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Predicting free parking slots via deep learning in short-mid terms explaining temporal impact of features

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ABSTRACT Looking for available parking slots has become a serious issue in urban mobility, since it influences traffic and emissions. This paper presents a set of metrics and techniques to predict the number of available parking slots in off-street parking facilities. This study deals with deep learning model solutions according with a mid-term prediction of 24 hours, every 15 minutes. Such a mid-term prediction can be useful for citizens who need to plan a car transfer well in advance and to reduce as much as possible any computational effort. Since most solutions in literature are focused on 1-hour ahead prediction, the proposed solution has been also tested in these conditions. The proposed solution is based on Convolutional Bidirectional LSTM models. Results have been compared in terms of precision metrics based both on occupancy and free slots. The paper also provides a framework to pass from an assessment model based on occupancy to models based on free slots and vice-versa. The obtained results have improved those already available in literature. A formal study has been conducted to perform feature relevance analysis by using explainable AI technique based on gradient and integrated gradient and proposing new heatmaps which highlighted the difference from LSTM and Bidirectional LSTM, feature relevance (base line, weather, traffic, etc.) and the impact of seasonality on predictions, namely the temporal relevance of features. The comparison has been performed on the basis of data collected in garages in the area of Florence, Tuscany, Italy by using Snap4city platform and infrastructure.

INDEX TERMS smart city, available parking lots, prediction model, machine learning, deep learning, explainable AI.

I. INTRODUCTION

Traffic management and sustainable mobility are central topics for intelligent transportation systems (ITS) so as to monitor and reduce vehicular traffic congestion [1], [2] and emissions [3], [4], [5]. Services providing available parking slots (in real time or as predictions) are becoming relevant for urban mobility management due to the increment of vehicles which need to park in cities. Drivers do waste a considerable amount of time while trying to find a vacant parking lot, especially during peak hours and in specific urban areas (e.g., hospitals, stations, parks, sport stadium). Searching for available parking spots can be a time-consuming task that simultaneously increases traffic flow [6], [7] and greenhouse gas pollution.

Parking slots can be located on the street (they are called *on-street parking*) or in parking garages with gates (named as *off-street parking*). Searching for an available parking space

has a harmful impact on both transportation system efficiency within the urban tissue and sustainability. Actually, any car parking searching activity generates unnecessary traffic workload and may affect the environment negatively due to increased vehicle emissions. These issues are surely valid when it comes to searching on-street parking, and they can be also considered in the context of off-street parking. More precisely, off-street parking with gates can be full in certain area and time slots; while in other areas, they may become full unexpectedly or due to conditions unknown to drivers. Recently, it is possible to collect real-time parking information - i.e., capacity, garage prices, number of empty parking slots in the silos or in the area - in order to realize predictive models. In terms of prediction models, there is a substantial difference between parking garages (i.e., offstreet) and on-street parking. In fact, in parking garages, the total number of available slots can be estimated by considering the total tickets produced at the entrance gate,

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and the number of outputs from exits. On the other hand, as to on-street parking, it could be necessary to detect the occupancy by means of some distributed sensor systems. Thus, two distinct research lines can be found in the literature [8], [9], focusing on either on-street parking prediction or predicting free/available parking slots inside garages (offstreet),.

The car park selection performed by a driver is influenced by multiple factors, for instance: walking distance to destination, driving and waiting time, parking fees, service level, parking size, safety [10], [11], availability and accessibility [12]. In particular, two important attributes in a parking decision-making process of any driver are: the number of available parking spaces (if known), and past experience in finding available slots.

In this paper, a solution to predict the number of available/free parking slots (not occupied) in the parking garages with gates (e.g., silos, or on flat, or under railway station) is proposed. Predictions can be usually short-term (from 15 to 60 minutes in advance), and mid-term as 24 hours (1 day in advance). Most of the studies in literature have considered 1-hour time horizon, as short-term predictions to reduce local traffic and redirect drivers towards available services at short distance. Nevertheless, literature is quite poor with respect to mid-term predictions which can be more useful for citizens to program a dedicated car trip. For example, to know the number of available hospital parking slots 1-day in advance could be of significant value for patients who have scheduled medical examinations (or need to visit an admitted family member) at the hospital, so as to program within a day in advance any related transfer by car. Moreover, the predictive capability may be influenced by different characteristics of parking place locations. More precisely, different behaviors are registered in terms of free spaces for different kinds of parking places serving different areas: suburb hospital, shopping places area as well as downtown entertainment areas within historical and pedestrian city area; plus any possible combination of those aspects. As a result, it is expected that the produced predictions should be more accurate for cases presenting regular free slots trends and seasonality (daily, weekly, monthly, etc.), thus resulting in more predictable services, with respect to cases having strongly randomized behavior and trends. A partial solution to improve precision could be to consider additional information and real time data variables such as: the description of the parking area neighborhoods, the real time or predictions about traffic flow, and the information related to weather conditions and/or forecasts [13], [14], [15].

This paper is focused on presenting an approach for short- and mid-term prediction of the number of free slots on off-street parking area which overcome the solutions from literature in terms of precision in critical conditions. The solution proposed in this paper is based on convolutional bidirectional deep learning. In addition, the paper is presenting a new approach for reasoning on feature relevance of deep learning which addressed the aspects of feature and prediction seasonality, thus, contributing to improve techniques for explainable artificial intelligence, XAI, with feature relevance magnitude and time.

The next subsection is devoted to recall the related work to allow readers to better contextualize this research topic. After that, a more detailed description of the research with its aim and goalsis reported. Finally, the paper structure is presented and commented.

A. RELATED WORKS

In literature, the problem of parking predictions has been addressed through different approaches, most of the recent proposals are using deep learning techniques [16], [17], [18], [13]. Most of them are grounded on time-series predictions, and in particular with deep recurrent neural networks, because of their capability of exploiting previous data observations. Data are typically collected from parking slots in constrained areas (off-street parking), for example, parking garages/facilities with gates where the number of offered slots is typically high, and the whole status is clearly reported in real time at the garage entrance gate. Therefore, they offer a strong appeal to drivers that may arrive all together, especially when parking facilities are located closer to attraction centers such as commercial centers, hospitals, railway stations, theatres, and multiservice areas. Differently, the turnover is faster for *on-street* parking, which may be reserved to specific categories (e.g., resident, shops, wheelchairs). The availability of the remaining free slots onstreet is more unpredictable than the availability on off-street parking areas no matter if public or private. The parking occupancy is defined as the fraction of slots that are occupied by vehicles as part of the total number of potentially available parking slots for the parking area/facility. A number of representative papers dealing with various aspects of onstreet and off-street parking are reviewed and discussed in details in [9].

In **Table I**, a comparative summary of the state-of-the-art solutions is reported for slots predictions in off-street parking facilities, since this is the focus of the paper. Such a comparison highlights the predictive goals, the adopted features, the used techniques, and the obtained results in terms of metrics: *RMSE* (Root Mean Square Error), *MAPE* (Mean Absolute Percentage Error), *MSE* (Mean Squared Error) and *MAE* (Mean Absolute Error). The definition of some of these metrics is reported later in this paper, others are discussed here as follows.

Please note that, in some cases reported in the literature, assessment metrics have been provided in terms of occupancy (defined as (*parking capacity - number of free slots*) / *parking capacity * 100*), in others in terms of free number of slots. The two mentioned assessment approaches are not equivalent. For example, in terms of *MAE*:

$$MAE = \frac{\sum_{i=1}^{n} |obs_i - pred_i|}{n}$$



According to the definition of *occupancy*, the estimation of *MAE* occupancy, *MAEo*, depends on the parking size, that is, the *Capacity*:

$$MAEo = \frac{\sum_{i=1}^{n} |obs_i - pred_i|}{n \ Capacity} \ 100$$

Thus, the relationship between *MAE* assessed on free slots, *MAEf*, and *MAEo* results to be:

$$MAEf = \frac{MAEo\ Capacity}{100}$$

For MSE:

$$MSE = \frac{\sum_{i=1}^{n} (obs_i - pred_i)^2}{n}$$

We have the following relationship between *MSE* assessed on free slots, *MSEf*, and that based on occupancy, *MSEo*:

$$MSEf = \frac{MSEo \ Capacity^{\ 2}}{100^2}$$

Similarly, for *RMSE* which is calculated as: $RMSE = \sqrt{MSE}$, thus:

$$RMSEf = \frac{RMSEo\ Capacity}{100}$$

Unfortunately, similar relationships cannot be derived for other metrics (MAPEo, MAPEf), since they are un-linearly dependent on the parking Capacity. Therefore, the comparison of results by using a set of standard metrics should be carefully performed. Reasons are: (i) the usage of non-comparable metrics depending on capacity and lack of details, (ii) the usage of different parking data sets, (iii) the adoption of additional variables such as weather, traffic, etc., (iv) the computation of assessment metrics as average in the day or week period, instead of providing precision metrics in critical conditions, which typically occur when the parking facility risks to become empty (the observation becomes close to zero). Thus, when performing the analysis of the state of the art, the identification of the best model has to take into account the results obtained in the same paper, using the same metrics and data. Moreover, an additional analysis should be derived from the explainability of machine learning and deep learning techniques, in relation to additional variables and seasonality, as discussed hereafter.

In [14], classic machine learning and predictive models have been used for off-street parking, such as Bayesian Regularized Artificial Neural Network (BRANN) [19], Support Vector Regression (SVR) [20], Recurrent Neural Network (RNN) [21], and Autoregressive Integrated Moving Average (ARIMA) [22]. The adopted feature space has included historical data, seasonal information (day, day of the week, etc.), weather aspects, and traffic flow data. Both model and comparison assessment has been performed to provide short- and mid-term predictions, every 15 minutes for the next 24 hours, in different parking context (e.g., parking lots serving markets, hospital, railway stations). The metric to assess such a performance was mainly MASEf (Mean Average Scaled Error) on free slots which can produce reliable assessment without falling in singularity when the number of free slots is close to zero. Experiments have demonstrated a better performance for BRANN with respect to other models. More recently, in [23], models based on Neural Network (NN) [24], Convolutional NN (CNN) [24], and Random Forest (RF) [25], have been compared with the aim of predicting off-street occupancy in the range of 15'-60' minutes in advance. The exploited features are similar to the ones presented in [14].

The results in [23] could demonstrate the validity of NN for any occupancy prediction (from 15 to 60 minutes in advance) in terms of *MSEo*, *MAEo* and *RMSEo* (which are dependent on the size of the parking areas), with respect to CNN, RF. In [23], the model performance has been evaluated in the parking areas of Arnhem (NL) having capacity of 1050 spaces, not reported in the paper.

In [26], a comparison of RF and CatBoost [63] has been proposed as to parking predictions. CatBoost is based on the ensemble learning method called gradient boosting and it combines different learners to get a stronger learner. The assessment has been conducted in the city of Split where parking areas are equipped with sensors and the prediction is related to the concerned area. The city of Split has 50 parking areas equipped with ground parking sensors, or a total 1516 parking areas. The study has been conducted on 44 areas and the CatBoost resulted to be the best model for predicting park utilization/occupancy. Moreover, a feature relevance analysis has identified the most important features: the historical data of parking capacity, weather conditions. In [26], the model performance has been evaluated in parking areas having an average capacity of 25 slots.

In [27], a set of statistical models, machine learning and deep learning approaches have been tested: vector regressive (VAR) [28], Gated Recurrent Units (GRU) [29] which is a class of RNN, Graph Convolutional Neural Network (GCNN) [30]. The assessment performed on a number of data sets has identified the GCNN as the best results in terms of *RMSEo* for predicting short-term occupancy of parking areas. Models have been tested on three different datasets: 76 onstreet parking areas in Italy with an average capacity of 32.69 lots; 420 on-street parking area in San Francisco with an average capacity of 9.29 stalls; 17 off-street parking area in Birmingham with an average size/capacity of 676.88 stalls. In this case, the model has considered temporal features and a distance among stalls for on-street parking and an interesting feature relevance analysis on distance for onstreet parking has been provided.

Most recent studies are focused on the application of hybrid deep learning techniques, in particular Long Short-



	TABLE I Related work solutions for off-street parking predictions.							
Authors	Target	Features	Models	Best Mo	del / R	esults	/ performa	nce
J. C. Provoost et al. [23] (2020)	Off-street occupancy prediction: 15'-60' in advance (capacity 1050)	Parking data, traffic flow data, weather data	NN, CNN, RF (predictions at 60')	MSEo MAEo RMSEo	NN 7.18 1.91 2.68	CNN 8.27 2.20 2.88	RF 7.98 1.92 2.82	
G. Jelen et al. [26] (2021)	occupancy of parking areas prediction: 60' in advance (average capacity: 25)	Ground parking sensors data, weather data	catBoost, RF (predictions at 60')	MAEo MSEo	Cat 6.7 78.	Boost 1 62	RF 6.85 90.57	
C. Lucchese et al. [27] (2022)	Occupancy on/off-street parking prediction: 15', 30', 45' and 60' (average capacity: 678)	Spatio-temporal parking data	VAR, GRU, GCNN (predictions at 60')	GCNN Parking in Parking S Parking E	n Italy an Fran irmingh	cisco iam	RMSE0 60' 0.073 0.131 0.042	
[31] (2021)	prediction: 10' in advance (up to 120')	(Euralille capacity: 2600, Gare Lille: 520)	SARIMAX, RNN-LSTM	RMSE0 MAPE0 MAPE0 >	0. 0. 6% at	126 66 60'	0.556 0.03]
C. Zeng et al. [16] (2022)	Availability of free slots off- street parking prediction (underground car park): 10' in advance	Parking data (capacity: 250)	LSTM, CONV- LSTM, BI-LSTM, CONV-BI-LSTM, DWT-Bi-LSTM	RMSEf MSEf MAEf	CONV LSTM, 10.27 105.65 7.53	-BI- 10'	DWT-B 10' 7.42 55.16 4.64	i-LSTM
Y. Feng et al. [17] (2022)	Availability of free slots off- street parking prediction: 5',15', 30', 45', 60' in advance	Spatio-temporal parking data (St7 capacity: 800)	LSTM, GRU, SVR, KNN, etc., and dConvLSTM-DCN (predictions at 60')	(St7) RMSEf MAEf MAPEf	dCon 24.60 17.69 7.28	vLSTM	-DCN, 60'	
R. K. Kasera, T. Acharjee [18] (2022)	Off-street occupancy rate prediction: time window not formally defined	Parking data (capacity from 300 to 480)	ARIMA, MLP, CNN, LSTM, GRU, CNN-LSTM	RMSE0 MAE0	28.65 8.54	LSTM k-	Avg. Percent	
E. S. Fokker et al. [13] (2022)	Occupancy off-street parking prediction: 60' and 6 months ahead (capacity from 260 to 1000)	Parking data, weather data, events, parking fee, public transport lines data	SARIMAX, ETS (6 months), LSTM (predictions at 60') (5) is a parking which may go to 0 free slots in daily hours	Diff. Parl RMSE0 (2 RMSE0 (2 RMSE0 (2 RMSE0 (2 RMSE0 (2 RMSE0 (2	king king 1) 1 2) 1 3) 1 5) 5	LSTM 0.202 1.104 1.061 0.656 2.179 1.803	SARIMAX 28.03 43.73 51.89 51.20 60.25 70.76	

Term Memory (LSTM) models [31], [32], by using the (baselines) features related to parking data time-series only. In [31], SVR, Multiple Linear Regression (MLR) [33], SARIMAX (which is seasonal ARIMA with exogenous variables) [34], and RNN-LSTM [35] have been compared. The experiments performed on several off-parking structure have demonstrated that RNN-LSTM outperformed the other models. The used dataset contained data regarding occupancy of 27 parking lots, representing a total of 18180 parking areas. The performance assessment has been conducted in Parking Euralille (center commercial) and Parking Gare Lille Europe (railway station) in the North of France, with a capacity close to 2500 and 500 stalls, respectively.

In [16], several models have been tested: LSTM, CONV-LSTM (convolutional LSTM), BI-LSTM (Bidirectional LSTM), CONV-BI-LSTM, and DWT-BI-LSTM which integrated a wavelet transform with BI-LSTM, as proposed in [36]. Such a transform divides the entire time domain into equally spaced local regions, each of which is approximated as smooth, and then the Fourier series is computed. It decomposes the signal into multiple wavelet functions according to two parameters, displacement and scale factor, in order to carry out a better extraction of time-frequency components and reduce any noise effect in the data for shortterms prediction. The described techniques are used to predict free slots of off-street parking in the next 10 minutes using the parking historical data. The used dataset includes data about the occupancy of 2 off-street parking in Chongqing. In [16], the model performance is evaluated in one of them, having its capacity close to 250 spaces.

In [17], few models have been compared: LSTM, GRU, SVR, KNN, etc., and the proposed dConvLSTM-DCN (dual Convolutional Long Short-Term Memory with Dense Convolutional Network, DCN). The latter turned out to be better to predict time slots from 5' to 60' minutes. It consists of two parallel ConvLSTM components and a DCN [37] to fully exploit the spatial-temporal correlations in the historical data related to free parking spaces considering 9 parking lots. In such a study the target is the availability of prediction related to free off-street parking spaces, up to one hour in advance. In [17], the used dataset contains the free parking spaces of 9 off-street parking lots in California. The model performance comparison is evaluated on parking (St7) with capacity close to 800 slots.

In [18] a hybrid CNN-LSTM model is proposed with multilevel parking occupancy percentage prediction via different time steps (up to 100) where no additional information in terms of external data is considered. However,



the adopted model has a best fit with respect to a set of compared models: ARIMA, MLP, CNN, LSTM and GRU for off-street occupancy rate prediction in terms of *RMSEo* and *MAEo*. The used dataset contains data about the occupancy rate of an off-street multilevel parking which is formed by 3 floors having the following capacity: 300, 317 and 480 slots, and it is not clear which parking area results are referring to. The prediction is conducted via time steps (from 1 to 100 time-steps) and a time window is not formally defined. As results, it is reported the average percentage of parking occupancy rate accuracy at k time steps (k-Average Percent).

In [13], the used dataset is enriched with weather data, events, parking fees and public transport lines data leading to both short-term prediction (60 minutes in advance) and long-term prediction (6 months ahead) for 57 off-street parking occupancy. In such a work, the comparison of models is among: SARIMAX (seasonal ARIMA with exogenous variable) [38], ETS (exponential smoothing) [39], LSTM. As described in [13], external variables, which affected parking occupancy, are related to weather conditions and events.

In [13], the used dataset contains data about the occupancy of 57 off-street parking lots in Amsterdam. The model performances have been evaluated for 6 of them having the capacity respectively close to: (1) 260, (2) 360, (3) 450, (4) 350, (5) 400, (6) 1000 (numbers corresponding to the assessment in **Table I**).

B. PAPER'S AIM AND ORGANIZATION

This work is focused on presenting research results related to a solution for predicting the number of available parking slots (free slot of off-street parking facilities) for garages in the city of Florence. Prediction of available parking spaces is a complex non-linear process whose dynamic changes involve multiple factors. Parking facilities provide several different working conditions. Some of them are dedicated to a specific facility (football stadium, hospital), others are meant for multipurpose (station, expo, downtown, etc.), and others are located on city outskirts. Variability and performance are one of the main problems to be addressed, together with the precision in critical time slots, which is when the parking is getting full, running out of available slots.

The major focus of this paper is on:

- Identification of the best prediction models among a number of machine and deep learning techniques covering what has been presented in the literature, for example: BRANN, RNN, CNN-GRU, CNN-LSTM, and CNN-BI-LSTM.
- The production of predictions, not only few minutes in advance, but for the **next 24 hours, with 15-minute sampling** with satisfactory precision. This would drastically reduce the computing prediction costs, since prediction is performed only once per day and not every few minutes, as typically proposed in literature. In addition, it may be of help for drivers planning their travel the day before. Most of state-of-the-art solutions produce predictions 1-hour ahead.

- Clarify how the different solutions can be compared one another and compare the results on the basis of assessment metrics. Compare the results in terms of Occupancy rate and Free slots according to their corresponding metrics, in the 1-hour slot prediction.
- Provide prediction results with respect to critical conditions for parking occurring when the parking facility is almost empty or full. This factor has been neglected in most solutions of related literature.
- Propose explainability techniques (XAI, explainable artificial intelligence) for assessing feature relevance (among the several ones identified in the literature) in terms of their magnitude and temporal impact, or seasonality. This approach has been adopted for the proposed deep learning solution and can be used for almost all ML and AI models in literature.

The proposed prediction model has been created in the context of a national center on sustainable mobility (MOST, in Italy) within the spoke on urban mobility and funded by the Ministry of Research, and by exploiting data and facilities of Snap4City, https://www.snapcity.org, infrastructure in the Florence / Tuscany area, Italy for Smart City [40], [41].

The paper is organized as follows. Section II considers the data description and the features definition applied to our field of research. In Section III, the deep learning model definitions are presented with their hyper-parameters tuning. Section IV presents the obtained results with short and mid-terms prediction of 1-hour and 24-hours in advance, respectively. The feature relevance analysis for the best model is described in Section V by applying gradient-based techniques. Finally, conclusions are drawn in Section VI.

II. DATA DESCRIPTION AND FEATURE DEFINITION

The main goal of current work is to find a solution to predict the number of available parking slots (free slots) in parking garages/facilities, for example controlled by a gate (off-street parking facilities). This study concerns off-street parking located in the municipality of Florence so as to identify a common predictive and flexible model for different parking areas. Such areas are of different capability and provide different behaviors in different days of the week, as well as moments of the day. Some of them may experience critical conditions when the available parking slots are close to zero. Figure 1 reports the typical daily trends of available slots for the considered parking garages, where workdays and weekends are examined. Trends are significantly different, and their related behaviors depend on the city areas and services. Therefore, there is clearly a daily and weekly seasonality. More precisely, we have considered three different representative parking areas: a suburb hospital parking location (namely Careggi car park) the behavior of which is reported in Figure 1(a), with its corresponding confidential trend considering the related standard deviation, and a capacity of 514 slots; a central parking location (namely



Beccaria car park) which is very close to the historical and pedestrian city area, having its related behavior reported in **Figure 1(b)** and a capacity of 203 slots; a parking garage located in the historical center of Florence (namely *S. Lorenzo car park*) having its related behavior reported in **Figure 1(c)** and a capacity of 179 slots. Please note that trends (working days and weekends) have been reported with their standard deviations. This permits to stress their corresponding noise level. Among them the noisiest one is *S. Lorenzo car park* due to the daily hours of market activities and the evening hours of *movida* and restaurants.

The used data refer to the period from March 1, 2022, to June 5, 2022. For each parking facility, the number of available slots has been checked and registered every 15 minutes.



(a) Careggi car park (hospital), capacity: 514



(b). Beccaria car park (downtown access), capacity: 203



(c) S. Lorenzo car park (old town access), capacity: 179

FIGURE 1. Typical daily trends (and std. dev) of available lots for different parking garages in Florence, where workdays and weekends are examined.

According to the state-of-the-art analysis, three groups of features have been identified as possible predictive metrics and they are briefly discussed in the following (see **Table II**).

TABLE II OVERVIEW OF THE EXPLOITED FEATURES THAT CAN BE OF HELP IN DESCRIBING THE CONTEXT OF PARKING USAGE WITH THEIR: CATEGORY, FEATURES AND DESCRIPTION.

Category	Features	Description of features
	Free parking slots	Real number of available slots recorded every 15 minutes
se slo	dateTime	Date and time (day, hour and minutes)
fre	dayWeek	0 for working days, 1 else
eatures of	Previous observation's difference (POD)	Difference between the number of free spaces at time i and number of free spaces at time $(i - 15 \text{ minutes})$ recorded in the previous week
Baseline f data	Subsequent observation's difference (SOD)	Difference between the number of free spaces at time i , and the number of free spaces at time (i + 15 minutes) recorded in the previous week
ier Sc	Temperature	City temperature measured one hour earlier than Time (°C)
Weatl featur	Humidity	City humidity measured one hour earlier than Time (%)
ors	Average Vehicle Speed	Average speed of vehicles on the road nearest to the parking, over one-hour period (km/h)
Sense	Vehicle Flow	Number of vehicles passing nearest to the parking, over one-hour period
affic	Average Vehicle Time	Average of distance between vehicles, over one-hour period
Tra fea	Vehicle Concentration	Number of vehicles per kilometer, over one-hour period

The features related to the *Baseline* category consider measures related to direct observation of parking data and derived information over time. This category is ordered on the basis of date and time when measures are taken. The latter include number of available slots, working day or not, etc. Values are recorded every 15 minutes. These variables are used to consider the data seasonality, which may have different trends -- i.e., the workdays with respect to the weekends, etc. Two other features have been included in the model:

- POD: difference between the actual and previous number of available spaces at the same time, recorded one week before;
- SOD: difference between the actual number of parking spaces and the next one at the same time, recorded one week before.

Features belonging to *Weather* are also collected every 15 minutes, that is, *temperature* and *humidity*. According to our analysis, the most significant values are those related to the hour before the parking time in the context of *1-hour* prevision time horizon. Therefore, in order to predict the number of free slots in a garage at 3 pm, weather features at 2 pm are relevant. In fact, weather conditions typically affect decisions, when it comes to taking the car or the public transportation. For example, the expected behavior held by citizens when it rains (according to an appropriated value of humidity and temperature), is to drive a car, instead of the



motorcycle. By doing so, more parking lots will be occupied. On this line, one would supposed to exploit long term weather forecasts (6 hours or days in advance), since they could also impact on decisions (they are accessible on the Snap4City smart city platform).

Features related to Traffic Sensors refer to values of traffic recorded by sensors which are in the neighborhood of the parking area, and mainly on the streets that can be used to reach the area [42]. Not unlike from weather data, traffic sensors values seem to be relevant if available for the previous hour with respect to the time of prediction. Typical values are the ones related to vehicle flow, concentration, average time and average speed [43]. They are estimated every 15 minutes. These metrics adopted for traffic flow estimation are those that typically are accessible from city traffic flow sensors. In this context, the value of traffic flow is used for assessing traffic conditions, and thus average values are satisfactory. Traffic sensors which are relevant for each garage may be one or more and they should be chosen considering the direction of travel and the most likely route to reach the garage. On the other hand, for other applications, such as routing path finding or what-if analysis in traffic reconstruction, more precise data and predictions should be used [44], [45], [46], [47].

III. DEFINITION OF THE PREDITING MODELS

This study can be divided into different steps: data collection, pre-processing, model training, evaluation, and deployment. In this process a large amount of data about parking occupancy must be collected, cleaned, normalized and imputed. Data missing is an unavoidable problem when dealing with real-world sensors. Parking data sensors may suffer of problems such as detector malfunction and communication failure, while there could be also some problems during every data acquisition process. All these problems can affect the monitoring of the parking state and may limit the predictive capability of the predictive models at runtime. In general, approaches of data imputation for producing surrogate data may help in creating dense data in training and execution [48].

The settings used the temporal data explicitly as the input for models, therefore it was necessary to have observations consistent and complete. Temporal data has been so rearranged to have 96 timestamps per day (24 hours and samples every 15 minutes). Missing observations of parking data have been imputed as follows: at a timestamp t of the day d a missing observation has been imputed using the average of the timestamp t of the most similar 3 days to the same day d. The model used for the imputation is K-NearestNeighbours [49] with k equal to 3, where the similarity is computed as the Euclidean distance with the nearest neighbors. More precisely, in training, we consider the imputation of missing free car parking data which corresponds to 1.1% of the measured (original) dataset.

In our general framework, different approaches are tested: BRANN, RNN, CNN-LSTM, CNN-BI-LSTM and CNN- GRU models applied well to the features presented above. More precisely, BRANN is the model producing the most reliable results according to the previous study carried out in [14] by considering data in the same car parks in Florence as it occurs in this study. Then, we have considered the most recent deep learning techniques by applying CNN-LSTM, CNN-BI-LSTM and CNN-GRU models to the datasets to improve the prevision performance.

A. ARTIFICIAL NEURAL NETWORKS WITH BAYESIAN REGULARIZATION

The Artificial Neural Network (ANN) is a supervised learning technique and it inspired by theories about how the human brain works [50], [51], [52]. Usually, ANNs tends to overfit, which in substance means to have trained the NN (Neural Network) to fit the noise trend without producing a good generalization, as expected by the ANN. However, Bayesian Regularized ANNs (BRANNs) attempts to overcome the overfitting problem by incorporating Bayes' modeling into the regularization scheme [19]. In general, the risk of overfitting increases when a neural network grows through additional hidden layer neurons. BRANN approach avoids the overfitting because regularization pushes unnecessary weights towards zero. On such grounds BRANN method is more robust and efficient than classical ANNs and network weights are typically more significant in modeling the phenomena [19]. BRANN model fits a three-layer neural network as described in [53] and [64]. The layer weights the which is initialized by the Nguyennetwork, Widrow initialization method [54], and thus, the model is given by:

$$y_{i} = g(x_{i}) + e_{i}$$

$$y_{i} = \sum_{k=1}^{s} w_{k} g_{k} \left(b_{k} + \sum_{j=1}^{p} x_{ij} \beta_{j}^{[k]} \right) + e_{i}, \quad i = 1, ..., n$$
where:

- $e_i \sim N(0, \sigma_e^2);$
- *s* is the number of neurons;
- w_k is the weight of the *k*-th neuron, k = 1, ..., s;
- b_k is a bias for the k-th neuron, k = 1, ..., s;
- $\beta_i^{[k]}$ is the weight of the *j*-th input to the net, j =1, ..., *p*;
- $g_k(\cdot)$ is the activation function: in this case:

$$g_k(x) = \frac{e^{2x} - 1}{e^{2x} + 1}$$

The objective function consists in minimizing $F = \alpha E_W +$ βE_D , where E_W is the sum of squares of network parameters (weight and bias), and E_D is the error (sum of squares), α and β are the objective function parameters.

B. RECURRENT NEURAL NETWORK

Neural Networks have been the focus of great interest for many decades, due to the desire to understand the human brain and to build learning machines. Recurrent Neural



Networks (RNNs) are basically a Feedforward Neural Network with a recurrent loop [21]. RNNs are considered a powerful model for sequential data and they are applied to a wide variety of problems involving time sequences of events and ordered data. RNN are neural networks that consists in a hidden state h and an output y that operates on a sequence of variables $\mathbf{x} = (x_1, ..., x_T)$. At each time step t, the hidden state of the RNN is updated by $h_{(t)} = f(h_{(t-1)}, x_t)$, where f is a non-linear activation function. Note that, while in principle the recurrent network is a simple and powerful model, in practice, it is hard to train properly [55].

C. CNN-LSTM

Long short-term memory (LSTM) network is an improved recurrent neural network (RNN). Many studies have shown that CNN-LSTM, which is based on a combination of a CNN layer followed by an LSTM layer, shows better prediction performance than single CNN or LSTM models [56], [57], [58]. A CNN layer normally computes input data via a convolution layer and a pooling layer and then computes the characteristic descent. The result value is obtained based on the characteristic descent. As soon as the CNN layer computation is completed, the outcome is calculated via the LSTM layer, and result values are determined. The addition of a convolutive layer is grounded on the advantage of combining powerful feature extraction of CNN with LSTM capability in capturing temporal dependencies. Two main customization techniques can be considered to optimize the model performance. They concern both architecture of the CNN-LSTM network and tuning of the hyper-parameters used during the training phase. Generally, to determine the LSTM network structure, the following variables are considered: number of layers, number of neurons and dropout function.

Moreover, as to hyper-parameters tuning of the mentioned network, several items also are considered, namely: type of optimizer, learning rate, momentum, etc. Regarding CNN network, hyper-parameters tuning is primarily related to the following items: number of filters and kernel size. In the case of study, CNN-LSTM has a 6-layers architecture structured such as:

- the first two layers are made of CNN unit layer and average pooling layer;
- the other four layers are made of LSTM network having 2 hidden layers, a dropout layer and a last layer which is a Dense layer with 96 units.

The implementation of recurrent neural networks is stateful with a number of timesteps considered equal to 96, which corresponds to the data of one day prior (24 hours) to the observation/prediction time in the case of mid-term prevision of 24 hours in advance.

The training process has been made with early stopping with patience set to 60 and weights restored to the best model. Hyperparameters, that have been optimized through a Random Search, are reported in **Table III**.

TABLE I	I HYPERPARAMETER	OPTIMIZED.

hyperparameters	value
LSTM units number	256, 512, 1024, 2048
LSTM-1 units number	16, 32, 64, 128
Filters number	4, 8, 16, 32, 64
Kernel size	2, 3, 4, 5
Dropout rate	0.0, 0.1, 0.2, 0.3, 0.4, 0.5 0.6
Learning rate	0.1, 0.01, 0.001, 0.0001
Momentum	0.0, 0.2, 0.4, 0.6, 0.8, 0.9, 0.99
Optimizer	SGD, RMSprop, Adam

The structure of the defined CNN-LSTM network is made up of the following 2 components:

- The first component is made up of a Convolutional 1dimensional layer with 16 filters and a kernel size of 3, and a AveragePooling 1dimensional layer.
- The second component consists in LSTM layers, in particular: 2 hidden layers with 1024 and 32 units, respectively, a dropout layer of 0.3 and a dense layer with 96 units.

The considered activation function is ReLu. The used optimizer is Adam Optimizer with learning rate equals to 0.001 and momentum equals to 0.9. *MAE* was selected as the loss function to be monitored during optimization. The batch size has been set to 16 and the number of epochs was set to a maximum value of 600, because the training strategy used the Early Stopping method with patience parameter set to 60 to determine the optimum epoch number, restoring the weights of the best model at the end of the learning process.

D. CNN-BI-LSTM

The LSTM layers in the above model are improved by means of a *Bidirectional* approach. The idea of Bidirectional LSTMs (BI-LSTM) is to aggregate input information in the past and future of a specific time step in LSTM models. In BI-LSTM, at any point in time, it is possible to preserve information from both past and future. In particular, the structure of the defined CNN-BI-LSTM network is made up of the following 2 components:

- The first component is made up of a Convolutional 1dimensional layer with 16 filters and a kernel size of 3, and a AveragePooling 1dimensional layer.
- The second component is the BI-LSTM layers, in particular: 2 hidden layers with 2048 (1024 +1024) and 64 (32 + 32) units, respectively, a dropout layer of 0.3 and a dense layer of 96 units.

All model settings in CNN-LSTM are preserved in the CNN-BI-LSTM one.

E. CNN-GRU

For the sake of completeness, we also consider the described model for Gated Recurrent Units (GRUs) application. GRUs are a gating mechanism in recurrent neural networks introduced in [59] and they are considered as a variation on the LSTM because both are designed similarly. In particular, GRU can be seen as a long short-term memory (LSTM) with



a forget gate, then GRU has fewer parameters than LSTM, as it lacks an output gate.

F. CONSIDERATIONS

Actually, LSTM, BI-LSTM and GRU are improved recurrent neural network (RNN) and we are going to compare them in our case of study preserving the same model setting (described above). In summary, the structure of the advanced RNN network has a CNN component, 2 (LSTM/BI-LSTM/GRU) layers, a dropout layer of 0.3 and a dense layer of 96 units, respectively. The architecture of the adopted CNN-BI-LSTM model and the related graphical representation is reported in **Figure 2**.

Layer (type)	Output Shape	Param #
conv1d (Conv1D)	(None, 166, 16)	496
average_pooling1d (AveragePooling1D)	(None, 83, 16)	0
bidirectional (Bidirectional)	(None, 83, 2048)	8527872
dropout (Dropout)	(None, 83, 2048)	0
bidirectional (Bidirectional)	(None, 64)	532736
dense (Dense)	(None, 96)	6240
Total params: 9,067,344 Trainable params: 9,067,344 Non-trainable params: 0		



FIGURE 2. The adopted CNN-BI-LSTM model architecture.

IV. EXPERIMENTAL RESULTS AND DISCUSSION

According to the data and considerations reported, the identified challenge was to create a model and tools for predicting the number of free slots in off-street parking facilities with a resolution of 15 minutes for the next 24 hours, primarily. Each predictive model produces the 96 predictions for the next day, and it can be executed for updating them every 24 hours. So that, the update every 15' nor every hour would not be strictly needed.

As usual, the dataset is split in several parts used for training the model in the learning phase and testing it, that is comparing the forecasts obtained with the trained model with the actual data contained in the testing set. As a training dataset we have elected a sample of three months, from March 1st, 2022, to June 1st, 2022. The test set has been composed by 96 daily observations (every 15 minutes) recorded during the weeks from May 23th (Monday) to June 5th (Sunday).

A. ERROR MEASUREMENT DEFINITION

As discussed in the Introduction, to calculate the prediction error, in the literature, most of the researchers have adopted the occupancy approach using *MAEo*, *MSEo* and *RMSEo*. In this paper, we prefer to use metrics based on free slots to produce measures which are independent on the parking area capacity.

The identification of the model for measuring the error is very relevant, since it has to work well close to zero. This is due to the fact that on the particular issue of street-parking predictions, critical cases occur when the available parking slots are close to zero. For this reason, we have chosen the Mean Absolute Scaled Error (MASE) by Hyndman and Koehler, 2006 in [60]. The Mean Absolute Scaled Error is calculated as follows:

$$MASE = mean(|q_t|), t = 1, ..., n$$

and

$$q_t = \frac{obs_t - pred_t}{\frac{1}{n-1}\sum_{i=2}^n |obs_i - obs_{i-1}|}$$

where:

- $obs_t = observation$ at time t
- $pred_t = prediction at time t$
- *n* is the number of the values predicted over all test sets (96 daily observations per 7 days).

Note that, as it can be easily verified, MASEf is identical to MASEo and is clearly independent on the scale of the data, and on capacity. When MASE is used for comparing predictive models, the best model is the one presenting the smaller MASE. Therefore, the MASE should be the best solution to compare solutions assessed on the basis of the occupancy or free slots.

Additional metric, with respect those presented above and, in the introduction, can include Mean Absolute Percentage Error (*MAPE*), which is calculated as follows:

$$MAPE = \frac{\sum_{i=1}^{n} \left| \frac{obs_i - pred_i}{obs_i} \right|}{n} * 100.$$

Relationship among metrics *MAPEo*, *MAPEf* cannot be easily computed a posteriori, since they are un-linearly dependent on the parking Capacity. Also, R-squared (*R2*) is not linear and for this reason has not been taken into account in the comparison.

B. PREDICTION MODEL RESULTS

The comparison has been focused by considering BRANN, RNN, CNN-GRU, CNN-LSTM and CNN-BI-LSTM on the set of car parks in Florence which is composed by (a) *Careggi* car park (Hospital) having its capacity closed to 514 spaces; (b) *Beccaria* car park (market and downtown access) having its capacity closed to 203 spaces; (c) *S. Lorenzo* car park (historical center) having its capacity closed to 179 spaces. As a result, **Table IV** reports the comparison in terms of *MASE*, *MAE* and *RMSE* over the predicted week, considering a target of 24 hours in advance, for the number of free parking spaces applied to the different locations. Moreover, a specific estimation for daily periods: morning (from 06:00:00 to 11:59:59), afternoon (from 12:00:00 to 17:59:59), evening (from 18:00:00 to 23:59:59) and night (from 00:00:00 to 05:59:59) is also considered in order to evaluate the daily moment having greater accuracy. The most critical day window is the **afternoon** to the access at the restaurant areas and for the visiting at the hospitals.

The comparison of the predictive models has been estimated on a training period of 3 months and the dataset is scaled with respect to the mean value. The error metrics have been estimated on a testing period of 1 week after the 23th of May 2022 by considering the next 24 hours. More precisely, each input (test) set gives a prevision according to the next 96 timestamps (having 15 minutes of resolution) starting from the next hour related to the last time observation in the considered input set. Each input test set admits 1 week data observation sampled each hour (168 samples or timestamps) and two consecutive input tests are progressively defined. Given two consecutive input sets A, B then A is defined in the time interval $[t_0, ..., t_{167}]$ and B is defined in the time interval $[t_0 + 15', \dots, t_{167} + 15']$. Then, each input test admits a prevision in different moment of the day. In order to evaluate the error according to a specific day moment, we are going to collect together the previsions belonging to a specific time window according with morning, afternoon, evening and night.

The comparison has put in evidence that CNN-BI-LSTM approach produced the most reliable results. Please note that the metrics are reported according to the daily time slots, in which the most critical is the afternoon since in that slot some of the parking facilities may reach zero free slots.

TABLE IV COMPARISON AMONG PREDICTIVE MODELS FOR 24 HOURS IN Advance, every 15 minutes. Darker cells are those that present better values. The metrics assessment has been performed over 1 week, with 15 minutes step.

Composison	Forecasting Techniques					
Error	DDANN	DNN	CNN-	CNN-	CNN-BI-	
LIIUI	DRAININ	KININ	GRU	LSTM	LSTM	
	Careggi ca	ar park (ho	ospital)			
MASE Night	34.2	27.0	24.0	20.4	20.7	
MASE Morning	8.6	7.2	5.3	6.0	4.7	
MASE Afterno.	10.9	7.6	5.6	6.8	5.2	
MASE Evening	10.1	6.4	7.4	6.2	6.0	
MASE (total)	10.6	8.7	7.1	7.5	6.2	
	Beccaria c	ar park (d	owntown))		
MASE Night	8.6	12.1	14.0	8.5	11.9	
MASE Morning	7.0	5.7	4.2	3.8	3.2	
MASE Afterno.	10.2	8.2	7.7	7.8	6.8	
MASE Evening	6.2	6.2	6.1	6.2	5.9	
MASE (total)	8.2	7.6	6.9	6.3	6.0	
	S. Lorenzo	o car park				
MASE Night	13.7	23.8	21.1	23.4	16.0	
MASE Morning	9.2	6.1	5.7	5.8	6.0	
MASE Afterno.	5.0	4.4	5.6	4.6	5.3	
MASE Evening	3.8	4.0	3.1	3.7	2.9	
MASE (total)	6.9	6.4	6.2	6.3	5.8	

Comparison	Forecastin	ig Techni	iques				
Error	DDANN	DNIN	CNN-	CNN-	CNN-BI-		
LIIOI	BRAININ KINI		GRU	LSTM	LSTM		
	Careggi car park (hospital)						
MAEf Night	27.6	28.7	25.6	21.7	22.0		
MAEf Morning	116.4	97.1	71.5	80.5	63.6		
MAEf Afterno.	111.8	83.4	61.9	74.4	57.5		
MAEf Evening	58.7	31.0	35.8	30.2	29.3		
MAEf (total)	78.6	60.0	48.7	51.7	43.1		
	Beccaria car park (downtown)						
MAEf Night	12.3	12.5	14.4	8.7	12.2		
MAEf Morning	38.8	30.6	22.3	20.4	17.3		
MAEf Afterno.	38.7	33.5	31.4	31.8	27.7		
MAEf Evening	30.8	20.2	19.9	20.1	19.2		
MAEf (total)	30.2	24.2	22.0	20.2	19.1		
	S. Lorenzo car park						
MAEf Night	14.3	22.1	19.6	21.7	14.9		
MAEf Morning	39.1	27.6	25.9	26.5	27.2		
MAEf Afterno.	18.4	16.9	21.4	17.7	20.3		
MAEf Evening	17.6	15.1	11.8	14.1	11.2		
MAEf (total)	22.3	20.4	19.6	20.0	18.4		

Commercian	Forecasting Techniques						
Error	BRANN	RNN	CNN- GRU	CNN- LSTM	CNN-BI- LSTM		
	Careggi ca	Careggi car park (hospital)					
RMSEf Night	38.2	36.1	32.5	28.3	27.4		
RMSEf Morning	152.6	123.5	102.7	100.4	93.8		
RMSEf Afterno.	134.1	103.0	78.9	94.6	86.0		
RMSEf Evening	72.4	40.0	46.7	39.2	39.1		
RMSEf (total)	109.5	84.8	70.7	73.1	68.0		
	Beccaria car park (downtown)						
RMSEf Night	15.6	15.7	17.2	11.7	16.7		
RMSEf Morning	45.7	39.6	29.0	28.5	23.7		
RMSEf Afterno.	45.1	42.6	39.5	37.8	36.1		
RMSEf Evening	38.6	25.8	25.0	24.9	24.1		
RMSEf (total)	38.3	32.8	28.8	27.4	26.1		
	S. Lorenzo	o car parl	ĸ				
RMSEf Night	17.2	24.7	11.5	23.6	17.8		
RMSEf Morning	44.8	31.0	29.1	29.6	30.8		
RMSEf Afterno.	23.1	21.0	26.6	23.2	25.8		
RMSEf Evening	23.4	18.6	14.9	16.9	14.4		
RMSEf (total)	29.1	24.3	23.6	23.7	23.1		

The above-presented results are related to the mid-terms forecast for the next 24 hours in terms of *MASE*, *MAEf*, *MSEf* and *RMSEf*. The computing of predictions for each hour for the next 24 hours reduces the computational costs and energy. When the data are very noisy, the results obtained with CNN-BI-LSTM are not the best but still comparable with the best results. In the critical day period, the afternoon, the best results are obtained in most cases in terms of *MASE* and *MAEf* by CNN-BI-LSTM.

In **Table V**, according to the literature, we have assessed the results with respect to 1-hour horizon consisting of the first timestamp prevision of our output model, at 24 hours. Also in this case, the CNN-BI-LSTM resulted the best model for almost all parking cases. Good results have been also obtained by CNN-GRU.



	Forecasting Techniques					
Comparison Error	BRANN	RNN	CNN- GRU	CNN- LSTM	CNN- BI- LSTM	
	Careggi car park					
MASE (1H/24)	10.6	6.6	7.4	5.9	5.5	
MAEf (1H/24)	78.6	45.8	51.2	40.6	38.0	
RMSEf (1H/24)	109.5	71.7	75.1	56.0	44.4	
	Beccaria ca	r park				
MASE (1H/24)	8.2	5.7	5.9	5.2	4.9	
MAEf (1H/24)	30.2	18.5	19.3	17.1	16.0	
RMSEf (1H/24)	38.3	25.2	24.3	23.0	20.6	
	S. Lorenzo car park					
MASE (1H/24)	6.9	6.9	5.8	6.5	5.7	
MAEf (1H/24)	22.3	22.3	18.7	21.1	18.3	
RMSEf (1H/24)	29.1	26.0	22.6	24.9	23.0	

TABLE V COMPARISON AMONG PREDICTIVE MODELS FOR 1 HOUR IN ADVANCE, ASSESSING PRECISION OF THE FIRST HOUR OF THE 24 HOURS PREVISION TARGET MODEL.

Furthermore, the studied models have been also trained for producing *1-hour* prevision, by modifying the number of units of the dense (last) layer, appropriately. So that, we specifically trained the models to produce *1-hour* prediction only. The results are reported in **Table VI**. In this case, the CNN-BI-LSTM resulted unequivocally the best model. Moreover, as expected, the estimation of a specifically trained models produced better results of the model trained for 24hours predictions. On the other hand, the differences are limited. The CNN-BI-LSTM model obtained a *MAEf* equals to 14.8, 10.3 and 9.6 and *RMSEf* equals to 17.7, 12.3 and 11.7 for *Careggi, Beccaria* and *S. Lorenzo* car parks respectively (in the context of 1-hour forecast target).

TABLE VI COMPARISON AMONG PREDICTIVE MODELS FOR 1 HOUR IN ADVANCE, ADOPTING A SPECIFIC TRAINED MODEL.

Companiaon	Forecasting Techniques						
Error (1H)	BRANN	RNN	CNN- GRU	CNN- LSTM	CNN- BI- LSTM		
	Careggi car park						
MASEf (1H)	10.6	2.4	1.8	2.2	1.1		
MAEf(1H)	78.6	32.5	24.8	29.5	14.8		
RMSEf (1H)	109.5	43.7	31.5	36.5	17.7		
	Beccaria ca	r park					
MASEf (1H)	8.2	3.3	2.7	3.3	2.0		
MAEf(1H)	30.2	16.4	13.6	16.7	10.3		
RMSEf (1H)	38.3	21.0	17.1	25.0	12.3		
	S. Lorenzo car park						
MASEf (1H)	6.9	3.4	2.8	2.2	2.0		
MAEf (1H)	22.3	16.6	13.7	10.8	9.6		
RMSEf (1H)	29.1	19.3	16.5	15.1	11.7		

According to the specific error estimation for daily periods (morning, afternoon, evening and night) we obtain **Table VII** for *MAEf* estimations and **Table VIII** for *MAEo* estimations. By means of the relation between *MAEo* and *MAEf* reported in Section I.A.

TABLE VII DAILY $MAEf$ for CNN-BI-LSTM models for 1 hour in
ADVANCE, ADOPTING A SPECIFIC TRAINED MODEL.

Companian	CNN-BI-LSTM (1 hour direct)				
Error	Careggi car Beccaria car		San Lorenzo		
LIIOI	park	park	car park		
MAEf Night	15.8	10.6	9.0		
MAEf Morning	14.2	8.4	9.9		
MAEf Afternoon	9.4	8.9	10.2		
MAEf Evening	18.7	14.1	9.7		
MAEf (daily)	14.8	10.3	9.6		

TABLE VIII DAILY MAEO FOR CNN-BI-LSTM MODELS FOR 1 HOUR IN
ADVANCE, ADOPTING A SPECIFIC TRAINED MODEL.

Companian	CNN-BI-LSTM (1 hour direct)		
Error	Careggi car	Beccaria car	San Lorenzo
LIIOI	park	park	car park
MAEo Night	3.07	5.22	5.03
MAEo Morning	2.76	4.14	5.53
MAEo Afternoon	1.83	4.38	5.70
MAEo Evening	3.64	6.95	5.42
MAEo (daily)	2.88	5.07	5.36

As it can be noticed, the best results have been registered for *Careggi* park during the morning and afternoon day periods, which are the most critical. *S. Lorenzo* provided a very noisy trends resulting in less predictable values.

C. LITERATURE COMPARISON DISCUSSION

As mentioned in the Introduction, the comparison of results with respect to the literature has to be carefully performed. Since in most cases we registered: (i) the usage of un-linear metrics or the usage of metrics depending on capacity without providing details, (ii) the usage of different parking data sets (different noise level and seasonality, see explainability in the following), which in some case also adopt additional variables such as weather, traffic, etc., (iii) the computation of assessment metrics as average in the day or week period instead of providing them in the day hours and thus in critical conditions.

Our target is related to the availability of free parking slots prediction in off-street parking which is formally different with respect to the occupancy prediction of free parking spaces in off-street parking. The most recent deep learning models have been applied to *1-hour* short-term parking prediction or shorter which is very computationally expensive.

For these reasons, the performance comparison in terms of precision can be performed only with respect to a limited number of state-of-the-art results. With the aim of comparing the results, it should be noticed that [31] and [Jelen] provide relevant values for error percentage at 60' with respect those presented in **Table VIII** with our CNN-BI-LSTM, and in particular *MAEo* of 6.71 for [31], and a *MAPEo* > 6% for [26]. Moreover, according to **Table VIII**, the proposed CNN-BI-LSTM model provides a *MAEo* of 1.83 for critical hours which overcomes the NN solution of [23] providing *MAEo* of 1.91, and those of [17]. In [17], as reported in **Table I**, the dConvLSTM-DCN model for the availability of free parking spaces prediction at *1-hour* in off-street context has been



proposed. Thus, on not very noisy car parks, it obtained a larger absolute error as *MAEf*, and comparable results normalizing their results computing *MAEo* with the information provided.

On the other hand, for mid-term predictions of 24-hours, the literature does not provide specific results, except for the analysis of [31] which detected a strong increment of error in increasing the prediction time. As it can be easily obtained by Table 4 and the definition of *MAEo*, the results for H24 prediction are: a *MAEo* of 8.39 for *Careggi* park for the whole day, which is good compromise to avoid computing 24 or 96 estimations, over 24 hours.

D. COMPUTATIONAL PERFORMANCE ANALYSIS

In **Table IX**, the comparison of execution time performance needed for the used techniques in the case of 24 hours predictions models of **Table IV**. The case of study in Beccaria car park is considered in the mentioned Table. Deep learning solutions have been executed on GPU as NVIDIA Quadro GV100 with 32GByte Ram, which has 5120 CUDA Cores, FP64 perf as 7.4 TFLOPS.

Note that, the CNN-BI-LSTM model provides a training execution time shorter than the CNN-LSTM model due to the used training strategy involving the Early Stopping method with patience parameter set to 60 to determine the optimum epoch number. In the case, the CNN-BI-LSTM model admits the optimum epoch number equal to 188 with a training execution time of 1162.32 s, while the CNN-LSTM model admits the optimum epoch number equal to 378 with a training execution time of 989.95 s. Then, for a single epoch the CNN-BI-LSTM model is time consuming with respect to CNN-LSTM as seen in the results related to the prediction execution.

TABLE IX COMPARISON OF PERFORMANCE OF THE DEEP LEARNING TECHNIQUES IN THE CONTEXT OF PARKING PREDICTION.

Model	Training	Prediction execution (s), 24	
	execution (s)	hours, 96 predictions	
BRANN	137.66	0.032	
RNN	327.41	0.836	
CNN-GRU	523.56 (130 epochs)	5.191	
CNN-LSTM	1162.32 (378 epochs)	3.926	
CNN-BI-LSTM	989.95 (188 epochs)	7.386	

V. PREDICTION MODEL EXPLAINABILITY

The level of importance of features and time lags for the multi-step prediction can be analyzed by using the gradient and integrated gradient technique [61]. Gradient, denoted by G, is a fundamental concept in machine learning to identify the direction and magnitude of the maximum growth of a function at a specific point. To calculate the Gradients and the Integrated Gradients, we created x_{test} dataset consisting of 672 arrays of timeseries (from data of Table 2) starting from Sunday to Saturday. Each array includes a timeseries of 1-week data observations sampled each hour (168 samples / timestamps).

Two consecutive arrays *A*, *B* in the x_{test} set of arrays, are translated of 15 min. Then, *A* is defined in the time interval $[t_0, ..., t_{167}]$ and *B* is defined in the time interval $[t_0 + 15', ..., t_{167} + 15']$. Let Γ be the set of features such that $\Gamma = \{POD, freeParkSlots, SOD, averageVehicleSpeed, vehicleFlow, averageVehicleTime, vehicleConcentration, temperature, humidity, dayWeek} from$ **Table II**, then we are going to consider the*j* $– th feature <math>X^j$ in Γ and $X^j_{t,i}$ is the related *i* – th observation in the *t* – th week of the *j* – th feature, with $0 \le t \le 671$, $0 \le i \le 167$ and $0 \le j \le 9$. Thus, x_{test} can be represented as follows:

$$x_{test} = \bigcup_{j=0,\dots,9} \begin{bmatrix} X^{j}_{0,0} & \cdots & X^{j}_{0,167} \\ \vdots & \ddots & \vdots \\ X^{j}_{671,0} & \cdots & X^{j}_{671,167} \end{bmatrix}$$

The visualization of the gradient helps us to understand how the steps of the input features $X^{j}_{t,i}$ affect the output of the model at each timestep *i*. In a nutshell, the gradient provides a representation of the input areas that are important for the model in predicting.

Formally, for each $X^j \in \Gamma$, we have:

$$G^{j}_{t,i} = \frac{\partial F}{\partial X^{j}} \left(X^{0}_{t,i}, \dots, X^{9}_{t,i} \right)$$

where *F* is the output function and $G^{j}_{t,i}$ is the related i – th gradient in the t – th week of the j –th feature, with $0 \le t \le 671$, $0 \le i \le 167$ and $0 \le j \le 9$.

Figure 3 shows the gradient map for the features considering CNN-BI-LSTM and CNN-LSTM models, respectively. The point having coordinates (t, i) in the j –th feature represents the i – th Gradient value according to t – th week. The steps of data input which more positively influence the prediction are reported in green, while in red are those that negatively influence the prediction. In white, the steps of input that have a low influence the predictions output.





FIGURE 3. Gradient for features for the (a) CNN-BI-LSTM and (b) CNN-LSTM models. In green, red and white the steps that influence positively, negatively and marginally the predictions, respectively. (Careggi Car Park).

According to Figure 3(a) with bidirectional layer, the features having the greatest influence at a higher value of the prediction are freeParkSlots, averageVehicleSpeed, vehicleflow and dayWeek. While the features that affect lower values of prediction are: humidity, temperature and averageVehicleTime. Humidity and freeParkSlots are the features that a larger number of steps affect the prediction of the x_{test} considered. The analysis of Figure 3(b) without the bidirectional layer, put the evidence that the predictions are obtained a quite different manner, taking into account positively POD and freeParkSlots, and negatively Humidity and DayWeek. Please note that also the scales are different in the two graphs of Figure 3. In Figure 3(a), the first 30 steps and the last 45 steps of the input have greater importance in the forecast than the middle steps. This is related on the bidirectional approach of taking data. In fact, Figure 3(b), presents relevant features only in the last hours. Thus, the white central area the Figure 3(a) graph could be interpreted that the data older than 45 hours could be less relevant for the models.

Figure 4 shows the normalized cumulated gradients for all features, as a function of hours slots for the CNN-BI-LSTM and CNN-LSTM models, respectively. On the x-axis, the i - th step of the input week hours is shown and on the y-axis the value of the normalized cumulated gradient.





FIGURE 4. Normalized cumulated gradient plot for the CNN-BI-LSTM and CNN-LSTM models, from 1 to 168 samples, Careggi car park.

Again, a different behavior is shown for bidirectional and non-bidirectional models. In fact, for the **Figure 4(b)**, the input steps most influential to the prediction are those closest to the prediction, thus the last 75 steps of the input week. These steps are much more influential than in the bidirectional model because they generate larger gradients. Thus, the structure of the CNN-BI-LSTM model allows us to capture information on the weekly seasonality of the amount of parking predicted and may need a shorter time window data to provide predictions.

D. ANALYSIS VIA INTEGRATED GRADIENTS

By estimating the Integrated Gradients, IG [62], is possible to determine the importance of individual input features for each time step of the output/prediction. The IG estimates the gradient of the output/prediction with respect to the interpolated input/features. Thus, features that play a relevant role in certain prediction sequences are identified. The idea behind IG is to calculate the weighted average of the gradients of the output/prediction function with respect to the input/features using a reference baseline.

$$IG^{j}_{t,i} = \left(\left(X^{0}_{t,i}, \dots, X^{9}_{t,i} \right) - \left(b^{0}_{t,i}, \dots, b^{9}_{t,i} \right) \right) \int \frac{\partial F}{\partial X^{j}} \left(\left(b^{0}_{t,i}, \dots, b^{9}_{t,i} \right) + \alpha \left(\left(X^{0}_{t,i}, \dots, X^{9}_{t,i} \right) - \left(b^{0}_{t,i}, \dots, b^{9}_{t,i} \right) \right) \right) d\alpha$$

where: *b* is the baseline, *F* is the output function and α is a scale value between 0 and 1 that allows interpolation between the baseline and the input. **Figure 5** shows the *IG* maps for the features and the corresponding time trend, in a week from Sunday to Saturday (right). The prediction is for the next Sunday.

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FIGURE 5. Integrated Gradient for predictions with respect to the features, for *Careggi* Car Park. In green, red and white the steps that influence positively, negatively and marginally the predictions, respectively. In blue the time trend of the feature.

Figure 5 reports the typical *IG* heatmaps computed for the CNN-BI-LSMT model on *Careggi* car park. On the other hand, it can be applied as a generic XAI approach for almost all ML and AI models in the literature.

For each j –th map, on the x-axis are the observations considered in our test dataset, and on the y-axis are the predictions considering 1-day observation with time lags of 15 minutes (96 timestamps, 24x4 time slots of 15'). In green are the steps of the output model that are most positively influenced in the prediction by means of the j –th feature, in red are the steps that are negatively influenced and in white the steps that are low influenced.

From the *IG* heatmaps, we can make several considerations. Please note that, the heatmaps of the features do not have all the same scale; *Humidity* and *freeParkSlots* are those with large magnitude. *Humidity* influences the prediction steps from step 25 up to step 50.

From almost all heatmaps, it is evident the presence of a week seasonality and a difference in relevance with a daily seasonality (along y). A different week seasonality has been registered for freeParkSlots with respect to vehicleConcentration and vehicleFlow, which are data coming from traffic flow sensors. Moreover, it is also confirmed that the predictions on Sunday are based on the values of previous Saturday, Friday, and Sunday (see averageVehicleTime). The averageVehicleTime feature has a greater influence on the first part of the forecast series. Temperature always affects negatively the predictions, with more relevance in the central part of the day. Features such as vehicleFlow, average VehicleSpeed, averageVehicleTime, vehicleConcentration and temperature have a greater influence in the prediction from step 40 to step 65.

This approach has been adopted for the proposed deep learning solution CNN-BI-LSMT and could be applied for almost all ML and AI models in the literature, with some differences in the interpretations as occurred in the gradient.

VI. CONCLUSION

The Availability off-street parking spaces prediction is a complex non-linear process involving multiple kinds of factors, as the variety of parking areas (downtown, on hospital and others on the periphery, close to theaters, airports, etc.).

The present work has been focused to find a solution for predicting the number of available parking slots in off-street case in the city of Florence for the next 24 hours in advance, every 15 minutes. Such a mid-term prevision could be very useful for drivers to plan their travel and parking the day before. Moreover, the 24H predictions allow to drastically reduce the computational costs. To this aim, we have considered and compared a number of different techniques and metrics to assessment them. We discovered in the literature two main approaches for parching prediction assessment. One based on metrics for assessing occupancy rate as percentage of fullness, and the other of absolute measure of the error in *free slot* estimation. The assessment approaches have been analyzed and compared to produce a framework which allows to compare the results obtained and measured according to these different methods.

According to the analysis a number of techniques have been compared: BRANN, RNN, CNN-GRU, CNN-LSTM, and CNN-BI-LSTM to identify the best solution in terms of precision, especially for the estimation of free slot in critical conditions (when the free slot risk to become zero). The solution identified results the better ranked in these conditions 1-hour in advance, and in producing prediction



24hours in advance (mid-terms). The comparison has been performed considering several metrics according to the two different approaches: occupancy rate and free slots.

In addition, the paper has performed a feature relevance analysis to identify the most relevant features and their impact over time since some of them provide different seasonality, and also the predictions are affected by seasonality over the week and the 24 hours. To this end, features such as the historical data, the weather conditions and the traffic flow data have been exploited and analyzed. In almost all predictive models, the historical data, traffic flow sensors and weather have demonstrated high predictive capabilities in explaining the number of free parking slots. The research documented in this paper demonstrated by using the gradient the differences from CNN-LSTM and CNN-BI-LSTM. And by using the integrated gradient and a new heatmap representations impact of seasonality in the parking predictions. This approach can be used for almost all ML and AI models in the literature.

The prediction model proposed has been created by exploiting data in the Snap4city platform and infrastructure in Florence and Tuscany area, Italy.

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