

AN INNOVATIVE UAV WITH VTOL CAPABILITIES

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ABSTRACT

Object of this work is the design and the simulation of a hybrid UAV with VTOL capabilities that has been designed for landing on naval moving platforms. The work is focused on the innovative propulsion layout adopted on the UAV. Authors discuss how adopted low level control strategies can exploit the innovative features of the proposed system assuring a good rejection of transversal wind disturbances. Particular attention is dedicated to low level modelling and control of the system emphasizing how chosen solutions can improve performances and robustness against crosswind. Main advantage of the proposed system is the combined control of vehicle heading and longitudinal propellers. In both fixed and rotating wing mode, performances in terms of robustness against crosswind disturbances are improved. Also the pose of the plane in terms of roll and pitch rotations is improved especially in rotating wing mode. Both these contributions are quite important allowing a more stable handling of the vehicle in complex mission scenarios

Keywords: Unmanned Aerial Vehicles, Hybrid Propulsion, Sliding Mode Control, Robust Control, Vertical Take Off and Landing

ADOPTED SYMBOLS

ψ = heading angle (ψ_{id} is the ideal path value, ψ_{ref} the reference one)

χ = course angle (χ_r is the course error)

V_g =ground speed

W =wind speed

V_a =speed respect to air

α =heading direction from current plane position to the next waypoint

δ = error between α and ψ_{id}

k_h =gain of the heading controller

$sat_i^j(x)$ =saturation function (saturates x between a min. value i and a max. one j)

d =transversal position error

s =sliding mode variable defined as the sum of contributions

s_1, s_2

k_1 =calibration variable of sliding mode controller

k_2 =gain of the sliding mode feedback

R =curvature radius

ϕ, θ =roll and pitch angles (ϕ_{id}, θ_{id} =desired values)

h, h_{id} =altitude and desired altitude

p, q, r = angular speed along the three directions

m, g = mass and grav. acceleration

T_{tot} = total prop. force respect to a fixed ref. ($T_{tot, i}$ is the i^{th} component)

M_{tot} = tota prop. torque respect to a fixed ref. ($M_{tot, i}$ is the i^{th} component)

T_i = thrust of the i^{th} propeller

x_{body} =longitudinal axis aligned to vehicle heading

x, y = position along x and y axis (x_{id}, y_{id} are desired values)

τ_i =forces along i -th direction in body reference frame (τ_{r_i} are the torques)

a, b_1, b_2 = dimensions describing the position of propellers

k_{it}, k_{qi} =thrust (pedex t) and torque (pedex q) coefficients of the i -th propeller

x_s, v_s =position and sailing speed of the support ship/moving landing platform

x_i, h_i = desired positions and altitudes corresponding to different waypoints

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1 INTRODUCTION

The object of this work is an innovative propulsion layout for an UAV with VTOL (Vertical Take Off and Landing) capabilities and the way in which adopted path following

control can contribute to exploit the performances of the proposed system.

Proposed system is mainly devoted for marine operations [1] involving the usage of ship-based helipads, this is an application that is still the object of very recent studies [2] for its relevant industrial interest.

The study is applied to propulsion and path control of a real industrial product [3] with a relevant impact also on specialized technical media [4],[5],[6].

Propulsion layouts of UAV can be classified according to the way in which lift, and propulsion are generated following a classification that is often adopted by review papers in literature [7]:

- Lighter than air UAVs (Airships, Dirigibles, Blimps and Balloons): the mean density of the vehicle is equal or lower respect to surrounding air, so lift forces are automatically granted. These kinds of vehicles are still proposed in recent works [8] since they offer the best ratio between lifted load and consumed energy. Additional propellers can be used control vehicle path. However, their low density also involves a higher sensitivity to crosswinds, also limiting maximum cruising speed.
- Rotary/Rotating Wing Systems: in a rotating wing system weight of the UAV is sustained by the efforts developed propellers that are consequently vertical or slightly inclined. UAV can perform VTOL and hovering, maneuverability at low speed is excellent [9],[10]. Known drawbacks are the poor propulsion efficiency (large part of installed power is employed to sustain the weight of the drone) and consequently limited autonomy and poor performances with harsh environmental conditions. Since propellers are vertical, longitudinal, or transversal propulsion efforts can be obtained only producing a corresponding pitch or roll rotation of the hull vehicle, so the control of the pose cannot be completely decoupled respect to translational motion [11].
- Fixed Wing Systems: In fixed wing systems lift is caused by the vehicle speed through the interaction of wings or other aerodynamic surfaces with the incoming flux of air. Propellers are used only to provide the longitudinal thrust against drag forces due to motion. Lift provided by wings is typically ten to twenty times higher respect to drag resistances [12]. Propulsion efficiency and autonomy are much higher respect to a rotating wing solution. Cruising velocity cannot be lower than stall speed precluding VTOL capabilities. Fixed wing drones often adopt catapults [13] for takeoff or landing nets or hooks for landing [14].
- Mixed Solutions: mixed propulsion configurations are a feasible compromise mixing the capabilities of both fixed and rotating wing systems, such as tilt rotors [15], tail sitters [16] and fixed wing systems with thrust vectoring of multiple fixed-axis propellers [17].

In this work this last solution [17] is adopted. A similar layout is also adopted for overcited marine applications involving the landing on a ship deck [1]. As shown in Fig.1 and Table I, proposed propulsion layouts introduce some distinctive innovations respect to the work of Dunder[12]

since proposed system is not pure electric but hybrid: an ICE (Internal Combustion Engine) moves a rear propeller that provides the longitudinal thrust during fixed wing cruising. This choice was preferred to maximize autonomy since fossil fuels are still the lightest way to store energy on an aerial system; a direct mechanical connection of the propeller with ICE involves a high propulsion efficiency as verified by past studies of the same authors [18]. The ICE is connected to an alternator that recharge batteries sustaining all the electrical loads of the UAV. The alternator is controlled by a four-quadrant drive: the same electrical machine can be used to boost the performances of the rear propeller realizing a parallel hybrid system [19], [20] that exploits energy stored in batteries. All the other propellers are driven by electric motors feed by batteries: an additional longitudinal electric propeller is placed in the front of the vehicle; eight vertical propellers sustain UAV weight during rotating wing propulsion. Adopted full-electric/hybrid-series configuration [20] is not efficient as the direct mechanical connection of the rear propeller, but it allows an easier coordination of multiple vertical and horizontal propellers during VTOL maneuvers when the UAV is working as a rotating wing drone.

Ailerons and ruddervators are used to control vehicle path during fixed wing cruising.

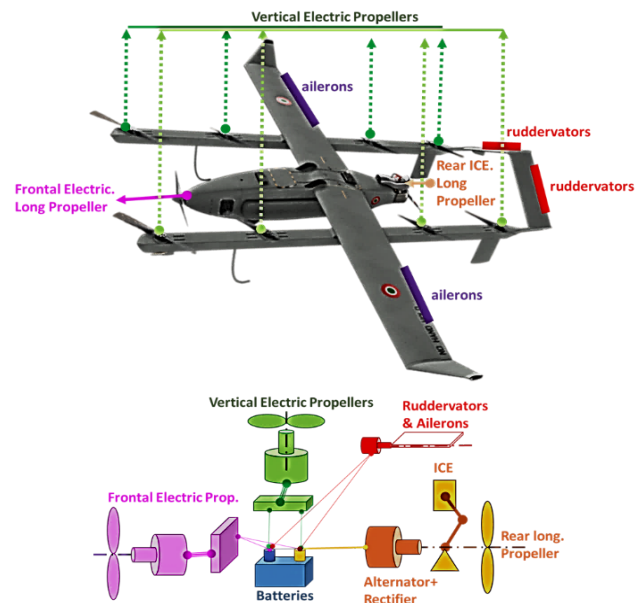


Figure 1. Investigated Propulsion Layout (top) and corresponding layout of the power management system (bottom)

To better exploit the performances of the proposed layout, authors investigate how different path control algorithms can improve vehicle performances especially against crosswind disturbances both in fixed wing cruising or during VTOL operations when rotating wing mode is activated.

In particular for what concern the fixed wing mode there is a wide literature [21],[22] concerning the way in which

path following can be implemented distinguishing among the following approaches:

- VTP (Virtual Target Point) techniques and control methods [23],[24]. exploit geometric approaches to generate virtual targets upon the path to be tracked real time.
- Control Methods: these methods are designed to assure the convergence of cross track error of the UAV while maintaining a preset airspeed. To the latter category for example belongs the Vector Field (VF) technique[[25],[26]], which involves designing a vector field to guide the aircraft on the desired path even in the presence of a constant wind disturbance.

A Further distinction[24] can be made distinguishing between look ahead [27], Non-Linear Guidance Law (NLGL) [28], Pure Pursuit and Line of-Sight (PLOS)[29] methods. However comparisons performed by the same literature sources [23],[24] confirm the general suitability of vector field techniques against constant crosswind disturbances and their overall robustness and performance in terms of maintaining stable paths with relatively efficient and smooth behavior in terms of performed actuations/corrections.

Table I- Main features of the investigated UAV[3]

PARAMETER		VALUE
Wingspan [m]		3.6
UAV Weight [kg]		43.23
UAV Typ. Operational Speed [m/s]		24
Vert.Props.	Max Thrust [kgf]	13.3 (Max Thrust Tested)
	Max Power [W]	3200 (Datasheet)
	Installed Storage Size [Ah]	3.25 (x8)
ICE Long. Prop.	Max Thrust [kgf]	6 (only ICE)/ 12.5(ICE+electrical boost)
	Max Power [W]	1515 (only ICE)
	ICE Power [W]	1500@7000rpm (1800@9000rpm)
	ICE Motor	2 Stroke Engine 29cc
Elect.Long. Prop.	Max Thrust [kgf]	12.2 (Max Thrust Tested)
	Max Power [W]	3744 (Datasheet)
	Installed Storage Size [Ah]	23

In this work, authors adopted for fixed wing cruising a vector field control based on the SMC approach (Sliding Mode Control) [30],[31]. Adoption of a sliding mode control has been recently proposed in literature for path control of fixed wing drones [32]. However, most of the over cited works in literature focused their attention on the control of the heading angle of the plane (whose definition will be cleared in the following section of this work), while the SMC proposed in this work is focused on the control of the course angle introducing a further improvement that is useful for the rejection of the crosswind disturbances.

Another innovative contribution of this work is represented by the path following control proposed in this work during the VTOL phase while the vehicle is operating in rotating wing mode. Conventional rotating wing UAVs are controlled during VTOL using only vertical propellers [33],

in this sense there is a plenty of work in literature in which this approach is applied and its further improved by adopting different approaches aiming to improve the robustness of adopted control respect to unmodelled dynamics [34] or to improve the modelling of the controlled UAV through identification procedures [35]. Both these approaches are suboptimal respect to the control of UAVs with hybrid mixed propulsion layouts as the one proposed in this work: mixed propulsion layouts involve the presence of wings and of additional longitudinal propellers.

The presence of wing involves a higher and anisotropic sensitivity against crosswinds that should be further increased by roll and pitch rotations that are normally performed to control transversal and longitudinal efforts of rotating wing drones. Otherwise, the presence of longitudinal propeller can provide an additional longitudinal effort that is quite fundamental to assure UAV stability against crosswind.

For this reason, the authors propose in this work a “directional VTOL” control which is specifically designed for this kind of vehicles: pose of the vehicle is kept constant to avoid additional disturbances, longitudinal propellers are exploited to cause vehicle motion and the vehicle is kept aligned along a position error direction to both exploit longitudinal propeller and to optimize the aerodynamic behavior of the plane respect to incoming flux of air. Also, this approach is quite innovative respect to current literature because the way in which path control is performed during VTOL operations is specifically designed for known features of the proposed hybrid, mixed propulsion layout. Also this kind of control is much more similar to heading/course control performed during fixed wing cruising simplifying the transition between the two modes during take-off or landing maneuvers.

Finally, for Directional VTOL desired efforts are allocated on propellers with a model-based approach that calculate desired speed references for each propeller from desired thrusts and torques. Also this approach is quite more refined respect to allocation criteria that conventionally adopted on drones since model based allocation according thruster model is more commonly adopted in recent studies [36],[37] concerning the control of AUVs (Autonomous Underwater Vehicles).

Innovative contributions of this research work can be summarized in the following points:

- A redundant hybrid and mixed propulsion layout is proposed for the design of an innovative UAV with VTOL capabilities
- Performances in cruising/fixed wing mode are improved adopting an SMC control of the course angle.
- During VTOL operations the vehicle is controlled with a specific controller able to better exploit vehicle features respect to conventional approaches followed on quad rotors.
- Allocation of speed references for the ESCs (Electronic Speed Controls) of each propeller is performed considering its torque and thrust coefficients, accelerating both calibration and scaling of the system.

Proposed work is organized in the following way:

- **UAV Modelling:** a brief section introducing the adopted model of UAV
- **Innovative SMC Path Control:** a section related to the description of the proposed SMC control for fixed wing mode.
- **Innovative directional VTOL Control:** proposed directional control adopted for VTOL operation is shown.
- **Simulation Results:** an extended simulation campaign is performed to show main features of proposed control strategies respect to the benchmark test UAV.
- **Conclusions and Future Developments**

2 UAV MODELLING

Investigated UAV described in Fig. 1 and Table 1 is modelled using a complete model that has been described in a previous publication [38] in which the UNIFI simulation platform that is used in this work was defined and described. Respect to this previous work, current propulsion layout has a higher number of both vertical propellers (eight instead of four) and longitudinal propellers (two instead of four) to assure a higher level of redundancy required by marine/naval operations:

- VTOL is possible with 75% of availability of vertical propellers (2 faulted propellers).
- Fixed wing propulsion can be assured by a single longitudinal propeller (the front or the rear one).

A scheme of the complete Matlab-Simulink™ model of the UAV is described in figure 2/a.

The model is designed to allow a multi-thread implementation for sub-systems representing the behavior of continuous physical systems respect to discrete/digital systems corresponding as example to the navigation and control logic of the vehicle.

Discrete systems are implemented considering their known sampling frequency (from 10 to 250Hz).

For continuous/physical systems the integration must be conversely higher: if the model is used only for simulation purposes a robust variable step solver (Ode 23tb a “stiff solver”) is adopted. For real time implementation a fixed step solver (Ode 1/Euler) running at higher frequency (1000Hz) is chosen. In this way the same model can be used also for RT (Real Time applications), such as HIL & SIL testing [39].

The Following sub-models, as shown in figure 2/a are implemented:

- **Mechanical Model of the UAV:** UAV dynamics is calculated according to a multibody model [40] that take count of propeller thrusts, and aerodynamic forces due to the incoming flow of air adopting corresponding matrices of linearized coefficients representing inertial and viscous effects. Followed approach is substantially based on the one that has been proposed by Fossen for both aerial [27] and marine [41] autonomous vehicles. Modelled UAV shares almost the same aerodynamics with a pre-existing UAV, the rapier X-25 [42] which have only one longitudinal propeller. So main data concerning

aerodynamics are available from previous experiences. In proposed AUV propellers are changed respect to the original X-25 project, so authors verified experimentally the target data of motors [43] and propellers [44]

Environment: the interaction with the surrounding environment is reproduced. Air density and crosswinds are tabulated respect to altitude and position[45]. During VTOL contact with the landing deck is evaluated using a contact-penalty method [46].

- **Energy Management:** All the loads on the UAV (actuators propellers, auxiliaries etc.) are simulated. Simulated hybrid power management system is described by a past research work of authors[18].
- **Sensors:** all the measured/estimated states of the system are evaluated through sensors sub models. For this work, it was preferred the hypothesis of a perfect estimation of system state (ideal sensors).
- **Control:** the UAV is controlled by a three-level nested architecture often proposed in literature[47], that is implemented using Stateflow™. The top level of the control is represented by Path Planning that has been previously described in [38] and it’s not the object of the current work. The respect of the path decided by the Path Planning is assured by an inner/nested loop, the so-called Path Following Control which decide how to correct route of the vehicle. Desired path corrections involve the Allocation of corresponding control references for propellers and actuators. This work is mainly focused on the two inner loops (Path Following and Allocation).
- **Safety Management:** safety protections and failure mitigation policies are modelled in this sub-model.

Resulting model can simulate different propulsion modes and the transition between them during a typical mission profile which is shown in Figure 2: proposed UAV can perform VTOL using only vertical propellers as a standard octocopter [48]. As the UAV reaches an assigned altitude, transition from VTOL to fixed wing mode and vice versa can be performed using transition methods proposed in literature [49].

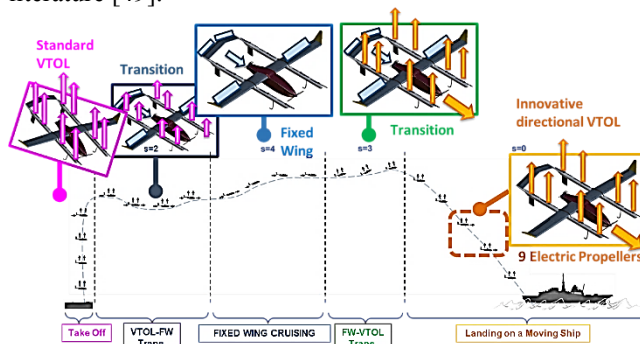


Figure 2. Sequence of different propulsion and control modes during a mission

Respect to full electric systems [17], autonomy in fixed wing mode is much higher since the rear propeller is directly connected to the ICE. The innovative directional VTOL Control proposed in this work is mainly designed for a more efficient landing on a moving ship deck. For this

work, it is supposed as landing deck an Italian ship [50] performing a straight cruise with a constant maximum speed of no more than 10m/s (about 20knots). Landing is performed with a straight trajectory aligned to the stern of the ship.

3. INNOVATIVE SMC PATH CONTROL

Most of Path following controls proposed in literature for fixed wing cruising perform a feedback control of the heading angle ψ . As shown in Figure 3, ψ is defined as the angle that describe the geometric orientation of the plane respect to North in a fixed reference frame.

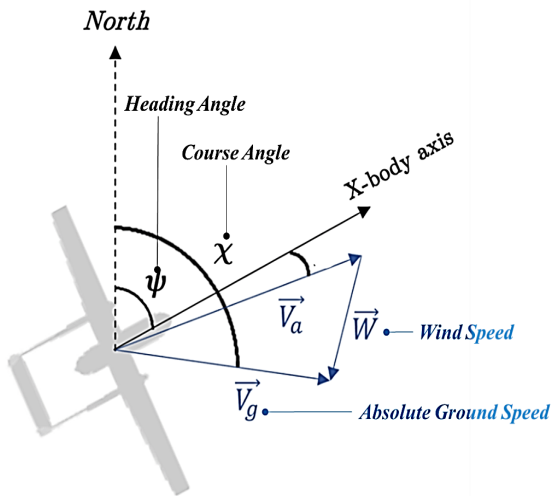


Figure 3. definition of heading and course angles

The course angle χ defines the direction of V_g , the ground speed of the UAV. V_g is the absolute speed of the plane which can be decomposed in two components: \vec{W} is the wind velocity (the velocity of the air) and V_a is the velocity respect to air. The control that was previously implemented [51] on the drone was described by equation (1) and by the scheme of figure 4/a. The angle α describes the orientation of the segment that connect the current UAV position with the next waypoint. ψ_{id} is the ideal heading direction of the minimal distance between successive waypoints. δ is defined as the error between α and ψ_{id} . The plane is controlled by imposing a reference heading angle ψ_{ref} (1) equal to the sum of ψ_{id} and a feedback term proportional (gain k_h) to the angular error δ ; to avoid excessive corrections the feedback terms is saturated to a maximum value equal to $\pi/4$ (sat is the saturation function). A unitary value of the gain k_h produces a desired ψ_{ref} that is equal to ψ_{id} .

$$\psi_{ref} = \psi_{id} + sat_{\frac{\pi}{4}}^{\frac{\pi}{-4}}(k_h \delta) = \psi_{id} + sat_{\frac{\pi}{4}}^{\frac{\pi}{-4}}(k_h(\alpha - \psi_{id})) \quad (1)$$

Recent scientific literature [52] is also proposing the control of the course angle χ as an easier way to reject wind disturbances reducing the error between the direction of vehicle speed V_g and the heading ψ . In this work SMC

(Sliding Mode Control) of the course angle χ is proposed to further increase robustness against crosswind disturbances. The term sliding mode refers to a state feedback variable structure controller that modifies the behavior of a nonlinear system by forcing it with a high-frequency control signal [30],[31]. The time-variant sliding surface, that represents the desired dynamics, is defined by the scalar variable s (2):

$$s = 0 \quad (2)$$

As shown in figure 4/b, two kinds of errors are considered:

- Transversal Position error d : UAV position is translated respect to desired path of a transversal distance d
- Course Orientation error χ_r : in ideal conditions course angle χ should be equal to ψ_{id} (V_g is aligned to path). So χ_r the error between χ and ψ_{id} must be minimized.

For the chosen sliding surface both errors must asymptotically converge to zero (3-4)

$$\lim_{t \rightarrow \infty} d = 0 \quad (3)$$

$$\lim_{t \rightarrow \infty} \chi_r = 0 \quad (4)$$

The sliding variable s (5) is defined as the sum of two terms (s_1 and s_2) that assure the respect of both desired behaviors described by (3) and (4):

$$s = s_1 + s_2 = \chi_r + \frac{1}{2} \tan^{-1}(k_1 d) \quad (5)$$

$$s_1 = \chi_r$$

$$s_2 = \frac{1}{2} \tan^{-1}(k_1 d)$$

In (5) the gain k_1 is introduced to calibrate the rejection of the transversal error d respect to the angular one χ_r . \tan^{-1} is limited to a maximum value of $\pi/2$ so $s_2(5)$, is saturated to a maximum value of $\pi/4$; this is the same value to which is limited the heading controller (1) to prevent unstable behaviors of the plane. In (5) the usage of \tan^{-1} produces a smooth behavior to prevent chattering. Derivative of the sliding variable s (5) is described by (6):

$$\dot{s} = \dot{\chi}_r + \frac{1}{2} \frac{k_1}{1 + (k_1 d)^2} \dot{d} \quad (6)$$

SMC guidance law is composed by two terms [30]:

- Model based Contribution: this term is calculated by imposing a null error dynamic $\dot{s} = 0$
- Discontinuous Contribution: a feedback term of the sliding variable s forces the convergence to the sliding surface rejecting disturbances and unmodeled dynamics. To reduce chattering, proportional feedback with gain k_2 is preferred.

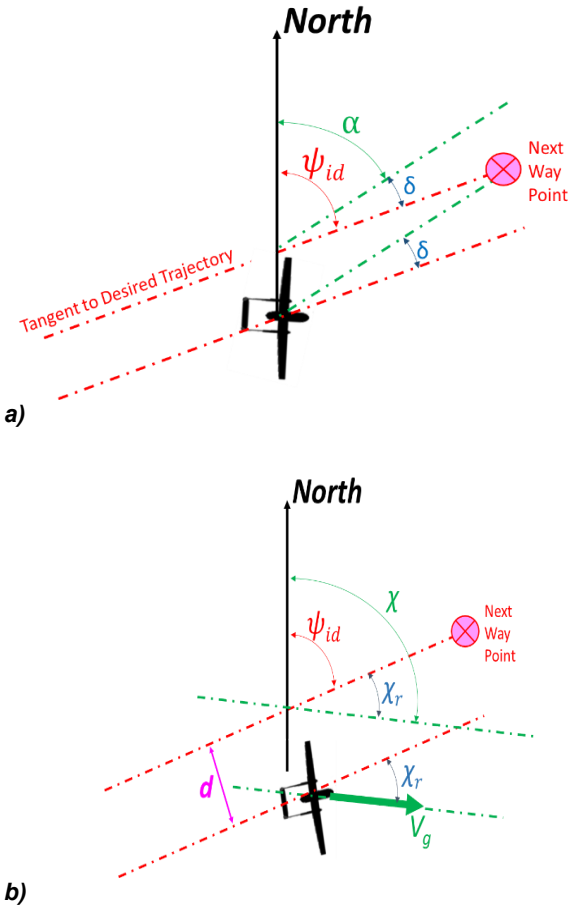


Figure 4.(a) definition of conventional heading control (GH) and the proposed (b) course control (GC)

For the synthesis of SMC, a model of a fixed wing UAV is needed. As shown in figure 5, the plane is supposed to be controlled by three internal loops aiming to control altitude (acting on rear propeller speed), speed (acting on elevators) and heading ψ (by regulating roll ϕ through ailerons).

As shown in figure 6, Aerodynamic lift L must equilibrate both lateral inertial forces due to trajectory curvature (R =curvature radius) and gravity. A steady state relation between the roll angle and path curvature is calculated imposing equilibrium (7), that is known in literature [53] as the equation describing a “banking” or “bank-to-turn” maneuver.

$$\begin{cases} L \cos \phi = mg \\ L \sin \phi = m \frac{V_g^2}{R} \end{cases} \rightarrow \phi = \tan^{-1} \left(\frac{V_g^2}{Rg} \right) \quad (7)$$

For a stationary turn, curvature radius is equal to ratio between ground speed V_g and the course one $\dot{\chi}$. For a slow changing path (ψ_{id}) the difference between derivatives $\dot{\chi}$ and $\dot{\chi}_r$ is negligible (8):

$$(8)$$

$$\dot{\chi}_r \approx \dot{\chi} = g \frac{\tan \phi}{V_g}$$

Derivative of the transversal error d is a function of V_g and χ_r (9)

$$\dot{d} = V_g \sin \chi_r \quad (9)$$

Using Model (7-9) desired roll $\phi_{ref}(d, \chi_r)$ is calculated (10):

$$\phi_{ref} = \tan^{-1} \left\{ -\frac{V_g^2}{2g} \frac{k_1}{1 + (k_1 d)^2} \sin \chi_r - k_2 \text{sign} \left[\chi_r + \frac{1}{2} \tan^{-1}(k_1 d) \right] \right\} \quad (10)$$

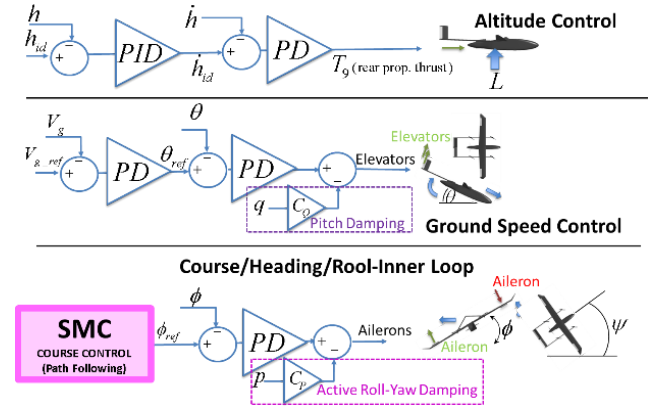


Figure 5. inner control loop

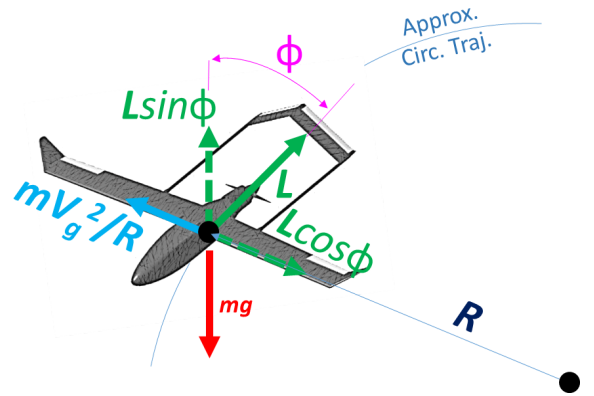


Figure 6. simplified model used for the design of SMC

4. INNOVATIVE DIRECTIONAL VTOL CONTROL

Proposed UAV can be controlled as a standard octocopter [54]. As shown in figure 7, the total propulsion force T_{tot} (respect to a fixed frame) is the sum (11) of the contributions of the eight vertical propellers (T_1 - T_8). UAV attitude is described with Euler angles (roll ϕ , pitch θ and yaw ψ) as shown in figure 8.

$$T_{tot} = \begin{bmatrix} (\sin \psi \sin \phi + \cos \psi \cos \phi \sin \theta) \\ (-\cos \psi \sin \phi + \sin \theta \sin \psi \cos \phi) \\ (\cos \theta \cos \phi) \end{bmatrix} \sum_{i=1}^8 -T_i \approx \begin{bmatrix} (\sin \psi \sin \phi + \cos \psi \sin \theta) \\ (-\cos \psi \sin \phi + \sin \theta \sin \psi) \\ 1 \end{bmatrix} \sum_{i=1}^8 -T_i \quad (11)$$

$$T_{tot} = \begin{bmatrix} (\sin\psi \sin\phi + \cos\psi \cos\phi \sin\theta) \\ (-\cos\psi \sin\phi + \sin\theta \sin\psi \cos\phi) \\ (\cos\theta \cos\phi) \end{bmatrix} \sum_{i=1}^8 -T_i \approx \begin{bmatrix} (\sin\psi \sin\phi + \cos\psi \sin\theta) \\ (-\cos\psi \sin\phi + \sin\theta \sin\psi) \\ 1 \end{bmatrix} \sum_{i=1}^8 -T_i$$

Propulsion mode described by (11) has a poor efficiency respect to power expended by vertical propellers. Roll and pitch rotations negatively affect the attack angle of the wings, producing large aerodynamics disturbances and an increased sensitivity against crosswind.

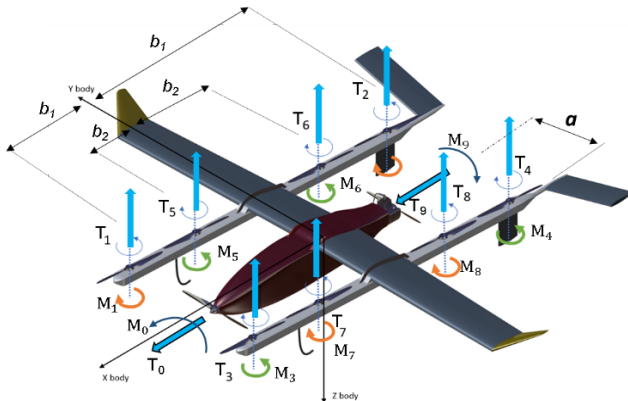


Figure 7. applied forces and reaction torques.

Authors proposed to keep a stable attitude (both roll ϕ and pitch angle θ are equal to zero). Total propulsion forces T_{tot} (12) and torques M_{tot} (13) are calculated respect thrusts T_i and reaction torques M_i of both vertical and longitudinal propellers.

$$T_{tot} = \begin{bmatrix} T_{tot,x} \\ T_{tot,y} \\ T_{tot,z} \end{bmatrix} = \begin{bmatrix} \cos\psi & -\sin\psi & 0 \\ \sin\psi & \cos\psi & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{bmatrix} \begin{bmatrix} T_0 \\ T_1 \\ T_2 \\ T_3 \\ T_4 \\ T_5 \\ T_6 \\ T_7 \\ T_8 \\ T_9 \end{bmatrix} \quad (12)$$

$$M_{tot} = \begin{bmatrix} \cos\psi & -\sin\psi & 0 \\ \sin\psi & \cos\psi & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & -a & -a & a & a & -a & -a & a & a & 0 \\ 0 & b_1 & -b_1 & b_1 & -b_1 & b_2 & -b_2 & b_2 & -b_2 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{bmatrix} \begin{bmatrix} T_0 \\ T_1 \\ T_2 \\ T_3 \\ T_4 \\ T_5 \\ T_6 \\ T_7 \\ T_8 \\ T_9 \end{bmatrix} + \begin{bmatrix} -100 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 11 & -1 & -1 & -1 & -1 & -1 & -1 & -1 & 0 \end{bmatrix} \begin{bmatrix} M_0 \\ M_1 \\ M_2 \\ M_3 \\ M_4 \\ M_5 \\ M_6 \\ M_7 \\ M_8 \\ M_9 \end{bmatrix} \quad (13)$$

$$M_{tot} = \begin{bmatrix} \cos\psi & -\sin\psi & 0 \\ \sin\psi & \cos\psi & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & -a & -a & a & a & -a & -a & a & a & 0 \\ 0 & b_1 & -b_1 & b_1 & -b_1 & b_2 & -b_2 & b_2 & -b_2 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{bmatrix} \begin{bmatrix} T_0 \\ T_1 \\ T_2 \\ T_3 \\ T_4 \\ T_5 \\ T_6 \\ T_7 \\ T_8 \\ T_9 \end{bmatrix} + \begin{bmatrix} -100 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 11 & -1 & -1 & -1 & -1 & -1 & -1 & -1 & 0 \end{bmatrix} \begin{bmatrix} M_0 \\ M_1 \\ M_2 \\ M_3 \\ M_4 \\ M_5 \\ M_6 \\ M_7 \\ M_8 \\ M_9 \end{bmatrix}$$

In this way vertical propellers are used to control torques along the three axis ($M_{tot,x}$, $M_{tot,y}$, $M_{tot,z}$) and the vertical force $T_{tot,z}$. As shown in figure 9, four closed loops control

the altitude of the vehicle h and the angular pose in terms of ϕ, θ, ψ without any further coupling with the longitudinal motion of the plane. Longitudinal propellers (numbered as 0 and 9 in figure 7) are used to control the value of the ground speed V_g since their thrust is aligned to x_{body} axis (body ref. frame).

As shown in figure 8, V_g direction is affected by errors:

- Course χ is not parallel to the ideal path described by the angle ψ_{id} .
- Path is translated of a transversal error d .

The shortest path to reach the setpoint is described by the angle ψ_{ref} that is the direction of the segment connecting the current position of the UAV with desired one.

So χ is corrected to align V_g to ψ_{ref} , that is the shortest path to reduce position error e between current position and the next waypoint. The transversal position error d is also rejected. This control is based on the idea that the position error can be rejected by aligning longitudinal propeller against the direction of the direction of the error e , so authors called this method ‘‘Directional VTOL’’.

The scheme of the controller is shown in figure 9:

- Inputs are desired altitude ($h_{id}(t)$), position ($x_{id}(t)$, $y_{id}(t)$). Roll and pitch references (ϕ_{id} , θ_{id}) are held constants.
- Altitude roll and pitch are controlled by three loops which calculate desired efforts in body reference frame: the vertical force τ_z and the torques respect to x and y axis τ_x and τ_y .
- Position errors respect to x and y directions are used to evaluate χ , ψ_{ref} and the errors χ_r , e .
- A loop calculates τ_x (force along x direction) to reduce e ; another loop calculates τ_z (torque along the z-axis) to
- Propellers are speed controlled by their ESCs (Electronic Speed Controllers). Both thrust (T_i) and torque (M_i) exerted by the i-th propeller are proportional to the squared value of its angular speed ω_i through thrust (k_{ti}) and torque(k_{qi}) coefficients [55]. Desired efforts (τ_x , τ_y , τ_z) are converted in desired values of ω_i^2 through the allocation matrix A (14), that is calculated from relations (12) and (13).

$$A = \text{Pinv} \begin{bmatrix} k_{t0} & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & k_{t9} \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & -k_{t1} & -k_{t2} & -k_{t3} & -k_{t4} & -k_{t5} & -k_{t6} & -k_{t7} & -k_{t8} & 0 \\ 0 & -k_{q0} & -a k_{t1} & -a k_{t2} & a k_{t3} & a k_{t4} & -a k_{t5} & a k_{t7} & a k_{t8} & k_{q9} \\ 0 & b_1 k_{t1} & -b_1 k_{t2} & b_1 k_{t3} & -b_1 k_{t4} & b_2 k_{t5} & -b_2 k_{t6} & b_2 k_{t7} & -b_2 k_{t8} & 0 \\ 0 & k_{q1} & k_{q2} & -k_{q3} & -k_{q4} & -k_{q5} & -k_{q6} & k_{q7} & k_{q8} & 0 \end{bmatrix} \quad (14)$$

Matrix A (14) is calculated calculating the pseudo-inverse according to Moore-Penrose. This approach involves two useful consequences:

- Moore-Penrose approach minimizes the quadratic norm of the vector of calculated ω_i^2 . This is a very useful properties since this produce an optimization also of energy consumptions of the drone as also stated by recent works [56] in which this property is exploited to improve efficiency and autonomy of drones.

- If a failure of a propeller is detected, matrix A can be recalculated taking count of the failure of a propeller (matrix can be resized or recalculated with the same size considering a null value of the thrust coefficients associated to the damaged actuator). In this way calculated thrust actuation is still optimal respect to the current state of the propulsion layout mitigating the effect of failures, as stated by recent publication that are still exploiting this interesting property of pseudo-inverse allocation matrix on redundant propulsion layout [57].

Transition from fixed wing cruising mode and the proposed directional VTOL is performed by reducing the UAV velocity. As the UAV approaches stall speed, VTOL is activated imposing a desired altitude h_{id} and a desired fixed attitude ($\phi=\theta=0$). SMC control of the course angle is switched off, substituted by the two position loops aiming to control vehicle x and y positions. Typical transition procedures proposed by authors have been also previously described by authors in a recent publication [40]. This transition is almost bump-less because both SMC and directional VTOL regulate the course angle to assure the alignment of V_g to the shortest path for the next waypoint.

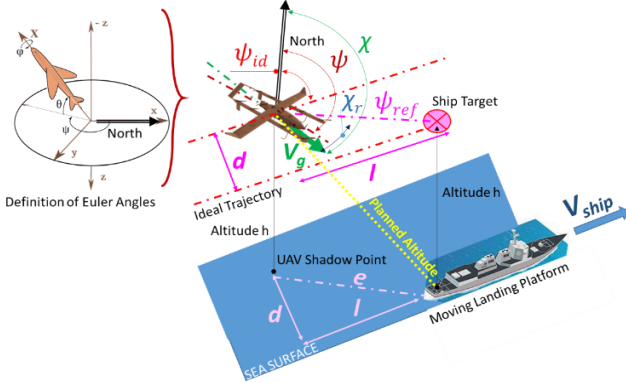


Figure 8. proposed directional control (kinematics)

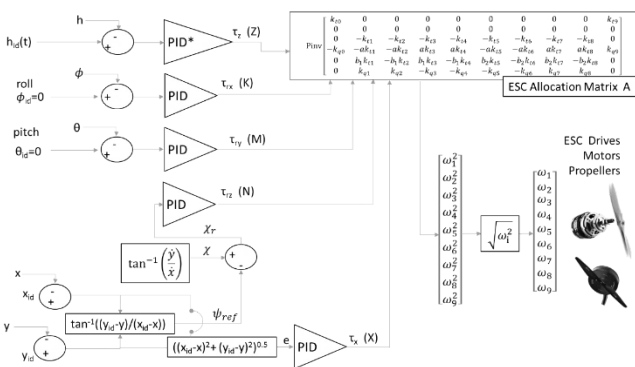


Figure 9. simplified structure of the proposed controller

5 SIMULATION RESULTS

Thanks to the availability of a complete and efficient modelling platform, it is possible to evaluate various aspects of proposed propulsion layout and path control strategies with a particular attention to the modelling of

thousands different conditions. The objective of the activity is to verify how proposed control strategies in synergy with chosen propulsion layout can improve stability and robustness against crosswinds. As shown in flowcharts of figures 10/a/b/c, the analysis is divided in two phases, first it is evaluated the performances of the system in a fixed wing cruising scenario in which is substantially evaluated the performance of SMC path control of the course angle.

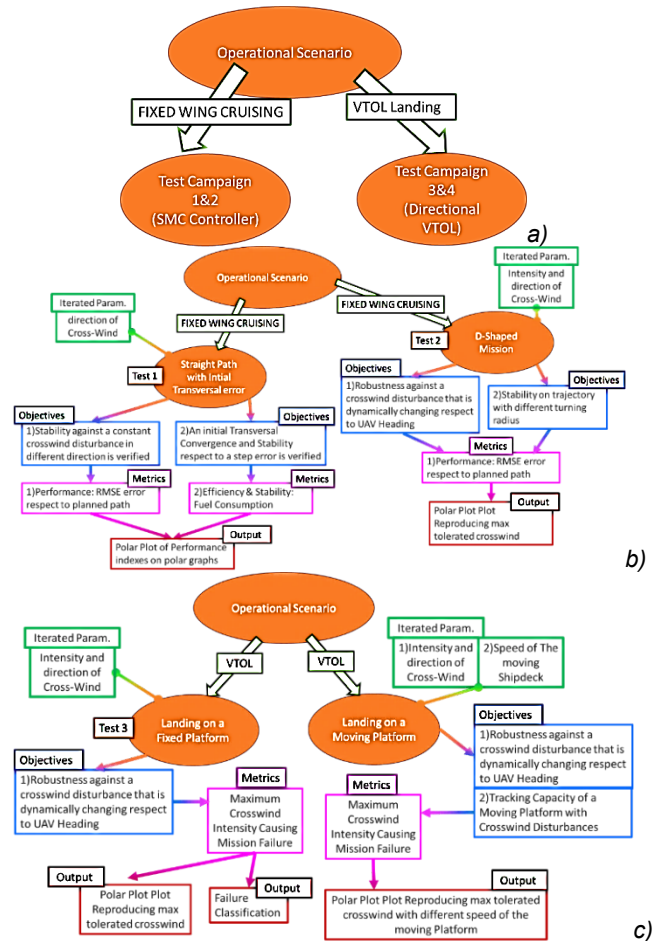


Figure 10. Performed Testing (simulation) campaigns (a) for fixed wing cruising (b) and VTOL operations (c)

Then it is evaluated the behavior during a landing maneuver in which the UAV mostly operate in rotating wing mode (directional VTOL control). As shown in figure 10/b, testing of the SMC is performed with two consecutive testing campaigns (straight path tests and D-Shaped closed loop path) in which static and dynamic performances of proposed SMC controller are verified. As shown in figure 10/c. Directional VTOL controller is tested on two sequences of landing maneuvers in which different parameters are verified iteratively considering first only the effect of crosswind in different direction and then with the combined effect of a longitudinal motion of the ship. Also, in this case, performances are evaluated in terms of polar graphs that represent the maximum intensity of crosswind that prevents the completion of planned mission. The use of polar graphs representing few concise performance indexes

such as the maximum intensity of wind, is also a contribution of the work: in this way it's possible to have a very compact evaluation of system performances of thousands of different simulations.

5.2 TEST CAMPAIGN 2: D-SHAPED TRAJECTORY

A D-Shaped mission profile at constant altitude is reproduced. Path is described by straight segments connecting waypoints to test performances and robustness respect to sharp direction changes. Test is repeated considering the presence of constant wind disturbance of about 15ms. Imposed path is studied to deliberately stress the performances of proposed controllers by imposing "sharp", "zero curvature" turns on some waypoints in order to verify the behavior of the system also when highly non linear saturated behavior is excited. Performances of the heading regulator (1) and SMC control are compared.

As shown in figure 13, SMC controller is much more precise respect to the heading one in terms of RMSE both in calm and windy conditions. SMC is a bit more fuel consuming (about 10%). This higher consumptions are recorded on strongly disturbed paths designed to excite non linear-saturated behavior of the system so authors are quite confident that considering more relaxed cruising profiles also differences in terms of consumption should become negligible.

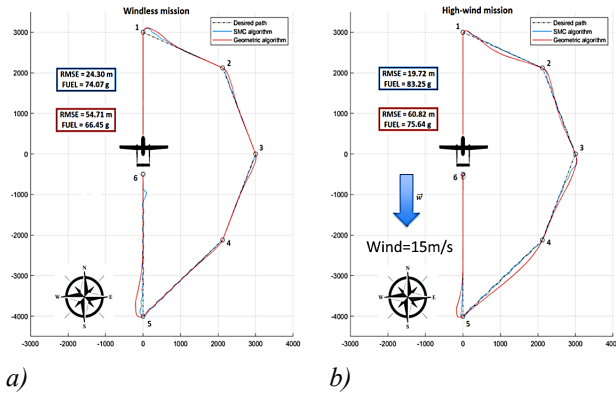


Figure 13. D-Shaped Mission Comparison between performed trajectory with SMC and Heading Control in windless conditions(a) and with a constant wind disturbance of 15ms(b)

As shown in figure 14, with SMC, course angle is better aligned to desired path resulting in a more precise control. SMC turns the Heading of the plane against the incoming flux of air to reject wind disturbances, this also justifies higher fuel consumption. This is an interesting feature considering that the imposed "zero curvature" turn of more than 120° imposed to the UAV in figure 14, excites non linear behavior of the systems and saturation effects (saturation of both roll and heading angle corrections) that, in the heading controller substantially amplifies the action of the cross wind disturbance. Otherwise with SMC it is not possible to avoid an initial overshoot on curves (visible

both in figure 13a/b and 14) since these behavior is due to a saturation of UAV performances. However the regulator exhibit a faster capability and a more robust behavior that is typical property of SMC controllers.

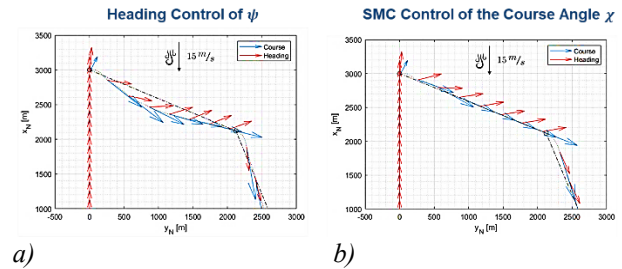


Figure 14. Comparison of regulated heading and course angles with different controllers, geometric heading control (a) and SMC Course Control (b)

Simulations are repeated varying both intensity (steps of 0.1m/s) and direction of crosswind(step of 1°). Thousands of simulations are performed compiling the UAV model for fast execution and parallelizing the execution on 32 threads. Polar diagrams of figure 15 describe the maximum wind for which the simulated mission is successful respect to crosswind direction. Polar plot is not symmetric since the proposed D-shaped mission profile is also asymmetric. This is a desired feature of the chosen mission profile to widely check system performances.

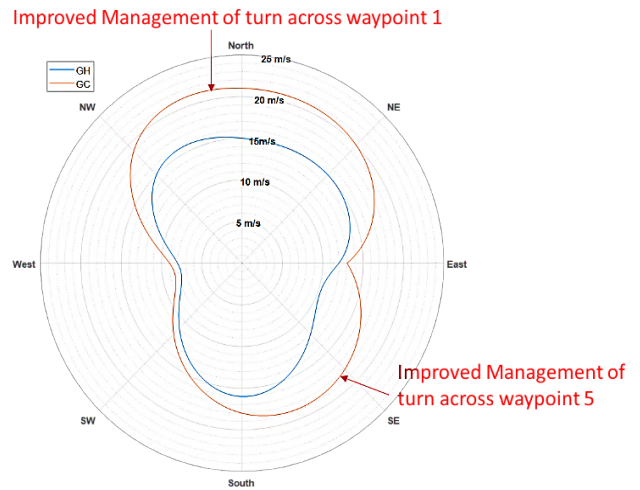


Figure 15. Polar plot of the maximum wind disturbance that the UAV can reject without failing the D-shaped mission respect to its direction

SMC exhibits higher performances respect to the heading controller in almost every condition. Both heading(GH) and SMC(GC) regulators are quite sensitive to lateral winds in east and west direction causing the failure of sharp turning maneuvers around waypoints 1 & 5. A smoother trajectory planning should be able to further improve the response of the system (authors are currently working on this topic but this will be the object of another publication).

5.3 TEST CAMPAIGNS 3&4: LANDING MANOEUVERS ON A SHIPDECK

Performances of proposed directional VTOL system are evaluated simulating the landing on a moving platform according the scheme of figure 16:

- The landing platform (the deck of a ship) is supposed to be located under the Waypoint 6 traveling with a straight trajectory at a constant sailing speed v_s . A perfect knowledge of ship position is supposed. This hypothesis is optimistic but the aim of this work is to evaluate performances of proposed propulsion layout respect to a near to realistic mission profile. Any consideration regarding high level control or dynamic path planning should be the object of a future work. Aerodynamic Turbulence arising from interaction with ship structure is omitted, since this kind of phenomena are very difficult to be simulated with a lumped model like the proposed one. However the presence of this disturbances in real application is a further justification for strict requirements concerning performances and robustness of implemented controllers.
- AUV is performing a D-Shaped mission as the one described in figure 13. At the end of the mission (about 400m before the last waypoint the sixth one), the UAV is decelerated from its cruising speed (around 90 km/h) to a final speed equal to the sailing speed of the ship, v_s , performing the transition from fixed wing mode to directional VTOL. At the end of the transition UAV is aligned to the straight trajectory of the ship.
- As the UAV arrives at waypoint 6, the landing is performed by imposing a variable path that is composed by a sequence of vertical descents alternated with constant altitude translations to moving waypoints that are continuously updated according the know trajectory of the ship ($x_s(t)$). The imposed sequence is also described in table III.

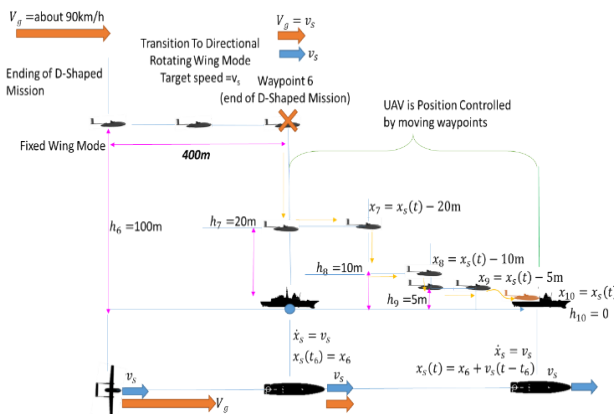


Figure 16. landing of UAV on a moving platform

Table III- Landing Sequence

LANDING SEQUENCE (ORDER)	POSITION OF NEXT WAYPOINT ALONG SHIP TRAJ. X	DESIRED ALTITUDE
0	x_6 (ship is supposed to be under Waypoint 6 for simplicity)	100m

1	x_6	20m
2	$x_7 = x_s(t) - 20m$	20m
3	$x_8 = x_s(t) - 10m$	5m
4	$x_9 = x_s(t) - 5m$	5m
5	$x_s(t)$	0m (landing)

Preliminary simulations are performed assuming a fixed landing platform ($v_s=0$). These simulation are repeated considering a variable intensity (with increasing steps of 0.1m/s) and direction (steps of about 1°) of crosswind.

Aim of the simulation campaign (involving the simulation of about 35000 missions) was to calculate the maximum crosswind intensity that should cause a failure of the mission.

For what concern the usage of longitudinal propellers only the electrical one is exploited (propeller θ in figure 7)

Failure criteria are related to the maximum positioning error on shipdeck (5m), max landing speed(1.4m/s) and maximum duration of the mission (1200s).

The same simulations are repeated controlling the UAV as a conventional octocopter: only vertical propellers are used as described by equation(11). Polar representations of the maximum tolerated crosswind are visible in figure 17/a.

UAV approaches the shipdeck from the stern of the ship, so crosswind direction is evaluated respect to this direction. Maximum crosswind intensity tolerated by directional VTOL is at least two times higher than the one of the conventional control that exploits only vertical propellers.

This is a very interesting result because the max power developed by the longitudinal propeller is only one eight of the max power of vertical ones. So it should be concluded that directional VTOL is much more efficient in exploiting installed power to reject crosswind disturbances.

Directional VTOL controller exhibits best performances against frontal crosswind arriving from bow. In this direction, in case of excessive wind, the failure of the mission is associated to an excessive duration. In the other directions performance of VTOL are lower and the typical mission failure is associated to excessive errors in terms of final position and speed during landing.

Performances of the “conventional” control (only vertical propeller) are negatively affected by an high sensitivity against crosswinds in lateral direction.

Sentivity against lateral crosswinds is mainly caused by additional aerodynamic disturbances introduced by wings and by the disposition of vertical propellers which penalize the control of roll rotations respect to pitch ones.

Same simulations are finally repeated considering different values of sailing speed ($v_s=7-10$ m/s;) of the ship. Results are shown in figure 17/b.

With a sailing speed over 7m/s UAV landing is possible only with directional VTOL: if the UAV is controlled as a conventional octocopter, the mission cannot be completed (so results are not shown in figure 17/b). Performances of directional VTOL are negatively affected by the increase of v_s . This performance reduction is less evident for crosswind coming from rear/stern direction. As the value of v_s increases, crosswinds in lateral direction penalize UAV performances.

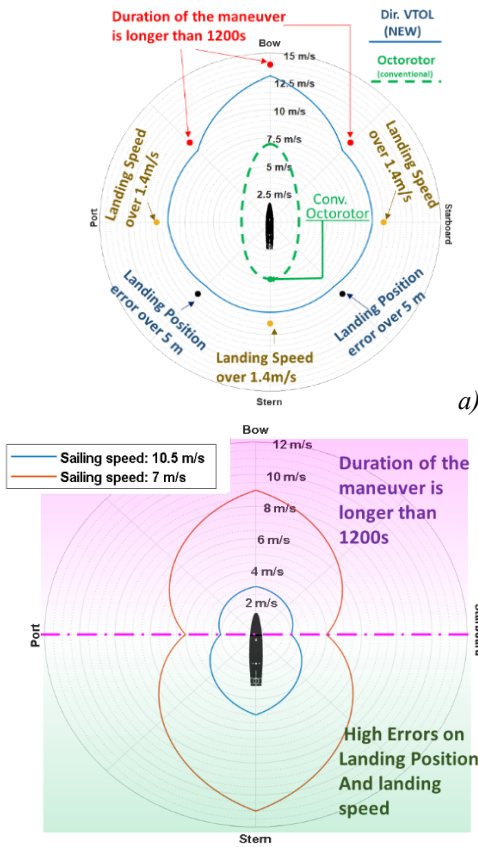


Figure 17. landing of on a moving platform with a fixed ship(a) or moving one(b)

Higher robustness of directional VTOL respect to conventional one (11) is even more evident if, as shown in figure 18/a, it is compared the UAV resistance to crosswind disturbances in a static hovering condition: the UAV is kept in a constant position hovering at constant altitude. Crosswind in different directions is applied; the maximum crosswind intensity for which the UAV is able to keep a steady position is represented. With directional yaw control, after a brief transient, the plane is able to align the longitudinal propeller against the incoming wind, so the maximum resistance to wind is substantial always the same. Otherwise, as shown if figure 18/b, the duration of the transient needed to reach a stable condition after applying the disturbance depends from the direction of wind respect to vehicle alignment. As shown in figure 18/a, applying conventional VTOL, anysotropic behavior of wing aerodynamics clearly penalizes the hovering stability of the plane along know directions.

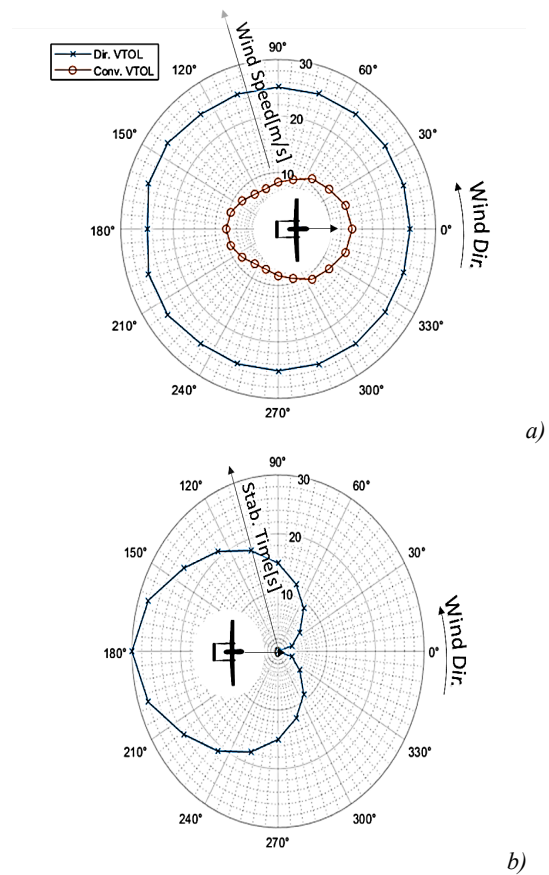


Figure 18. Maximum Tolerated Crosswind in Hovering (a), time needed by Directional VTOL to reach a stable behavior against crosswind (b)

CONCLUSIONS AND FUTURE DEVELOPMENTS

In this work authors have investigated the propulsion layout and the path control of an UAV with VTOL capabilities. Small but significant innovations introduced in both propulsion layout and path following control can increase performances and robustness of the proposed systems. Their effects can be verified with extended simulation campaigns as the ones described in this work. Considering complexity of the investigated matter thousands of different conditions and mission profiles should be evaluated confirming how powerful and efficient simulation tools are important for this kind of analysis.

The usage of concise and exhaustive graphical representations such as adopted polar plots can help researchers to summarize the general physical sense of obtained results:

- Aerodynamics of a fixed wing drone is strongly anisotropic respect to the incoming direction of crosswind disturbances. Both propulsion layout and path control algorithm used both in fixed and rotating wing mode, should be tuned to keep the plane aligned against the incoming wind maintaining a pose which is more favorable to a stable rejection of this disturbances in presence of wings. For this reason, pose in terms of pitch and roll angles should be kept stable as much as possible.

- The usage of longitudinal propeller both in fixed and rotating wing mode plays a key role. Long. propeller provides a longitudinal thrust to regulate the motion of the plane without altering the pose and without exploiting vertical propellers that are much less efficient for this purpose. In this sense a synergy between UAV alignment and action of long. propellers is fundamental.
- Crosswind disturbances introduce significant drifts respect to planned path so the control should privilege the regulation of course angle which is more representative of the real behavior of the plane respect to the heading one. Simple nonlinear controllers such as SMC are well suited to reject unmodelled dynamics and low frequency disturbances.

Next step of this work will be focused on dynamic path planning especially in the landing phase considering the interaction with the surrounding environment.

Simulation of landing maneuvers will be improved considering all the motions of the ship-deck due to wave induced motions exploiting previous research activities in the marine sector [58],[59]. Some identification of the flexible behavior of the drone [60] should be performed. Further themes for future research will regard health monitoring of actuation systems[61], integration of visual horizon line detection[62], the integration of fuzzy logic criteria in to proposed SMC controller[63].

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