# Strength data of Italian red spruce (Picea abies) 

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## Summary

Strength data of Italian grown spruce that has been gathered during various research projects over the last 13 years have been combined into one large dataset. The data has been analysed for mechanical properties such as bending strength, modulus of elasticity as well as density. Visual grades have been determined using the German and Italian standards and were analysed for their strength profiles. Normal, Lognormal and Weibull distributions have been determined. The use of ultrasound grading as an additional parameter has been tried, but was found not very useful in improving the yield in higher strength classes.

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## Introduction

The Val di Fiemme region in Trentino is one of the largest softwood producing areas of Italy for use in structural applications. The whole province of Trentino produces around 400.000 $\mathrm{m}^{3}$ of sawn timber each year, of which a large part is used structurally. In the last 15 years strength data has been gathered in several research projects consisting of a variety of material sizes, origins and qualities. The projects dealt with both visual and machine strength grading using ultrasound. The visual grading rules applied were in accordance with Italian standards which closely resemble the German visual grading rules for softwoods. Besides visual grading all beams were also graded using ultrasound. Strength profiles have been determined in accordance with European standards EN 384. Characteristic values and the strength profiles of the subsamples have been determined and the scatter in mean and characteristic values for bending strength, modulus of elasticity and density are analysed statistically. In addition, the whole sample is analysed for the depth effect, which was found to comply well with EN 384. Ultrasound grading has been performed and the efficiency is analysed. The yield in higher strength classes is determined. A combination of both visual and ultrasound grading improved the yield in high strength classes considerably. Boundaries for the ultrasound wave speed have been determined. It was found that traditional strength profiles of EN 338 are not satisfactory for the timber studied, and for use in combination with a design standard a specific strength profile has been determined.

## 2. Material and methods

The Val di Fiemme region in Trentino is one of the largest softwood producing regions in Italy, with a production of more than $50.000 \mathrm{~m}^{3}$ each year. White and Red Spruce are the main species. Over the last fifteen years several projects have been performed to determine the characteristic strength values of the timber. The samples from a number of these projects are gathered in table 1.
Due to the different research projects not all beams were graded and tested according to the same principles. However, from all beams the visual classification according to DIN

4074/UNI 11035 has been determined and a 'knot ratio' has been determined as knot size divided by the face dimension on which the knot is visible. Furthermore, density, local MoE and bending strength have been determined in the laboratory, including ultrasound wave speed and dynamic MoE.

Table 1. Samples of Italian spruce over 13 year span.

| Sample | Year | No. | Sizes |  |  |  |
| :---: | :---: | :--- | :--- | :--- | :--- | :--- |
|  |  |  | width | depth | length | test length |
| 1 | $1991 / 1992$ | 215 | 90 | 150 | 4000 | 2700 |
| 2 | 2003 | 45 | 45 | 70 | 1400 | 1260 |
| 3 | 2003 | 50 | 45 | 70 | 2000 | 1260 |
| 4 | 2003 | 45 | 70 | 110 | 2200 | 1980 |
| 5 | 2003 | 45 | 85 | 150 | 3000 | 2700 |
| 6 | 2004 | 45 | 90 | 150 | 2200 | 2100 |
| 7 | 2004 | 45 | 90 | 145 | 2200 | 2100 |
| 8 | 2004 | 42 | 90 | 145 | 2200 | 2100 |
| 9 | 2004 | 24 | 125 | 260 | 4000 | 3800 |
| 10 | 2004 | 78 | 75 | 200 | 4200 | 3800 |
| 11 | 2004 | 72 | 90 | 250 | 4200 | 3800 |
| 12 | 2005 | 48 | 60 | 150 | 3000 | 2700 |

## 3. Visual grades

Italian standard UNI 11035 is approximately similar to DIN 4074 with regard to the knot requirements. Three grades and reject are considered, namely Grade S1, S2 and S3, corresponding to the German grades $\mathrm{S} 13, \mathrm{~S} 10, \mathrm{~S} 7$ and Reject.

Table 2 Visual grades and yield for each subsample.

| Sample |  |  |  | S1 | S2 | S3 | Reject | Whole |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. | width | depth |  |  |  |  |  |  |
| 1 | 90 | 150 | n. | 67 | 117 | 28 | 1 | $215^{1)}$ |
|  |  |  | \% | 31.2 | 54.4 | 13.0 | 0.4 | 100 |
| 2 | 45 | 70 | n. | 10 | 17 | 11 | 7 | 45 |
|  |  |  | \% | 22.2 | 37.8 | 24.4 | 15.6 | 100 |
| 3 | 45 | 70 | n. | 10 | 11 | 24 | 5 | 50 |
|  |  |  | \% | 20.0 | 22.0 | 48.0 | 10.0 | 100 |
| 4 | 70 | 110 | n. | 15 | 20 | 6 | 4 | 45 |
|  |  |  | \% | 33.3 | 44.4 | 13.3 | 8.9 | 100 |
| 5 | 85 | 150 | n. | 15 | 24 | 4 | 2 | 45 |
|  |  |  | \% | 33.3 | 53.3 | 8.9 | 4.4 | 100 |
| 6 | 90 | 150 | n. | 9 | 26 | 9 | 0 | 44 |
|  |  |  | \% | 20.4 | 59.2 | 20.4 | 0 | 100 |
| 7 | 90 | 145 | n. | 3 | 25 | 17 | 0 | 45 |
|  |  |  | \% | 6.7 | 55.5 | 37.7 | 0 | 100 |
| 8 | 90 | 145 | n. | 8 | 14 | 15 | 0 | 37 |
|  |  |  | \% | 21.6 | 37.8 | 40.5 | 0 | 100 |
| 9 | 120 | 260 | n. | 4 | 12 | 4 | 3 | 23 |
|  |  |  | \% | 18.2 | 54.5 | 17.3 | 13.6 | 100 |
| 10 | 75 | 200 | n. | 3 | 21 | 23 | 25 | 72 |
|  |  |  | \% | 4.2 | 29.2 | 31.9 | 34.7 | 100 |
| 11 | 90 | 250 | n. | 0 | 30 | 13 | 27 | 71 |
|  |  |  | \% | 0 | 42.8 | 18.5 | 38.6 | 100 |
| 12 | 60 | 150 | n. | 10 | 17 | 16 | 5 | 48 |
|  |  |  | \% | 20.8 | 35.4 | 33.3 | 10.4 | 100 |

The German grades have been assigned to strength classes C30, C24, C16 of EN 338 respectively, wheras for the Italian grades specific profiles have been set up in the national standard [UNI 11035-2]. The typical characteristic density values for strength classes C30, C 24 and C 16 are 380,350 , and $310 \mathrm{~kg} / \mathrm{m}^{3}$. Mean values are approximately $20 \%$ higher. The Italian grades S1, S2 and S3 are assigned to EN 338 strength classes C27, C22 and C16 respectively, having characteristic density values of 370,340 and $310 \mathrm{~kg} / \mathrm{m}^{3}$. The characteristic density of the samples are gathered in Annex A show that in a number of cases the minimum requirements are not met. This is especially the case for strength class C30.

## 4. Test results

The data for density, static modulus of elasticity and bending strength have been gathered for each of the subsamples in Annex A, B and C respectively. If all samples are regarded as one, the dataset contains more than 750 test results. Correlation coefficients have been determined for this basic data as well as the graded data and are gathered in Table 3 and 4 respectively.

Table 3. Basic properties of ungraded spruce

| Property | Density | Modulus of <br> Elasticity | Bending strength |
| :--- | :---: | :---: | :---: |
| Average | 420.0 | 10131 | 39.1 |
| Standard <br> deviation | 30.6 | 2141 | 12.9 |

Table 4. Basic properties for graded spruce

|  |  |  | Density <br> $\mathrm{kg} / \mathrm{m}^{3}$ |  | Modulus of Elasticity <br> $\mathrm{N} / \mathrm{mm}^{2}$ |  | Bending strength <br> $\mathrm{N} / \mathrm{mm}^{2}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Grade | n | $\%$ | Average | St.dev. | Average | St.dev | Average | St.dev |
| S1 | 155 | 10.8 | 420.1 | 31.6 | 11315 | 1864 | 49.5 | 11.6 |
| S2 | 355 | 21.0 | 420.5 | 31.6 | 10207 | 1966 | 38.8 | 11.2 |
| S3 | 168 | 45.4 | 422.9 | 29.2 | 9375 | 2139 | 33.8 | 12.3 |
| R | 80 | 22.8 | 411.9 | 26.5 | 9085 | 2196 | 31.5 | 10.1 |

The low correlation coefficient between density and bending strength $\left(\mathrm{R}^{2}=0.09\right)$ indicates that visual grading may have an effect on the bending strength and modulus of elasticity, but hardly or no effect whatsoever on the density values. This influences the strength class assignment considerably. In table 5 the correlation coefficients between the different parameters are given.

Table 5. Correlation coefficients

| Property | Density | Modulus of <br> Elasticity | Bending <br> strength | KAR |
| :--- | :---: | :---: | :---: | :---: |
| Density | 1 |  |  |  |
| Modulus of <br> Elasticity | 0.43 | 1 |  |  |
| Bending <br> trength | 0.30 | 0.71 | 1 |  |
| KAR | -0.03 | -0.47 | -0.52 | 1 |

The relationship between the knot ratio (KAR), calculated as minimum knot diameter divided by the face dimension on which the knot is visible, is show in Figure 1. The existence of a depth effect has been studied by fitting a power- equation to the basic data. Therefore, all
data-values have been divided by the average bending strength and the ratio has been plotted against the depth, see Figure 2. The depth effect could be described using the following relationship:
$k_{h}=\left(\frac{150}{h}\right)^{0.2425}$


Figure 1. Relationship between KAR and bending strength


Figure 2. Depth effect for the full dataset

## 5. Frequency distributions

 and characteristic values For the three grades (data adjusted for the depth effect) as well as for the full (ungraded) dataset, the distribution functions have been determined. In all cases it was found that Weibull and Normal distributions described the data better than log-normal distributions. the parameters of the distributions have been gathered in Table 6. In Figure 3 the data and the distributions are shown. The cumulative frequency distributions of the three grades are shown in Figure 4.The non-parametric characteristic strength values have been determined for the three different grades as well as for the ungraded material, see Table 7. In addition, the characteristic values using the three distributions are also given. From the lower tail shown in Figure 3 it can be concluded that Normal and Lognormal give an underprediction of the 5-th percentile value of the strength data whereas the Lognormal distribution gives an overprediction.

Table 6. Distribution parameters of spruce of Val di Fiemme

|  | Normal |  | Lognormal |  | Weibull (2-parameter) |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Dataset | m | s | m | s | m | v |
| All data | 38.96 | 12.09 | 3.633 | 0.339 | 42.987 | 3.421 |
| Grade S1 | 48.17 | 10.97 | 3.844 | 0.262 | 52.265 | 5.127 |
| Grade S2 | 38.25 | 10.11 | 3.628 | 0.283 | 41.884 | 4.091 |
| Grade S3 | 32.47 | 10.98 | 3.433 | 0.359 | 35.531 | 3.204 |

Table 7. Characteristic values of the bending strength

| Dataset | Normal | Lognormal | Weibull | Non-parametric |
| :---: | :---: | :---: | :---: | :---: |
| All data | 18.98 | 21.65 | 18.04 | 20.27 |
| Grade S1 | 30.10 | 30.34 | 29.28 | 27.62 |
| Grade S2 | 21.61 | 23.63 | 20.26 | 21.97 |
| Grade S3 | 14.42 | 17.16 | 14.06 | 16.22 |



Figure 3. Ungraded data of spruce of Val di Fiemme. Left: full distribution, Right: lower tale

Whereas in most cases the Non-parametric value is in between the values of the three distributions, this is not the case for Grade S1. A lower value of close to $8 \%$ is observed in this case. The non-parametric values indicate that the grades exactly fulfil the requirements for C27, C22 and C16 strength classes.
With regard to the modulus of elasticity it may be concluded that not all the requirements for the strength classes C27, C22 and C16 have been met. The requirements are 11500, 10000 and 8000 respectively and from the test results it follows that for the S 1 grade the average modulus of elasticity is 11315 and for the S2 and S3 grade 10200 and 9375 respectively. So the S1 grade fails the modulus of elasticity by $1.7 \%$. The characteristic density values for the three classes are 368,368 and $375 \mathrm{~kg} / \mathrm{m}^{3}$ for S1, S2 and S3 respectively. Officially, also here the S 1 grade fails the requirement, but the difference is extremely small. ( 368 versus 370 required). It can be concluded that all requirements for the strength classes have been met,
except for the modulus of elasticity for the S 1 grade, which is slightly to low. The characteristic modulus of elasticity parallel to the grain however is 8240 based on a standard normal distribution, whereas EN 384 specifies a value of $0.67 E_{0, \text { mean }}=7580 \mathrm{~N} / \mathrm{mm}^{2}$.


Figure 4. Cumulative frequency distributions of Grades S1, S2 and S3


Figure 5. Relationship between MoE determined using ultrasound and the bending strength

## 6. Ultrasound measurements

All beams have been measured with the Sylvatest strength grading machine. The ultrasonic wave velocity has been determined and on that basis the ultrasound modulus of elasticity. The correlation with the bending strength is shown in Figure 5 and the correlation between dynamic modulus of elasticity and static modulus of elasticity is shown in Figure 6.

Correlation between squared ultrasound speed and bending strength was slightly better than ultrasound velocity with $R^{2}=0.325$ versus $R^{2}=0.317$. This has previously also been found by Ceccotti et al. [1]. With these relatively low coefficients of determination there seems to be no benefit in applying a grading machine based on ultrasound in the industry. Multiple regression analysis using $\mathrm{MoE}_{\text {static }}$ and knot parameter gives the following results:
$f_{m}=3.643 \cdot 10^{-3} \mathrm{MoE}_{\text {stat }}-18.563 \cdot K A R+10.847$ with $\mathrm{R}^{2}=0.572$ and shown in Figure 7. or:
$f_{m}=3.332 \cdot 10^{-3}$ MoE $_{\text {ultrasound }}-33.766 \cdot K A R+9.327$ with $\mathrm{R}^{2}=0.505$ when using $\mathrm{MoE}_{\text {ultrasound }}$ The use of density as a strength determining parameter does not give an improved prediction.


Figure 6. Relationship between static MoE and ultrasonic MoE


Figure 7. Multiple regression analysis

## 7. Conclusions

A dataset of Italian red spruce has been created containing on the basis of more than 700 bending tests on visually graded material. Distribution function parameters have been determined which may be used for the derivation of characteristic values and for probabilistic calculations.

## Literature

[1] Ceccotti, A., Nakia, T., Togni, M., Strength grading of structural timber by nondestructive methods: a case study in Italy. Proc. First European Symposium on
Nondestructive Evaluation of Wood, Vol. 2, September 21-23, 1994, Sopron, Hungary, Annex A. Density values for subsamples 1 to 12.

| Sample |  |  |  | S1 | S2 | S3 | Reject | Whole |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. | width | depth |  |  |  |  |  |  |
| 1 | 90 | 150 | n. | 67 | 117 | 28 | 1 | $215{ }^{1 /}$ |
|  |  |  | $\begin{gathered} \boldsymbol{\rho}_{\mathrm{k}} \\ \boldsymbol{\rho}_{\text {mean }} \end{gathered}$ | $\begin{aligned} & 381.7 \\ & 421.5 \end{aligned}$ | $\begin{aligned} & 373.3 \\ & 420.5 \end{aligned}$ | $\begin{aligned} & 381.0 \\ & 416.5 \end{aligned}$ | [-] | $\begin{aligned} & 376.9 \\ & 420.2 \end{aligned}$ |
| 2 | 45 | 70 | n. | 10 | 17 | 11 | 7 | 45 |
|  |  |  | $\begin{gathered} \boldsymbol{\rho}_{\mathrm{k}} \\ \boldsymbol{\rho}_{\text {mean }} \end{gathered}$ | $\begin{aligned} & 351.5 \\ & 407.0 \\ & \hline \end{aligned}$ | $\begin{aligned} & 397.3 \\ & 433.5 \end{aligned}$ | $\begin{aligned} & 403.8 \\ & 440.9 \\ & \hline \end{aligned}$ | $\begin{aligned} & 389.9 \\ & 417.4 \\ & \hline \end{aligned}$ | $\begin{aligned} & 382.4 \\ & 426.9 \\ & \hline \end{aligned}$ |
| 3 | 45 | 70 | n. | 10 | 11 | 24 | 5 | 50 |
|  |  |  | $\begin{gathered} \boldsymbol{\rho}_{\mathrm{k}} \\ \boldsymbol{\rho}_{\text {mean }} \end{gathered}$ | $\begin{aligned} & 377.6 \\ & 405.8 \\ & \hline \end{aligned}$ | $\begin{aligned} & 343.8 \\ & 416.1 \end{aligned}$ | $\begin{aligned} & 383.5 \\ & 417.5 \\ & \hline \end{aligned}$ | $\begin{aligned} & 384.6 \\ & 414.6 \\ & \hline \end{aligned}$ | $\begin{aligned} & 371.2 \\ & 414.6 \\ & \hline \end{aligned}$ |
| 4 | 70 | 110 | n. | 15 | 20 | 6 | 4 | 45 |
|  |  |  | $\rho_{\mathrm{k}}$ $\rho_{\text {mean }}$ | $\begin{aligned} & 374.2 \\ & 419.1 \\ & \hline \end{aligned}$ | $\begin{aligned} & 375.4 \\ & 416.3 \end{aligned}$ | $\begin{aligned} & 363.2 \\ & 410.7 \end{aligned}$ | $\begin{aligned} & 395.5 \\ & 403.0 \end{aligned}$ | $\begin{aligned} & 374.1 \\ & 415.3 \end{aligned}$ |
| 5 | 85 | 150 | n. | 15 | 24 | 4 | 2 | 45 |
|  |  |  | $\begin{gathered} \boldsymbol{\rho}_{\mathrm{k}} \\ \boldsymbol{\rho}_{\text {mean }} \end{gathered}$ | $\begin{aligned} & 379.0 \\ & 408.3 \\ & \hline \end{aligned}$ | $\begin{aligned} & 386.1 \\ & 421.4 \end{aligned}$ | $\begin{aligned} & \hline 372.1 \\ & 407.8 \\ & \hline \end{aligned}$ | $\begin{aligned} & \hline 392.4 \\ & 404.0 \\ & \hline \end{aligned}$ | $\begin{aligned} & 381.2 \\ & 415.0 \end{aligned}$ |
| 6 | 90 | 150 | n. | 9 | 26 | 9 | 0 | 44 |
|  |  |  | $\rho_{\mathrm{k}}$ <br> $\rho_{\text {mean }}$ | $\begin{aligned} & 340.2 \\ & 398.7 \end{aligned}$ | $\begin{aligned} & 350.1 \\ & 408.7 \end{aligned}$ | $\begin{aligned} & 392.4 \\ & 410.8 \end{aligned}$ | [-] | $\begin{aligned} & 354.8 \\ & 407.1 \end{aligned}$ |
| 7 | 90 | 145 | n. | 3 | 25 | 17 | 0 | 45 |
|  |  |  | $\begin{gathered} \boldsymbol{\rho}_{\mathrm{k}} \\ \boldsymbol{\rho}_{\text {mean }} \\ \hline \end{gathered}$ | $\begin{aligned} & 318.9 \\ & 368.4 \\ & \hline \end{aligned}$ | $\begin{aligned} & 343.1 \\ & 393.9 \end{aligned}$ | $\begin{aligned} & 361.4 \\ & 424.6 \\ & \hline \end{aligned}$ | [-] | $\begin{array}{r} 342.2 \\ 403.8 \end{array}$ |
| 8 | 90 | 145 | n. | 8 | 14 | 15 | 0 | 37 |
|  |  |  | $\begin{gathered} \boldsymbol{\rho}_{\mathrm{k}} \\ \boldsymbol{\rho}_{\text {mean }} \end{gathered}$ | $\begin{aligned} & 337.8 \\ & 424.9 \end{aligned}$ | $\begin{aligned} & 367.0 \\ & 413.6 \\ & \hline \end{aligned}$ | $\begin{aligned} & 362.6 \\ & 417.6 \end{aligned}$ | [-] | $\begin{aligned} & 358.7 \\ & 417.6 \end{aligned}$ |
| 9 | 120 | 260 | n. | 4 | 12 | 4 | 3 | 23 |
|  |  |  | $\begin{gathered} \boldsymbol{\rho}_{\mathrm{k}} \\ \boldsymbol{\rho}_{\text {mean }} \end{gathered}$ | $\begin{aligned} & 347.9 \\ & 399.1 \\ & \hline \end{aligned}$ | $\begin{aligned} & 370.7 \\ & 420.9 \\ & \hline \end{aligned}$ | $\begin{aligned} & 361.8 \\ & 416.0 \\ & \hline \end{aligned}$ | $\begin{aligned} & 360.4 \\ & 430.4 \end{aligned}$ | $\begin{aligned} & 364.4 \\ & 416.7 \\ & \hline \end{aligned}$ |
| 10 | 75 | 200 | n. | 3 | 21 | 23 | 25 | 72 |
|  |  |  | $\begin{gathered} \boldsymbol{\rho}_{\mathrm{k}} \\ \boldsymbol{\rho}_{\text {mean }} \end{gathered}$ | $\begin{aligned} & 356.1 \\ & 385.2 \\ & \hline \end{aligned}$ | $\begin{aligned} & 334.8 \\ & 408.4 \end{aligned}$ | $\begin{aligned} & 388.7 \\ & 430.8 \\ & \hline \end{aligned}$ | $\begin{aligned} & 355.0 \\ & 406.7 \\ & \hline \end{aligned}$ | $\begin{aligned} & 358.3 \\ & 416.7 \\ & \hline \end{aligned}$ |
| 11 | 90 | 250 | n. | 0 | 30 | 13 | 27 | 71 |
|  |  |  | $\begin{gathered} \boldsymbol{\rho}_{\mathbf{k}} \\ \boldsymbol{\rho}_{\text {mean }} \\ \hline \end{gathered}$ | [-] | $\begin{aligned} & 372.3 \\ & 405.1 \end{aligned}$ | $\begin{aligned} & \hline 369.4 \\ & 404.3 \\ & \hline \end{aligned}$ | $\begin{aligned} & 368.0 \\ & 413.2 \\ & \hline \end{aligned}$ | $\begin{aligned} & \hline 369.6 \\ & 408.2 \\ & \hline \end{aligned}$ |
| 12 | 60 | 150 | n. | 10 | 17 | 16 | 5 | 48 |
|  |  |  | $\begin{gathered} \boldsymbol{\rho}_{\mathrm{k}} \\ \boldsymbol{\rho}_{\text {mean }} \\ \hline \end{gathered}$ | $\begin{aligned} & 374.0 \\ & 422.8 \\ & \hline \end{aligned}$ | $\begin{aligned} & 380.7 \\ & 422.7 \\ & \hline \end{aligned}$ | $\begin{aligned} & 374.8 \\ & 424.5 \\ & \hline \end{aligned}$ | $\begin{aligned} & 362.6 \\ & 409.6 \\ & \hline \end{aligned}$ | $\begin{aligned} & 376.3 \\ & 422.9 \\ & \hline \end{aligned}$ |

1) Data given differs slightly for those presented by Ceccotti et al. [1994]. The difference is caused by the fact that here the basic data is reported wheras Ceccotti et al. reported the data of 192 beams that failed inside the loading points. Differences however are small and do not affect the conclusions drawn here.

Annex B. Local Modulus of elasticity for subsamples 1 to 12.

| Sample |  |  |  | S1 | S2 | S3 | Reject | Whole |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. | width | depth |  |  |  |  |  |  |
| 1 | 90 | 150 | n. | 67 | 117 | 28 | 1 | 215 |
|  |  |  | $\mathrm{E}_{\text {mean }}$ sd. | $\begin{gathered} 12064 \\ 1395 \\ \hline \end{gathered}$ | $\begin{gathered} 10733 \\ 1764 \\ \hline \end{gathered}$ | $\begin{aligned} & 9410 \\ & 1509 \\ & \hline \end{aligned}$ | [-] | $\begin{gathered} 10976 \\ 1843 \\ \hline \end{gathered}$ |
| 2 | 45 | 70 | n. | 10 | 17 | 11 | 7 | 45 |
|  |  |  | $\mathrm{E}_{\text {mean }}$ sd. | $\begin{gathered} 10727 \\ 2872 \\ \hline \end{gathered}$ | $\begin{aligned} & 12465 \\ & 1954 \end{aligned}$ | $\begin{gathered} 12687 \\ 2263 \\ \hline \end{gathered}$ | $\begin{aligned} & 7324 \\ & 2671 \\ & \hline \end{aligned}$ | $\begin{gathered} 11333 \\ 2968 \\ \hline \end{gathered}$ |
| 3 | 45 | 70 | n. | 10 | 11 | 24 | 5 | 50 |
|  |  |  | $\begin{gathered} \hline \mathrm{E}_{\text {mean }} \\ \text { sd. } \end{gathered}$ | $\begin{gathered} 10703 \\ 2251 \end{gathered}$ | $\begin{aligned} & 9007 \\ & 1771 \end{aligned}$ | $\begin{aligned} & 8726 \\ & 2073 \\ & \hline \end{aligned}$ | $\begin{aligned} & 6275 \\ & 1422 \end{aligned}$ | $\begin{aligned} & \hline 8943 \\ & 2270 \end{aligned}$ |
| 4 | 70 | 110 | n. | 15 | 20 | 6 | 4 | 45 |
|  |  |  | $\overline{\mathrm{E}_{\text {mean }}}$ sd. | $\begin{aligned} & 10955 \\ & 1492 \\ & \hline \end{aligned}$ | $\begin{aligned} & 9907 \\ & 1474 \\ & \hline \end{aligned}$ | $\begin{aligned} & 9534 \\ & 1621 \\ & \hline \end{aligned}$ | $\begin{aligned} & \hline 8048 \\ & 2082 \\ & \hline \end{aligned}$ | $\begin{gathered} 10041 \\ 1762 \\ \hline \end{gathered}$ |
| 5 | 85 | 150 | n. | 15 | 24 | 4 | 2 | 45 |
|  |  |  | $\begin{gathered} \hline \mathrm{E}_{\text {mean }} \\ \text { sd. } \end{gathered}$ | $\begin{gathered} 10235 \\ 1530 \end{gathered}$ | $\begin{aligned} & 8760 \\ & 1240 \end{aligned}$ | $\begin{gathered} \hline 7604 \\ 697 \\ \hline \end{gathered}$ | [-] | $\begin{aligned} & 9189 \\ & 1520 \end{aligned}$ |
| 6 | 90 | 150 | n. | 9 | 26 | 9 | 0 | 44 |
|  |  |  | $\begin{gathered} \mathrm{E}_{\text {mean }} \\ \text { sd. } \\ \hline \end{gathered}$ | $\begin{gathered} 11175 \\ 2062 \\ \hline \end{gathered}$ | $\begin{gathered} 10847 \\ 1543 \\ \hline \end{gathered}$ | $\begin{array}{r} 9733 \\ 1951 \\ \hline \end{array}$ | [-] | $\begin{gathered} 10690 \\ 1767 \\ \hline \end{gathered}$ |
| 7 | 90 | 145 | n. | 3 | 25 | 17 | 0 | 45 |
|  |  |  | $\begin{gathered} \mathrm{E}_{\text {mean }} \\ \text { sd. } \\ \hline \end{gathered}$ | $\begin{array}{r} 8877 \\ 639 \\ \hline \end{array}$ | $\begin{aligned} & 8066 \\ & 1722 \\ & \hline \end{aligned}$ | $\begin{aligned} & 7750 \\ & 1273 \\ & \hline \end{aligned}$ | [-] | $\begin{aligned} & 8001 \\ & 1519 \\ & \hline \end{aligned}$ |
| 8 | 90 | 145 | n. | 8 | 14 | 15 | 0 | 37 |
|  |  |  | $\begin{gathered} \mathrm{E}_{\text {mean }} \\ \text { sd. } \\ \hline \end{gathered}$ | $\begin{gathered} 10342 \\ 2660 \\ \hline \end{gathered}$ | $\begin{array}{r} 9412 \\ 1893 \\ \hline \end{array}$ | $\begin{aligned} & 8770 \\ & 1770 \\ & \hline \end{aligned}$ | [-] | $\begin{aligned} & 9347 \\ & 2217 \\ & \hline \end{aligned}$ |
| 9 | 120 | 260 | n. | 4 | 12 | 4 | 3 | 23 |
|  |  |  | $\begin{gathered} \mathrm{E}_{\text {mean }} \\ \text { sd. } \end{gathered}$ | $\begin{gathered} 11322 \\ 880 \end{gathered}$ | $\begin{aligned} & \hline 9893 \\ & 2320 \end{aligned}$ | $\begin{aligned} & 8142 \\ & 1096 \end{aligned}$ | $\begin{aligned} & 8645 \\ & 2508 \end{aligned}$ | $\begin{aligned} & 9743 \\ & 2138 \end{aligned}$ |
| 10 | 75 | 200 | n. | 3 | 21 | 23 | 25 | 72 |
|  |  |  | $\mathrm{E}_{\text {mean }}$ sd. | $\begin{gathered} 11045 \\ 1180 \end{gathered}$ | $\begin{gathered} 10621 \\ 1827 \\ \hline \end{gathered}$ | $\begin{gathered} 10739 \\ 1706 \\ \hline \end{gathered}$ | $\begin{gathered} 10278 \\ 1666 \end{gathered}$ | $\begin{gathered} 10709 \\ 1746 \\ \hline \end{gathered}$ |
| 11 | 90 | 250 | n . | 0 | 30 | 13 | 27 | 71 |
|  |  |  | $\mathrm{E}_{\text {mean }}$ sd. | [-] | $\begin{aligned} & 9976 \\ & 1407 \\ & \hline \end{aligned}$ | $\begin{aligned} & 8678 \\ & 1020 \\ & \hline \end{aligned}$ | $\begin{aligned} & 9408 \\ & 1970 \\ & \hline \end{aligned}$ | $\begin{aligned} & 9512 \\ & 1654 \\ & \hline \end{aligned}$ |
| 12 | 60 | 150 | n. | 10 | 17 | 16 | 5 | 48 |
|  |  |  | $\mathrm{E}_{\text {mean }}$ <br> sd. | $\begin{gathered} 10675 \\ 2217 \\ \hline \end{gathered}$ | $\begin{gathered} 10061 \\ 2232 \\ \hline \end{gathered}$ | $\begin{aligned} & 9258 \\ & 2354 \\ & \hline \end{aligned}$ | $\begin{gathered} 7754 \\ 322 \\ \hline \end{gathered}$ | $\begin{aligned} & 9681 \\ & 2266 \\ & \hline \end{aligned}$ |

Annex C. Bending strength values for subsamples 1 to 12 .

| Sample |  |  |  | S1 | S2 | S3 | Reject | Whole |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. | width | depth |  |  |  |  |  |  |
| 1 | 90 | 150 | n. | 67 | 117 | 28 | 1 | 215 |
|  |  |  | $\begin{gathered} \hline f_{\text {mean }} \\ \text { sd. } \end{gathered}$ | $\begin{gathered} 53.7 \\ 8.6 \end{gathered}$ | $\begin{gathered} 42.3 \\ 8.6 \end{gathered}$ | $\begin{gathered} 35.3 \\ 7.7 \end{gathered}$ | [-] | $\begin{aligned} & 44.5 \\ & 10.6 \end{aligned}$ |
| 2 | 45 | 70 | n . | 10 | 17 | 11 | 7 | 45 |
|  |  |  | $\begin{gathered} \hline f_{\text {mean }} \\ \text { sd. } \\ \hline \end{gathered}$ | $\begin{aligned} & \hline 57.91 \\ & 17.71 \\ & \hline \end{aligned}$ | $\begin{aligned} & 58.26 \\ & 13.42 \\ & \hline \end{aligned}$ | $\begin{aligned} & 50.85 \\ & 17.69 \\ & \hline \end{aligned}$ | $\begin{gathered} 30.89 \\ 9.84 \\ \hline \end{gathered}$ | $\begin{aligned} & 52.11 \\ & 17.56 \\ & \hline \end{aligned}$ |
| 3 | 45 | 70 | n . | 10 | 11 | 24 | 5 | 50 |
|  |  |  | $\begin{gathered} \hline f_{\text {mean }} \\ \text { sd. } \\ \hline \end{gathered}$ | $\begin{aligned} & 53.09 \\ & 11.41 \\ & \hline \end{aligned}$ | $\begin{aligned} & \hline 42.88 \\ & 10.39 \\ & \hline \end{aligned}$ | $\begin{aligned} & 39.38 \\ & 11.20 \\ & \hline \end{aligned}$ | $\begin{gathered} 28.51 \\ 7.97 \\ \hline \end{gathered}$ | $\begin{aligned} & 41.85 \\ & 12.56 \\ & \hline \end{aligned}$ |
| 4 | 70 | 110 | n . | 15 | 20 | 6 | 4 | 45 |
|  |  |  | $\begin{gathered} f_{\text {mean }} \\ \text { sd. } \end{gathered}$ | $\begin{aligned} & 48.88 \\ & 11.21 \end{aligned}$ | $\begin{aligned} & 42.92 \\ & 10.55 \\ & \hline \end{aligned}$ | $\begin{gathered} 34.01 \\ 9.92 \\ \hline \end{gathered}$ | $\begin{aligned} & 32.75 \\ & 13.35 \end{aligned}$ | $\begin{aligned} & 42.81 \\ & 11.98 \\ & \hline \end{aligned}$ |
| 5 | 85 | 150 | n. | 15 | 24 | 4 | 2 | 45 |
|  |  |  | $\begin{gathered} f_{\text {mean }} \\ \text { sd. } \end{gathered}$ | $\begin{gathered} 39.37 \\ 9.48 \\ \hline \end{gathered}$ | $\begin{gathered} 32.89 \\ 9.04 \\ \hline \end{gathered}$ | $\begin{gathered} 25.55 \\ 7.03 \\ \hline \end{gathered}$ | [-] | $\begin{gathered} 34.74 \\ 9.90 \\ \hline \end{gathered}$ |
| 6 | 90 | 150 | n . | 9 | 26 | 9 | 0 | 44 |
|  |  |  | $\begin{gathered} f_{\text {mean }} \\ \text { sd. } \\ \hline \end{gathered}$ | $\begin{aligned} & 41.78 \\ & 11.29 \\ & \hline \end{aligned}$ | $\begin{gathered} 37.58 \\ 7.58 \\ \hline \end{gathered}$ | $\begin{gathered} 32.84 \\ 7.01 \\ \hline \end{gathered}$ | [-] | $\begin{gathered} 37.47 \\ 8.62 \\ \hline \end{gathered}$ |
| 7 | 90 | 145 | n . | 3 | 25 | 17 | 0 | 45 |
|  |  |  | $\begin{gathered} f_{\text {mean }} \\ \text { sd. } \end{gathered}$ | $\begin{gathered} 41.47 \\ 2.92 \\ \hline \end{gathered}$ | $\begin{array}{r} 28.17 \\ 7.78 \\ \hline \end{array}$ | $\begin{gathered} 24.30 \\ 6.55 \\ \hline \end{gathered}$ | [-] | $\begin{gathered} 27.59 \\ 8.16 \\ \hline \end{gathered}$ |
| 8 | 90 | 145 | n . | 8 | 14 | 15 | 0 | 37 |
|  |  |  | $f_{\text {mean }}$ <br> sd. | $\begin{gathered} 37.86 \\ 7.88 \end{gathered}$ | $\begin{array}{r} 32.32 \\ 9.04 \\ \hline \end{array}$ | $\begin{gathered} 27.71 \\ 8.26 \end{gathered}$ | [-] | $\begin{gathered} 31.21 \\ 9.12 \\ \hline \end{gathered}$ |
| 9 | 120 | 260 | n . | 4 | 12 | 4 | 3 | 23 |
|  |  |  | $f_{\text {mean }}$ <br> sd. | $\begin{gathered} 35.75 \\ 7.57 \end{gathered}$ | $\begin{gathered} \hline 30.55 \\ 8.07 \end{gathered}$ | $\begin{gathered} 22.56 \\ 7.08 \end{gathered}$ | $\begin{gathered} 23.50 \\ 5.69 \\ \hline \end{gathered}$ | $\begin{gathered} \hline 29.42 \\ 8.52 \end{gathered}$ |
| 10 | 75 | 200 | n . | 3 | 21 | 23 | 25 | 72 |
|  |  |  | $\begin{gathered} \hline f_{\text {mean }} \\ \text { sd. } \end{gathered}$ | $\begin{aligned} & 45.67 \\ & 11.96 \\ & \hline \end{aligned}$ | $\begin{aligned} & 39.43 \\ & 12.82 \\ & \hline \end{aligned}$ | $\begin{gathered} 40.33 \\ 8.97 \\ \hline \end{gathered}$ | $\begin{gathered} 37.02 \\ 9.82 \\ \hline \end{gathered}$ | $\begin{aligned} & \hline 39.86 \\ & 10.98 \\ & \hline \end{aligned}$ |
| 11 | 90 | 250 | n . | 0 | 30 | 13 | 27 | 71 |
|  |  |  | $\begin{gathered} \hline f_{\text {mean }} \\ \text { sd. } \\ \hline \end{gathered}$ | [-] | $\begin{gathered} 33.56 \\ 8.85 \\ \hline \end{gathered}$ | $\begin{gathered} 24.27 \\ 7.85 \\ \hline \end{gathered}$ | $\begin{gathered} 28.83 \\ 8.30 \\ \hline \end{gathered}$ | $\begin{gathered} 29.98 \\ 9.03 \\ \hline \end{gathered}$ |
| 12 | 60 | 150 | n . | 10 | 17 | 16 | 5 | 48 |
|  |  |  | $\begin{gathered} \hline f_{\text {mean }} \\ \text { sd. } \\ \hline \end{gathered}$ | $\begin{aligned} & 51.38 \\ & 10.78 \\ & \hline \end{aligned}$ | $\begin{gathered} 36.45 \\ 8.36 \\ \hline \end{gathered}$ | $\begin{aligned} & 31.97 \\ & 12.45 \\ & \hline \end{aligned}$ | $\begin{aligned} & \hline 36.63 \\ & 13.43 \\ & \hline \end{aligned}$ | $\begin{aligned} & 37.95 \\ & 13.17 \\ & \hline \end{aligned}$ |

