

# A low-complexity multiuser detector for up-link CDMA QPSK mobile radio communications

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This paper deals with a multiuser detector based on a new decorrelating approach for asynchronous up-link DS/CDMA communications in which the QPSK modulation scheme is used in transmission. It is shown here that the receiver proposed is near-far resistant and exhibits a low complexity which allows real-time operation. Performance is expressed in terms of bit error rate (BER) which has been derived by simulations under the assumption of a slowly frequency-selective Rayleigh fading channel.

## 1. Introduction

The usefulness of CDMA systems in mobile radio communications is now generally acknowledged. The Rake receiver is a widely used detection scheme in CDMA systems. However, it has been demonstrated that the conventional Rake receiver performance is impaired by the so-called near-far effect. Some researchers [2–6] have concentrated their efforts on designing multiuser detectors capable of reducing these negative phenomena. The resistance of these receivers to the near-far problem implies promising outlook for these systems in the field of personal communications. The main drawback here is the implementation complexity which has so far prevented their complete development. The implementation complexity of a multiuser detection scheme may be reduced by the sliding window decorrelating algorithm (SLWA) proposed by Wijayasuria et al. [3]. This is a practical and flexible approach suitable for applications where the number of users is high and changing with time. A modified version of the Wijayasuria et al.'s approach was recently proposed by Yoon et al. [4] and by Zheng et al. [5]. In this case the cross-correlation from the past and future symbols in the asynchronous channels is eliminated (see figure 1) by using the frame format and periodical insertion of a zero-energy bit in transmission.

This paper deals with an extension of the Yoon et al.'s method [4] to the case of a QPSK modulation scheme and slowly frequency selective Rayleigh communication channel. In particular, the QPSK scheme has been considered in order to allow a better bandwidth occupancy with respect to the BPSK scheme. Differently from [4], it is necessary to account for interference effects due to both phase and quadrature components in order to accomplish a coherent detection. This task cannot be easily achieved as in [6] for BPSK modulated signals but a suitable phase compensation algorithm is needed as outlined in section 2. Performance comparisons with the classical Rake receiver in terms of

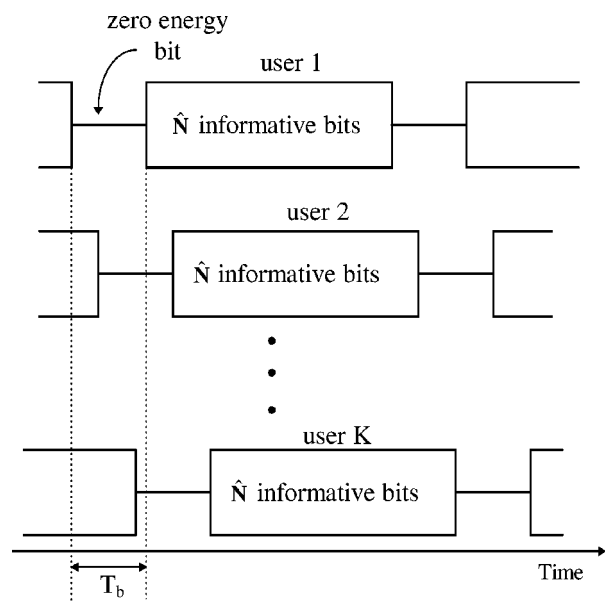


Figure 1. Transmitted data frame structure.

BER are shown in order to highlight the advantages of our detection approach.

## 2. System model

A communication system with  $K$  simultaneous users is considered herein. Each user is assumed to transmit a packet of  $N$  bits. Let  $n(t)$  be the AWGN introduced by the communication channel under the assumption of a QPSK modulation scheme and of the use of the same spreading sequence for the phase and quadrature components (as is shown in figure 2), and thus we have [2]

$$\begin{aligned}
 \mathbf{y}_I(l) + j\mathbf{y}_Q(l) = & \mathbf{R}(-1)\mathbf{C}(l+1)[i(l+1) + jq(l+1)] \\
 & + \mathbf{R}(0)\mathbf{C}(l)[i(l) + jq(l)] \\
 & + \mathbf{R}(1)\mathbf{C}(l-1)[i(l-1) + jq(l-1)] \\
 & + \mathbf{n}_I(l) + j\mathbf{n}_Q(l), \quad (1)
 \end{aligned}$$

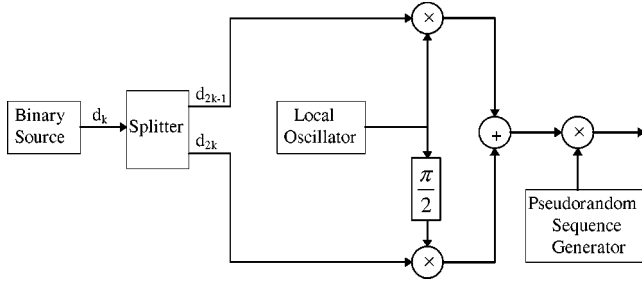


Figure 2. Transmission system block diagram.

where  $\mathbf{i}(l) + j\mathbf{q}(l)$  is the complex vector composed of the transmitted data. For example,

$$\mathbf{i}(l) = [i_1(l), i_2(l), \dots, i_{KL}(l)], \quad \text{where } i_k(l) \in \{\pm 1\}.$$

Each vector is comprised of  $KL$  elements, where  $L$  is the number of replicas of each user signal which can be discriminated at the receiving end. Each replica is considered as an individual user, so that it is still possible to exploit multiuser detection and to take advantage of the Rake diversity technique. Then,  $\mathbf{y}_I(l) + j\mathbf{y}_Q(l)$  is the complex vector composed of the matched filter outputs,  $\mathbf{C}(l)$  are the diagonal matrices whose components are the complex channel fading gains of average energy  $E_b$ :

$$c_k(l) = \sqrt{w_k(l)} e^{j\vartheta_k(l)}.$$

$\mathbf{R}(l)$  are the  $KL \times KL$  normalized signal cross-correlation matrices defined in [2] and  $\mathbf{n}_I(l) + j\mathbf{n}_Q(l)$  is due to the additive white Gaussian channel noise (AWGN) with zero mean and one-sided power spectral density equal to  $N_0$ .

Since  $\mathbf{C}(l)$  are complex matrices, it is possible to assume

$$\mathbf{C}(l) = \mathbf{C}_I(l) + j\mathbf{C}_Q(l).$$

Thus, the complex vectorial equation (1) may be decomposed in the two real vectorial equations:

$$\begin{aligned} \mathbf{y}_I(l) &= \mathbf{R}(-1)[\mathbf{C}_I(l+1)\mathbf{i}(l+1) - \mathbf{C}_Q(l+1)\mathbf{q}(l+1)] \\ &\quad + \mathbf{R}(0)[\mathbf{C}_I(l)\mathbf{i}(l) - \mathbf{C}_Q(l)\mathbf{q}(l)] \\ &\quad + \mathbf{R}(1)[\mathbf{C}_I(l-1)\mathbf{i}(l-1) - \mathbf{C}_Q(l-1)\mathbf{q}(l-1)] \\ &\quad + \mathbf{n}_I(l), \end{aligned} \quad (2)$$

$$\begin{aligned} \mathbf{y}_Q(l) &= \mathbf{R}(-1)[\mathbf{C}_I(l+1)\mathbf{q}(l+1) + \mathbf{C}_Q(l+1)\mathbf{i}(l+1)] \\ &\quad + \mathbf{R}(0)[\mathbf{C}_I(l)\mathbf{q}(l) + \mathbf{C}_Q(l)\mathbf{i}(l)] \\ &\quad + \mathbf{R}(1)[\mathbf{C}_I(l-1)\mathbf{i}(l-1) + \mathbf{C}_Q(l-1)\mathbf{q}(l-1)] \\ &\quad + \mathbf{n}_Q(l), \end{aligned} \quad (3)$$

where vectors  $\mathbf{i}(l)$  and  $\mathbf{q}(l)$  are unknown and have to be derived. To this end, we define

$$\begin{cases} \mathbf{I}(l) = \mathbf{C}_I(l)\mathbf{i}(l) - \mathbf{C}_Q(l)\mathbf{q}(l) \\ \mathbf{Q}(l) = \mathbf{C}_I(l)\mathbf{q}(l) + \mathbf{C}_Q(l)\mathbf{i}(l) \end{cases} \quad \forall l = 0, \dots, N-1. \quad (4)$$

By trivial substitution in (2) and (3), we have

$$\begin{cases} \mathbf{y}_I(0) = \mathbf{R}(-1)\mathbf{I}(1) + \mathbf{R}(0)\mathbf{I}(0) + \mathbf{n}_I(0), \\ \mathbf{y}_Q(0) = \mathbf{R}(-1)\mathbf{Q}(1) + \mathbf{R}(0)\mathbf{Q}(0) + \mathbf{n}_Q(0), \end{cases} \quad (5a)$$

$$\begin{cases} \vdots \\ \mathbf{y}_I(l) = \mathbf{R}(-1)\mathbf{I}(l+1) + \mathbf{R}(0)\mathbf{I}(l) + \mathbf{R}(1)\mathbf{I}(l-1) \\ \quad + \mathbf{n}_I(l), \\ \mathbf{y}_Q(l) = \mathbf{R}(-1)\mathbf{Q}(l+1) + \mathbf{R}(0)\mathbf{Q}(l) + \mathbf{R}(1)\mathbf{Q}(l-1) \\ \quad + \mathbf{n}_Q(l), \\ \forall l = 1, \dots, N-2, \end{cases} \quad (5b)$$

$$\begin{cases} \vdots \\ \mathbf{y}_I(N-1) = \mathbf{R}(0)\mathbf{I}(N-1) + \mathbf{R}(1)\mathbf{I}(N-2) \\ \quad + \mathbf{n}_I(N-1), \\ \mathbf{y}_Q(N-1) = \mathbf{R}(0)\mathbf{Q}(N-1) + \mathbf{R}(1)\mathbf{Q}(N-2) \\ \quad + \mathbf{n}_Q(N-1), \end{cases} \quad (5c)$$

Hereinafter, we focus on the first equations in (5). We will extend later the results obtained to the second equation. We considered a sequence formed by  $\hat{N}$  bits (window) for each user. From (5), by means of some algebraic manipulations, we have

$$\begin{aligned} &\begin{bmatrix} \mathbf{y}_I(M+1) \\ \mathbf{y}_I(M+2) \\ \mathbf{y}_I(M+3) \\ \vdots \\ \mathbf{y}_I(M+\hat{N}) \end{bmatrix} \\ &= \begin{bmatrix} \mathbf{R}(0) & \mathbf{R}(-1) & 0 & \dots & 0 \\ \mathbf{R}(1) & \mathbf{R}(0) & \mathbf{R}(-1) & \dots & 0 \\ 0 & \mathbf{R}(1) & \mathbf{R}(0) & \dots & 0 \\ \vdots & \vdots & \vdots & \vdots & \vdots \\ 0 & \dots & \dots & \mathbf{R}(1) & \mathbf{R}(0) \end{bmatrix} \begin{bmatrix} \mathbf{I}(M+1) \\ \mathbf{I}(M+2) \\ \mathbf{I}(M+3) \\ \vdots \\ \mathbf{I}(M+\hat{N}) \end{bmatrix} \\ &\quad + \begin{bmatrix} \mathbf{R}(1)\mathbf{I}(M) \\ 0 \\ \vdots \\ 0 \\ \mathbf{R}(-1)\mathbf{I}(M+\hat{N}+1) \end{bmatrix} + \begin{bmatrix} \mathbf{n}_I(M+1) \\ \mathbf{n}_I(M+2) \\ \mathbf{n}_I(M+3) \\ \vdots \\ \mathbf{n}_I(M+\hat{N}) \end{bmatrix}, \quad (6) \end{aligned}$$

where  $M$  is an offset from the start of the transmission and  $\hat{N} < N$  is the data temporal window length within the complete received sequence; the linear system (6) is composed of  $\hat{N}$  equations with  $\hat{N} + 2$  unknown values; in particular,  $\mathbf{y}_I(M+1)$  is dependent on  $\mathbf{I}(M)$  and, likewise,  $\mathbf{y}_I(M+\hat{N})$  on  $\mathbf{I}(M+\hat{N}+1)$ . Thus, we need to know these values to solve the linear system (6). One possible solution to this problem is to assume  $M = 0$  and  $\hat{N} = N$  (in this way  $\mathbf{I}(M)$  and  $\mathbf{I}(M+\hat{N}+1)$  are both equal to zero), but this is equivalent to considering the entire received sequence. This particular case is considered in [2] where  $\mathbf{R}$  is a  $NKL \times NKL$  matrix. This makes the inversion of  $\mathbf{R}$  not feasible for practical values of the sequence length  $N$ . Even the interesting solution proposed by Lupas

and Verdú [2] based on the implementation of an LTI filter becomes too complex for large  $KL$  values and cannot be performed in real time by the receiver. In order to avoid this drawback, we have adopted here a suitable approach. Our strategy is to assume terms  $\mathbf{I}(M)$  and  $\mathbf{I}(M + \hat{N} + 1)$  in (6) both equal to zero. This condition is fulfilled by means of the periodical insertion of a zero-energy bit in the informative bit sequence. In this way, the interference due to the cross-correlation of the actual symbols with the past and future symbols in the asynchronous channels can be eliminated (see figure 1). Then, parameter  $\hat{N}$  has been chosen in order to obtain a feasible solution of the linear system (6).

From figure 1 it can be seen that the transmission is arranged so that the relative differences in arrival times of the zero-energy bits at the base-station are smaller than the single-bit duration  $T_b$ , i.e.,

$$|\tau_k - \tau_l| \leq T_b \quad \forall k, l.$$

We note that the overhead needed to fulfill the synchronisation constraints is not too heavy to be unacceptable [4].

Now, the linear system (6) can be solved by exploiting the block tridiagonal structure of  $R$  (as can be seen in [3]) thanks to the following algorithm [3]:

*Sliding-window decorrelating algorithm*

$$\begin{aligned} \mathbf{Z}_1 &= \mathbf{R}(0)^{-1} \mathbf{R}(-1), \\ \mathbf{Z}_k &= [\mathbf{R}(0) - \mathbf{R}(1)\mathbf{Z}_{k-1}]^{-1} \mathbf{R}(-1), \quad k = 2, 3, \dots, \hat{N}, \\ \mathbf{W}_1 &= \mathbf{R}(0)^{-1} \mathbf{y}_I(M + 1), \\ \mathbf{W}_k &= [\mathbf{R}(0) - \mathbf{R}(1)\mathbf{Z}_{k-1}]^{-1} [\mathbf{y}_I(M + k) - \mathbf{R}(1)\mathbf{W}_{k-1}], \\ & \quad k = 2, 3, \dots, \hat{N}, \\ \mathbf{I}(M + \hat{N}) &= \mathbf{W}_{\hat{N}}, \\ \mathbf{I}(M + k) &= \mathbf{W}_k - \mathbf{Z}_k \mathbf{I}(M + k + 1), \\ & \quad k = \hat{N} - 1, \hat{N} - 2, \dots, 1. \end{aligned}$$

Thus, all the values of vectors  $\mathbf{I}(l)$  are determined. Then,  $\mathbf{Q}(l)$  is obtained by solving a similar linear system. This means that two decorrelation blocks must be used.

After all these iterations, the mutual interference among users has been eliminated, but the decorrelation block outputs are dependent on the random phase offset introduced by the multipath fading channel. Hence, a phase compensation block has been introduced. In particular, the  $k$ th element of (4) is equal to

$$\begin{cases} I_k(l) = \sqrt{w_k(l)} i_k(l) \cos \vartheta_k(l) - \sqrt{w_k(l)} q_k(l) \sin \vartheta_k(l), \\ Q_k(l) = \sqrt{w_k(l)} q_k(l) \cos \vartheta_k(l) - \sqrt{w_k(l)} i_k(l) \sin \vartheta_k(l), \\ \forall l = 1, \dots, N - 1, \end{cases} \quad (7)$$

where  $w_k(l)$  is the received power from the  $l$ th bit of the  $k$ th user and  $\vartheta_k(l)$  is the random phase introduced by the multipath fading channel. The perfect knowledge of  $\vartheta_k(l)$  is assumed, while  $w_k(l)$  has an unknown value. As can be easily seen, (7) is a simple linear system composed of two equations with two unknown values,  $\sqrt{w_k(l)} i_k(l)$  and

$\sqrt{w_k(l)} q_k(l)$ . Its solution is given by the following operations:

*Phase compensation*

$$\begin{cases} \sqrt{w_k(l)} i_k(l) = I_k(l) \cos \vartheta_k(l) + Q_k(l) \sin \vartheta_k(l), \\ \sqrt{w_k(l)} q_k(l) = Q_k(l) \cos \vartheta_k(l) - I_k(l) \sin \vartheta_k(l), \\ \forall l = 1, \dots, N - 1. \end{cases} \quad (8)$$

In this way all the values of vectors  $\mathbf{i}(l)$  are determined. Then,  $\mathbf{q}(l)$  is obtained by solving a similar linear system.

It should be emphasized that the simplicity of this solution is due to our choice of using only one pseudo-noisy sequence for each QPSK user.

Finally, the values of the decision variables are obtained. These values are affected only by the AWGN and the attenuation given by the multipath fading, but they are completely free from the interference caused by the other users and the random phase deviation introduced by the multipath fading channel. As described in [2], the decorrelation process results in a noise variance enhancement, but it does not affect its spectrum properties.

### 3. Simulation results

In this section the performance of the conventional Rake detector and that of the proposed receiver are compared in different interference environments. Moreover, the dependence of the BER performance on the frame length is investigated. In performing our simulations the following conditions have been assumed:

- Symbol rate for the QPSK modulation equal to 31.496 Ksymbols/sec.
- One spreading sequence assigned to each QPSK user (see figure 2).
- Spreading obtained through Gold sequences with processing gain equal to 127.
- Carrier frequency equal to 900 MHz.
- Doppler spread equal to 100 Hz.
- Ten interfering users communication system.

We consider an up-link Rayleigh multipath fading channel as in [1]. The hypothesis assumed allow us to consider resolvable all the 6 paths (suburban environment). Figures 3–5 show the BER performance of the proposed multiuser detector as a function of the ratio between the energy per bit at the receiving end ( $E_b$ ) and  $N_0$ , for different values of the power unbalance between the desired user signal and the interfering signals. The BER performance obtained for a classical Rake receiver with the same number of interfering users and a classical Rake receiver with a single user is also shown in the figures for comparison purposes. The good behaviour of the multiuser detector is apparent in figures 3–5. Of particular interest is the fact that the BER performance of the proposed multiuser detector is independent of the near–far effect.

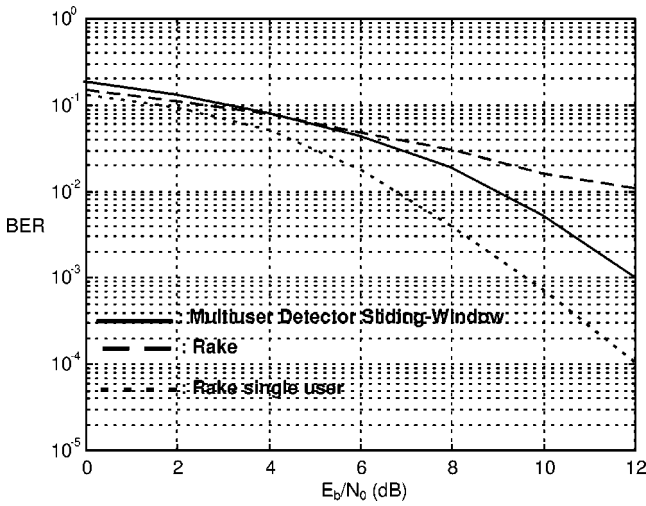


Figure 3. Bit error rate comparisons (ideal power control).

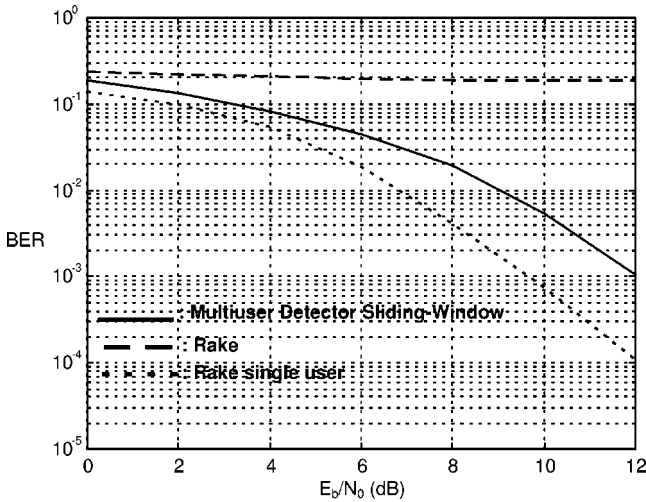


Figure 4. Bit error rate comparisons (power unbalance between the desired user signal and the interfering signals equal to 10 dB).

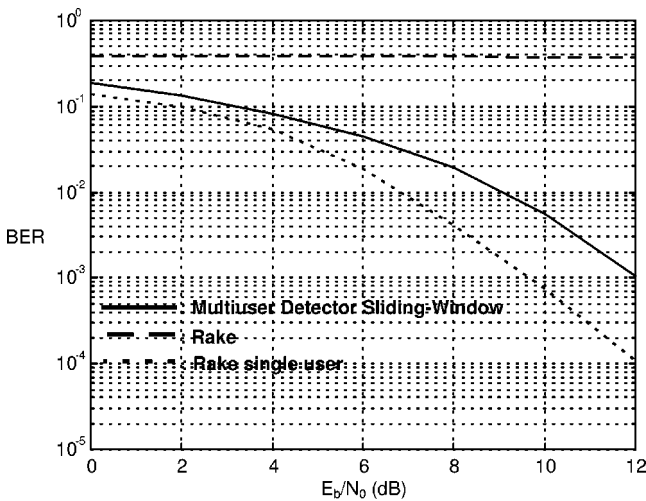


Figure 5. Bit error rate comparisons (power unbalance between the desired user signal and the interfering signals equal to 20 dB).

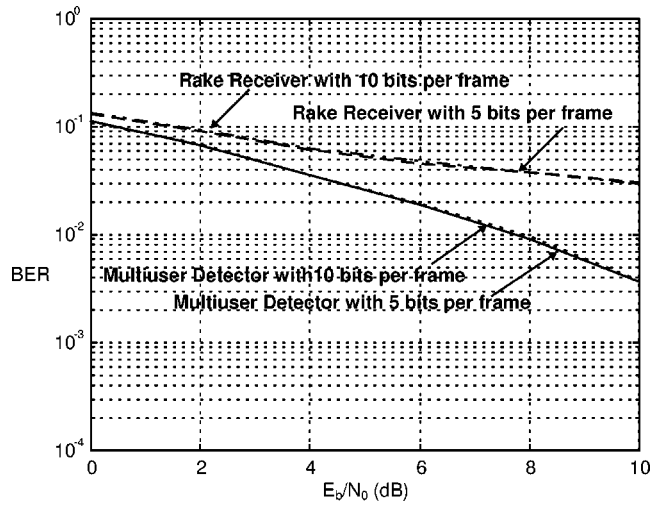


Figure 6. Bit error rate comparisons (power unbalance between the desired user signal and the interfering signals equal to 10 dB, with different frame lengths).

The results shown in figures 3–5 have been obtained by inserting a zero-energy symbol every four information bits ( $\hat{N} = 4$ ). This leads to an efficiency equal to 80%. This value is clearly too low for practical applications. The dependence of the BER performance of the proposed receiver on the frame length is investigated in figure 6 for the case of four interfering users and three resolvable paths. The power unbalance between the desired user signal and the interfering signals has been set to 10 dB. This figure proves that the BER performance is not dependent on the frame length; hence, high efficiencies are guaranteed.

#### 4. Concluding remarks

In this paper a multiuser receiver for DS/CDMA up-link communications has been presented. The near-far resistance of our receiver and its good behaviour with respect to the classical Rake receiver have been verified by means of computer simulations in the case of a slowly frequency-selective Rayleigh fading channel.

#### References

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