Collisions of Self-Bound Quantum Droplets

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We report on the study of binary collisions between quantum droplets formed by an attractive mixture of ultracold atoms. We distinguish two main outcomes of the collision, i.e., merging and separation, depending on the velocity of the colliding pair. The critical velocity v_c that discriminates between the two cases displays a different dependence on the atom number N for small and large droplets. By comparing our experimental results with numerical simulations, we show that the nonmonotonic behavior of $v_c(N)$ is due to the crossover from a compressible to an incompressible regime, where the collisional dynamics is governed by different energy scales, i.e., the droplet binding energy and the surface tension. These results also provide the first evidence of the liquidlike nature of quantum droplets in the large N limit, where their behavior closely resembles that of classical liquid droplets.

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Collisions between self-bound objects have been studied in the most diverse physical systems. The best known example is that of classical liquids. When they approach each other with a certain relative velocity, liquid drops can either merge in a single droplet (coalescence) or separate into two or more drops after collision, depending on whether or not the surface tension is sufficient to counteract the kinetic energy of the colliding pair [1-3]. Analogous studies have been carried out in the context of atomic nuclei to understand the dynamics of nuclear reactions and fission [4–7]. In the latter, for example, the transition from a single compound nucleus to the formation of two separate nuclei is governed by the interplay of collective macroscopic effects, described by the so-called liquid-drop model, and single-particle microscopic effects, related to shell corrections and pairing. Quantum effects in the collision of liquid droplets have been observed in the coalescence of helium clusters, where the merging dynamics occurs on a faster timescale with respect to classical fluids, due to the vanishing viscosity in their superfluid bulk [8–10]. In all of these cases the study of binary collisions has proved to be a powerful tool to probe the dynamical properties of self-bound systems.

In this Letter, we consider a new entry in this class of self-bound objects, i.e., quantum droplets formed by a mixture of ultracold atoms. They consist in dilute samples of bosonic atoms with attractive interactions, stabilized against collapse by the repulsive effect of quantum fluctuations [11–13]. This novel quantum phase was first predicted a few years ago [12] and it has drawn increasing attention in the community since then. Besides being a

macroscopic manifestation of quantum fluctuations, quantum droplets are predicted to display a number of interesting features. Despite being extremely dilute, for a large number of atoms they enter a liquidlike incompressible phase, highlighted by a uniform bulk density. Another exotic property is related to their excitation spectrum in the small atom number regime, where the discrete collective excitations are much higher in energy than the particle emission threshold [12], which gives rise to a selfevaporation mechanism that continuously cools the droplet, in close analogy with the decay of giant resonances in nuclei (see, e.g., Ref. [14] and references therein).

The first experimental observations of quantum droplets in atomic mixtures have been reported recently [15–17]. Besides proving the existence of a self-bound phase in a mixture of ³⁹K atoms, they also presented a first characterization of its phase diagram and equilibrium properties. In order to further look into its peculiar nature, in this work we study collisions between two quantum droplets. Analogous experimental studies in the context of ultracold atoms have been performed on bright solitons [18,19] and dipolar quantum droplets [20-22]. While in the latter case the result of collisions is mainly determined by dipolar interactions and the droplets repel each other [23], collisions of bright solitons in one-dimensional waveguides directly probe their intrinsic properties, being influenced by their relative phase or by deviations from one dimensionality [24,25]. Theoretical studies about collisions of selfbound atomic clouds have been carried out in Refs. [26,27] for one and two-dimensional mixture droplets and in Refs. [28,29] for analogous self-bound quantum balls stabilized by repulsive three-body interactions. In this Letter we show how the study of collisions between Bose-Bose mixture droplets is a powerful tool to verify the existence of a liquid regime at large atom numbers and to gain information about the energy scales of the system.

The experimental setup is analogous to the one described in Ref. [17], with a modified trap geometry adapted to the creation of two colliding droplets. We first create two separate Bose-Einstein condensates (BECs) of ³⁹K atoms in the $|1, -1\rangle$ hyperfine state (state 2) in a double-well potential, created by the superposition of a crossed dipole trap with a repulsive thin barrier that splits the BEC along the x direction [Fig. 1(a)]. By applying a radio-frequency (rf) pulse of 10 μ s, we transfer ~50% of the atoms in the $|1,0\rangle$ state (state 1), so as to create the desired attractive mixture. As already shown in Ref. [15] and Ref. [17], in a specific range of magnetic fields B, the Feshbach resonances of these two hyperfine states are such that the intraspecies scattering lengths a_{11} and a_{22} are positive, while the interspecies a_{12} is negative. When the effective scattering length $\delta a = a_{12} + \sqrt{a_{11}a_{22}}$ becomes negative, for $B < B_c = 56.85$ G, the attractive mean-field energy would lead to a collapse of the BEC, while the repulsive energy provided by quantum fluctuations, the so-called Lee-Huang-Yang energy [11], stabilizes the mixture and leads to the formation of self-bound atomic clouds. At the end of the rf pulse we thus have two quantum droplets separated by the repulsive barrier. In order to provide them a controlled and tunable velocity, we apply the following strategy [sequence sketched in Fig. 1(b)]. We first switch off the radial dipole trap and the repulsive barrier, leaving the atoms in the vertical dipole trap plus the optical

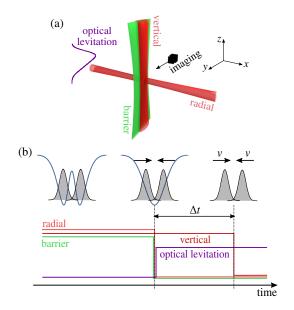


FIG. 1. Production of two colliding droplets. (a) Schematic representation of the geometry of the optical potentials. (b) Experimental sequence used to provide a controlled velocity to the droplets.

levitating potential introduced in Ref. [17]. Because of the harmonic confinement provided by the vertical beam along the x direction $[\omega_x = 2\pi \times 93(5) \text{ Hz}]$, the droplets move towards the center of the trap, acquiring an increasing velocity. After a time interval Δt we switch off the vertical beam and the two clouds keep moving towards each other along the x direction, at a constant velocity v. The value of v is tuned by changing Δt : for $\Delta t < \pi/(2\omega_x)$, increasing Δt corresponds to a larger v. Via absorption imaging along the y direction, we record the density profiles after a variable waiting time and observe the collisional dynamics.

We distinguish two different outcomes of the collision, as reported in Figs. 2(a), 2(d). When the droplets collide with velocities smaller than a critical value v_c , they merge in a single droplet, while for $v > v_c$ they separate after collision

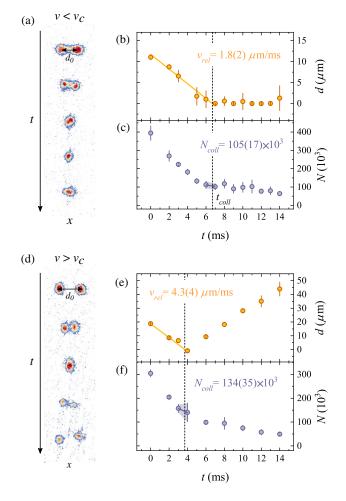


FIG. 2. Examples of two collision measurements resulting in merging (a) and separation (d) of the droplets. In (b) and (e) we report the corresponding evolution of the distance *d* between the droplets and in (c) and (f) of the total atom number *N*. A linear fit of d(t) before collision is used to measure v_{rel} and t_{coll} . N_{coll} is then deduced from a linear interpolation between the two data points adjacent to t_{coll} , as shown in (c) and (f). The data correspond to the average over four experiment repetitions. The error bars represent the statistical uncertainty and correspond to 1 standard deviation.

and keep moving in opposite directions. To measure the velocity of the collision, we fit the density profiles as a function of time t, using either a two-dimensional (2D) double-Gaussian or a single-Gaussian function, depending on whether there are two or one visible density peaks. In the former case we measure the distance between the droplets as $d = |x_L - x_R|$, where x_L and x_R are the centers of the left and right Gaussians along the x direction. In the single Gaussian case, we define d = 0. In Figs. 2(b), 2(e) we plot d(t) for the two experimental sequences reported in Figs. 2(a), 2(d): in the merging case d stabilizes to zero after collision, while it linearly increases with time when the droplets separate. Performing a linear fit of d(t) in the early stages of the collision, when the droplets are approaching each other, we can measure the relative velocity $v_{\rm rel}$ and thus the velocity of each droplet $v = v_{rel}/2$ [Figs. 2(b), 2(e)]. Another relevant parameter to characterize the observed collisional dynamics is the total atom number at collision N_{coll} . We estimate the collision time as $t_{\text{coll}} = d_0/v_{\text{rel}}$, where $d_0 = d(t = 0)$, and then we determine $N_{\text{coll}} = N(t_{\text{coll}})$ by performing a linear interpolation between the two closest data points, as in Figs. 2(c), 2(f).

We take several datasets as a function of v and N_{coll} . Note that, due to strong three-body losses in the system [as visible in Figs. 2(c), 2(f) and already described in Ref. [17]], we can tune N_{coll} by changing the initial distance between the droplets and thus the collision time t_{coll} . In the sequences reported in Fig. 2, for example, in order to have a similar N_{coll} in spite of the different v, d_0 was increased proportionally to v. In order to explore a broader range of atom numbers, we can also tune an additional parameter, i.e., the magnetic field *B*. As shown in Ref. [12], the proper variable for the description of quantum droplets is indeed the rescaled atom number

$$\tilde{N} = \frac{N}{(1+1/\alpha)n_1^{(0)}\xi^3}, \quad \text{with} \quad \xi^2 = \frac{3\hbar^2}{2m} \frac{1+\alpha}{|\delta g| n_1^{(0)}}, \quad (1)$$

where $\alpha = \sqrt{a_{22}/a_{11}}$, $\delta g = 4\pi\hbar^2 \delta a/m$, and $n_1^{(0)}$ is the equilibrium density for the atoms in state 1, whose definition is reported in Ref. [30]. \tilde{N} defines the shape of the droplet wave function, thus distinguishing between a compressible regime, where there is no distinction between the bulk and the surface, and an incompressible regime, where the wave function displays a clear flattop at the center, indicating the existence of a bulk with a fixed saturation density [Fig. 3(a)]. \tilde{N} depends on B via the scattering lengths a_{ii} , so that we can control \tilde{N}_{coll} by tuning B in a range between 56.23 and 56.44 G. Using the same rescaled units introduced in Eq. (1), the velocity of each droplet becomes $\tilde{v} = vm\xi/\hbar$. In Fig. 3(b) we report the results of the collision measurements as a function of \tilde{N}_{coll} and \tilde{v} , distinguishing between the two different outcomes: merging (red diamonds) and separation (blue squares).

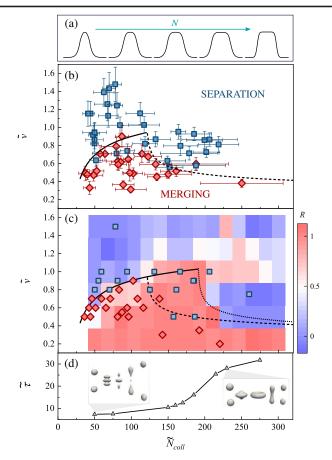


FIG. 3. Outcomes of the collision measurements (b) and simulations (c) as a function of \tilde{v} and \tilde{N}_{coll} . In (a) we draw the droplet wave function for increasing values of \tilde{N} , which shows the crossover from compressible to incompressible droplets. In (c) the results of simulations in the ideal case without losses are represented as a color plot of the ratio R introduced in the text, while the data points represent the results of the simulations with 3BL, distinguishing between merging (red diamonds) and separation (blue squares). The solid lines in (b) and (c) represent the expected trend $\tilde{v}_c \propto \sqrt{2|\tilde{E}_{drop}|/\tilde{N}}$ at small \tilde{N} , while the dotted in line in (c) is $\tilde{v}_c \propto (\tilde{N} - \tilde{N}_0)^{-1/6}$, which is the predicted scaling at large \tilde{N} . The dashed lines in (b) and (c) correspond to the same $\tilde{N}^{-1/6}$ scaling, but in this case they are simply used as a guide to the eye. In (d) we report the timescale of the collision $\tilde{\tau}$ as a function of \tilde{N}_{coll} and, in the insets, two examples of the collisional dynamics observed in the simulations without 3BL, in the two opposite cases of small and large \tilde{N} . A detailed description of the estimation of the error bars in (b) is reported in Ref. [30].

We observe a nonmonotonic behavior of the critical velocity \tilde{v}_c , setting the threshold between the two regimes: for small droplets, \tilde{v}_c increases with \tilde{N}_{coll} , while for larger droplets the trend is inverted.

In order to get a deeper insight in the physics of the collision and understand the observed behavior, we simulate numerically the dynamics of the collision by means of a modified Gross-Pitaevskii equation (GPE), equivalent to a time-dependent density functional theory within local density approximation [12,31] (see Ref. [30] for details). Similar approaches have been recently used to study both dipolar and mixture droplets [17,22,32]. Their validity for the ground state was also tested against Monte Carlo simulations [33,34]. In our case, we assume the density ratio n_1/n_2 to be frozen, which is justified by the experimental results reported in Ref. [17], where a fast stabilization of n_1/n_2 to its equilibrium value was observed. We can then write an equation for a single macroscopic wave function [12]. Using the rescaled units $\tilde{\mathbf{r}} = \mathbf{r}/\xi$ and $\tilde{t} = \hbar t/m\xi^2$, the modified GPE reads simply

$$i\frac{\partial}{\partial \tilde{t}}\psi = -\frac{1}{2}\Delta_{\tilde{\mathbf{r}}}\psi - 3|\psi|^2\psi + \frac{5}{2}|\psi|^3\psi, \qquad (2)$$

where the second term on the right-hand side corresponds to the negative mean-field energy and the last term is the positive Lee-Huang-Yang correction due to quantum fluctuations [30]. The initial state is represented by two quantum droplets with $\tilde{N}/2$ atoms each, separated by a certain distance to ensure that no overlap exists between them. We provide them a certain velocity \tilde{v} , so that they move towards each other, and then we observe the result of the collision. In order to distinguish between merging and separation, we measure, at large times after the collision, the ratio $R = n_{\rm cm}/(n_{\rm cm} + n_{\rm out})$, where $n_{\rm cm}$ is the density at the center of mass and n_{out} is the peak density of the outgoing clouds. The results are reported in Fig. 3(c). We observe a qualitative agreement with the experimental outcomes of Fig. 3(b), but a quantitative difference in the position of the maximum of $\tilde{v}_c(\tilde{N})$, which is here shifted to $\tilde{N} \sim 200$. To understand the origin of this discrepancy, we perform a new set of simulations including the effect of three-body losses (3BL). They are inserted in Eq. (2) as an imaginary term $-i(\tilde{K}/2)|\psi|^4\psi$, where the parameter $\tilde{K} = 0.53$ is determined by fitting the experimental atom number decay. In Fig. 3(c) we compare the new results (red diamonds and blue squares) with those obtained for the ideal case of no losses. While at small \tilde{N} the position of \tilde{v}_c is basically unaffected by losses, at larger \tilde{N} , 3BL shift the maximum of \tilde{v}_c to $\tilde{N} \sim 120$, in good agreement with the experimental results.

We can qualitatively understand the two opposite trends of $\tilde{v}_c(\tilde{N})$ at small and large \tilde{N} and the effect of losses, by drawing a simple argument. The possibility of forming a single droplet during the collision is related to the capability of the resulting merged droplet to absorb the excess kinetic energy $\tilde{E}_{kin} \propto \tilde{v}^2 \tilde{N}$. In the liquid regime at large \tilde{N} , we can decompose the energy of the droplet using the so-called liquid-drop model [35]: $\tilde{E}_{drop}(\tilde{N}) =$ $E_B \tilde{N} + E_S \tilde{N}^{2/3} + E_C \tilde{N}^{1/3}$, where the three terms represent the bulk, surface, and curvature energies, respectively. The first and the last term can be neglected, since the bulk

energy scales linearly with \tilde{N} , and is thus conserved during the collision, and the curvature energy is negligible for large \tilde{N} . The only relevant energy scale is thus provided by the surface, which can also host discrete excitations to absorb the collision kinetic energy. Analogously to the Weber number criterion for classical liquid droplets [2], we can thus conclude that the condition for merging should be given by $\tilde{E}_{kin} \lesssim E_s \tilde{N}^{2/3}$, which means $\tilde{v}_c \propto \tilde{N}^{-1/6}$. In the opposite case of small \tilde{N} , there is no distinction between the bulk and the surface and one would expect the whole binding energy of the droplet to be the relevant energy scale. By imposing $\tilde{E}_{kin} \sim \tilde{E}_{drop}$ one gets a critical velocity $\tilde{v}_c \sim \sqrt{2|\tilde{E}_{drop}|}/\tilde{N}$. In Fig. 3(c) we compare these expected trends with the numerical simulations performed in the absence of 3BL and we find that these simple energetic considerations qualitatively justify the observed behavior. The crossover from compressible to incompressible droplets, governed by the two different energy scales, is highlighted by the timescales of the collision. In the simulations without 3BL, we consider collisions with \tilde{v} slightly above \tilde{v}_c and we estimate the time interval $\tilde{\tau}$ between \tilde{t}_{coll} and the time when the distance between the two density peaks along x becomes larger than the radial size of the droplets, for different \tilde{N} [Fig. 3(d)]. We observe a clear slowing down of the collisional dynamics as the droplet enters the liquid regime, where the surface tension dominates. In that limit, our simulations show a behavior closely analogous to the reflexive separation known in the context of classical drops (see, e.g., Ref. [1]): after colliding, the two droplets form a single excited cloud for a certain time interval, but they eventually separate when the surface tension is not sufficient to compensate for the kinetic energy of the internal flow [right inset of Fig. 3(d)]. In the compressible case, instead, the separation occurs on a much shorter timescale, since the two droplets basically pass through each other [left inset of Fig. 3(d)]. The reason for the different importance of 3BL in the two regimes lies exactly in the different timescale of the collision. The longer $\tilde{\tau}$ in the incompressible regime implies that, in the presence of 3BL, the atom number decreases significantly during the relevant time interval, so that the final surface tension is reduced. This corresponds to a smaller \tilde{v}_c and thus to a shift in the position of the backbending, as highlighted by the dashed lines in Figs. 3(b), 3(c), used in this case as a simple guide to the eye, since a proper scaling in the presence of 3BL is harder to deduce.

As a final remark, it is worth mentioning that the experimental procedure used to prepare the two initial droplets is such that there is no definite relative phase between them. In order to reproduce the incoherent preparation of the experiment, in the numerical simulations we set the initial phase difference to zero, which corresponds to minimizing the effects of phase gradients during the collision, thus recovering the proper hydrodynamic

equations. Studying the effect of a finite relative phase is an interesting perspective of this work and it is the subject of ongoing investigations.

In conclusion we have shown that binary collisions are a good probe of the dynamical properties of 3D mixture droplets. By comparing our experimental results with the outcomes of numerical simulations, we found evidence of a crossover from compressible to incompressible quantum droplets driven by \tilde{N} . This is highlighted by the different trend of $\tilde{v}_c(\tilde{N})$, which is well justified by simple energetic considerations. In the future it would be interesting to study the coalescence dynamics of two droplets colliding at very small velocities, which, in analogy to previous studies on helium clusters [8–10], could be a probe of their superfluid properties. One could also investigate the formation of vortices during the collision and characterize the collective excitations of the merged droplets.

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