Strong AGN model

Fig. 5 shows the evolution of the marginalized bias, for mock data based on Illustris, over increasingly conservative approaches (from left to right). The blue bars represent the constraint obtained when relying only on the HMCODE mitigation parameters. When ignoring A and  $\eta_0$  limitations on fitting complex dynamics, the residual bias

goes highly above the  $2\sigma$  deviation for both  $\Omega_m$  and  $\sigma_8$ , as depicted in Table 3. However, studies on the HMCODE residuals obtained a different result from ours. Huang et al. (2019) obtained that, after marginalizing over 6 wCDM cosmological parameters, the halobased model effectively mitigates the bias impact to less than  $0.5\sigma$ for the  $\Omega_m$  and  $\sigma_8$  1D posteriors. The discrepancy between our results is likely due to our bias analysis being naturally overestimated by the limited parameter space, especially on the  $w_0$  and  $w_a$  parameters with a strong correlation with  $\Omega_m$  and  $\sigma_8$ .<sup>11</sup>

The Variance covariance matrix (red bars) drastically reduces the HMCODE's offset of  $\Omega_m$  from 3.9 $\sigma$  to 1.5 $\sigma$ , and  $\sigma_8$  from 2.7 $\sigma$  to 0.7 $\sigma$ , as shown in Table 3. If focusing on the more conservative method (grey bars) one sees that, in this extreme AGN model, the larger covariance amplitude pays itself in the bias mitigation: the offset of both cosmological parameters is less than the marginalized statistical uncertainty.

#### 6.3 Intermediate AGN models

Fig. 5 shows the marginal 1D distributions for the analysis based on AGN models that are not as underestimated as MB-II and not as unrealistically strong as Illustris. For the Horizon-AGN, both Mirror and Variance covariances are effective in reducing HMCoDE's residual error below the  $0.4\sigma$  shift for our setup. The mirror is more successful in reducing the bias of both parameters: reaching a  $0.1\sigma$  shift for  $\Omega_m$ and  $0.2\sigma$  deviation for  $\sigma_8$ . Compared with the Variance envelope, the Mirror approach degrades the 1D error of  $\sigma_8$  by 17 per cent to gain 10 per cent on the accuracy. For  $\Omega_m$ , the loss in statistical power, 8 per cent, compared to Variance statistics, is compensated by a 76 per cent accuracy improvement.

We can understand Variance and Mirror's different performances with Horizon-AGN by recalling the shape of their covariances amplitudes from the left-hand panel of Fig. 2. We can see that, for tomographic bins i = 0 and j = 0, the model's physics becomes underestimated as we move beyond  $\ell = 1000$ . On the other hand, the top left panel shows that the Mirror approach's amplitude has no problems with covering the same physics, leading to higher effective accuracy.

For the EAGLE based analysis, HMCODE fitting approach alone is effective enough to keep the bias within the 1 $\sigma$  statistical uncertainty for one marginalized cosmological parameter. Furthermore, our residual mitigation methods improve the HMCODE model accuracy on both  $\Omega_m$  and  $\sigma_8$  from 0.8 $\sigma$  and 1.0 $\sigma$ , respectively, to less than 0.2 $\sigma$  (0.4 $\sigma$ ) for the Variance (Mirror) approach.

Compared to the Gaussian method in which we only rely on the HMCODE mitigation, the Mirror method increases the error bar by 4 per cent and 19 per cent for  $\Omega_m$  and  $\sigma_8$ , respectively. Whereas for our less conservative mitigation covariance, the Variance method, the constraint on  $\sigma_8$  degrades just by 3 per cent and it *shrinks* for  $\Omega_m$  by 8 per cent. The first thing we can comment about these results is that both Mirror and Variance methods accuracy overcompensates the loss in precision, which means that they can extract more information from the likelihood analysis for the EAGLE scenario. Finally, we can see the gain of 8 per cent in statistical power in  $\Omega_m$ , from the  $1\sigma$  analysis, even though we would expect the modified covariance

matrix to degrade the cosmological constraints. Please notice that this unexpected result only appears for one simulation (EAGLE) and for one parameter ( $\Omega_m$ ). It may be a consequence of the non-linear relation between the data covariance matrix and the posterior 1D distribution on the cosmological parameters.

To summarize, our modified covariance models (Mirror and Variance) are successful in improving the HMCODE information gain in the cosmic-shear likelihood analysis. For the 'strong' and 'intermediate' baryonic scenarios (Horizon-AGN, ILLUSTRIS, and EAGLE), the accuracy refinement of our method dramatically outweighs the loss in statistical power of the tested cosmological parameters (compared to the Gaussian analysis). The MB-II scenario is the only exception in which our mitigation method does not seem to be necessary because it is already well-modelled by the HMCODE free parameters alone.

# 7 CONCLUSIONS

Baryonic physics can significantly affect the theoretical modelling of the matter power spectrum in the small-scale regime. Therefore, mitigation methods have to be developed and tested to properly take this source of uncertainty into account. In this work, we focused on the mitigation of the baryonic effects using as an example the shear angular power spectrum in an LSST-like survey. We propose a mitigation method to decrease the bias in the determination of cosmological parameters due to residual errors in the baryonic modelling that uses the halo model-based HMCODE (Mead et al. 2015).<sup>12</sup> This method is based on an augmented covariance matrix that incorporates baryonic uncertainties informed by hydrodynamical simulations.

The augmented covariance matrix is constructed using the residual errors in the best-fitting modelling of 13 hydrodynamical simulations using HMCODE. We interpret these residual errors as a random variable and integrate over them to obtain the augmented covariance matrix. Nevertheless, there is some freedom in this interpretation and therefore we studied three different possibilities for what is called the envelope of the residual errors: the Mirror, Variance, and 2Mirror envelopes. Although, we do not provide the ultimate prescription for how to robustly estimate the envelope of the theoretical error, the results from Fig. 5 and Table 3 show that the use of these augmented covariance matrices can lead to a significant reduction in the bias of the estimated cosmological parameters at the cost of a small increase in the uncertainties in the parameters. The proposed choices about baryonic errors are still very dependent on the set of simulations. How to optimize theoretical error without unnecessarily down-weighting any data points and in an as model-independent way as possible remains one of the main open questions that deserves more investigation in the future. Finding the answer is the key for having a truly robust analysis with reliable error bars on cosmological parameters.

It must be also emphasized that the presented analysis is a first exploratory investigation, as many simplifications were assumed such as a reduced space of cosmological parameters, neglecting non-Gaussian contributions to the fiducial covariance matrix, and not including other sources of systematic effects, e.g. intrinsic alignments (IA). In principle, the covariance is calculated for the total shear power spectrum, and includes IA contributions to the cosmic variance

<sup>&</sup>lt;sup>11</sup>Since  $w_0$  and  $w_a$  are strongly correlated with  $\Omega_m$  and  $\sigma_8$ , as we can see from Huang et al. Fig. 4, keeping them fixed during the likelihood analyses increases the information on the matter parameters posterior distributions. That information gain leads to a tighter constraint on  $\Omega_m$  and  $\sigma_8$  and, thus, on the overall bias.

<sup>&</sup>lt;sup>12</sup>During the completion of this work a new version of HMCODE was released (Mead et al. 2021). This new version includes gas expulsion by AGN feedback and encapsulates star formation. Different, more physical parameters are introduced. The study of the consequences of the new code to our analysis is beyond the scope of the present work.

term. While we often choose to marginalize IA parametrically, and ignore theoretical modelling uncertainties in the scale dependence of IA, one could extend the theoretical error covariance approach to include IA in the form of additional (additive) terms in the covariance. However, DES-Y3 results (Secco et al. 2021) prefer IA models with simple scale dependence, putting the focus on baryon mitigation.

Our results are encouraging since for the scenarios studied in this paper, the reduction in the residual bias consistently compensates for the increase in the statistical error. Furthermore, the proposed method is easy to implement and computationally inexpensive, providing an interesting alternative to the more conservative scale-cut methods. We conclude that mitigation method for baryonic uncertainties described here is a promising and viable option for analyzing data with the quality level expected at the future surveys like LSST and it deserves further investigation.

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#### DATA AVAILABILITY STATEMENT

The data and codes used in this paper are available upon request from Maria Gabriela Moreira (mgabroelaop@gmail.com).

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