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## HEAT TRANSFER APPLICATIONS IN TURBOMACHINERY

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### SUMMARY

This paper describes the development and validation steps needed to improve OpenFOAM standard release suitability for gas turbine heat transfer applications. The focus is on steady-state simulations as at the state of the art RANS is still considered a valid CFD approach especially for cases of industrial interest.

The most critical aspects were defined to be: the implementation of a steady state solver able at solving different kind of flow regimes, from almost incompressible to high Mach flows, and the turbulence modeling. A SIMPLE like algorithm was specifically developed to solve the fully three dimensional, steady state form of compressible Navier Stokes equations. Moreover a set of various eddy viscosity models, including several Low-Reynolds k-epsilon models also with realizability constraint and the Two Layer k-epsilon model were implemented. Due to the good performances obtained with the k-omega SST in wall-bounded flows using a Low Reynolds approach, an automatic wall treatment switching automatically from a wall-function to a Low-Reynolds formulation has been added for such model to obtain mesh independence also at high  $y_p^+$ . In addition an anisotropic model, doping lateral diffusion of turbulence, was coded to better perform in plane film cooling and effusion cooling tests. The accuracy of the implementations was validated comparing results with experimental data available both from standard literature test cases and from in-house performed experiments. The geometries considered as validation tests cover the typical heat transfer problems in gas turbine design, namely impingement jets, film cooling and effusion cooling. During the tests, OpenFOAM code has shown a good accuracy and robustness as well as a remarkable computational speed.

The purpose of this paper is to present the results of the work

done to test OF as an effective substitute for standard commercial CFD packages, both for academic and industrial users, in the specific field of heat transfer applications in turbomachinery.

### INTRODUCTION

It is known how the study of cooling devices for turbomachinery is nowadays a keypoint in the design of both aeronautic and heavy duty engines. This is due to the great influence such systems have on the entire machine behavior both in terms of enhancing life of hot components, increasing the overall efficiency of the system and reducing exhaust emissions.

Accurate heat transfer measurements are however very expensive to support due to the complexity of geometries, the high costs of measuring device and the long set up necessary to collect reliable data. CFD analysis is as a consequence becoming more and more popular in each phase of the design process. Nevertheless, the numerical evaluation of thermal loads and effectiveness of the cooling devices in gas turbine engines is one of the most complex to face.

First of all the intricate geometries of reference, such as ribbed or pin-finned internal blade ducts, require quite flexible mesh criteria and the capability of solving for hybrid unstructured meshes become a must. In addition the importance of well predicting the flow behavior in the vicinity of solid walls imposes a very fine spacial discretization increasing a lot grid dimensions and complexity. Moreover standard cooling systems involve many different kinds of flow, each one with its own peculiarity and characteristic, meaning that also the physical modeling will differ case by case. Typical example is the treatment of turbulence for which the use of specific advanced models is a

keypoint in the success of the numerical predictions. A large set of turbulence models is so necessary not to limit correct simulation to a specific class of flows.// All these requirements have up to now limited the choice of CFD codes to few well-known commercial codes, for heat transfer analysis in turbomachinery both in academic and industrial field. Even though these codes offers numerous advantages, amongst which the ease of use and the large amount of built-in models, expert users may find several big drawbacks. Being thought for being multipurpose solvers in fact, their performances in terms of computational time and allocating resources result very poor. Due to their fixed and hidden internal structure, the possibility to introduce in the code user-defined models is usually limited, time-consuming and not very efficient as the complexity of the model grows. This is a very limiting issue both for academic and industrial *R&D* departments who need to manipulate the code to introduce "ad hoc" models often tuned on specifically conducted experiments. A code like OpenFOAM is indeed more suited for this type of user. Anyhow the lack of a steady-state compressible solver and of advanced turbulence models for heat transfer phenomena of the official release, limit a lot the reliability of the numerical predictions for this specific case.// The aim of the present paper is so to show the developments introduced in OpenFOAM standard release to make it suitable for steady state heat transfer analysis able to assist gas turbine design process. A fully compressible steady state pressure-based solver has been introduced together with a set of turbulence two-equations closures with particular reference to a detailed near wall treatment. As confirmation of the work done a set of validation testcases were performed. In particular, in this paper, we will focus our attention on the validation of the code with some complex configurations typical of heat transfer problems such as film cooling and impingement cooling. Both film and impingement cases were analyzed with single and multi-hole configurations. Comparisons with experimental data are reported in terms of adiabatic effectiveness for film cooling tests and wall heat transfer coefficient for impingement runs. Furthermore, in order to verify the accurate implementation of selected turbulence models, a simple flat plate tests was considered, while to show the robustness of the steady state solver developed results of classical validation tests are briefly commented.

## NOMENCLATURE

$U$	Vector velocity	$[m\ s^{-1}]$
$D$	Hole diameter	$[m]$
$h$	Heat transfer coefficient	$[W\ m^{-2}\ K^{-1}]$
$k$	Turbulent kinetic energy	$[m^2\ s^{-2}]$
$L$	Height of the jet	$[m]$
$p$	Pressure	$[N\ m^{-2}]$
$p'$	Pressure corrector	$[N\ m^{-2}]$
$\dot{q}$	Heat flux	$[W\ m^{-2}]$
$Re$	Reynolds number	
$T$	Temperature	$[K]$
$T_s$	Turbulent time scale	$[s]$
$P_k$	Turbulence production term	
	$= \mu_t \left( \frac{\partial U_i}{\partial x_j} + \frac{\partial U_j}{\partial x_i} \right) - \frac{2}{3} \delta_{ij} \frac{\partial U_k}{\partial x_k} \frac{\partial U_i}{\partial x_j} - \frac{2}{3} \rho k \frac{\partial U_j}{\partial x_i}$	$[kg\ m^{-1}\ s^{-3}]$
$S$	Tensor strain $= 0.5 \left( \frac{\partial U_i}{\partial x_j} + \frac{\partial U_j}{\partial x_i} \right)$	$[s^{-1}]$
$X$	Streamwise direction	$[m]$
$Y$	Spanwise direction	$[m]$
$C_\rho$	Compressibility term $\frac{1}{RT}$	$[kg\ J^{-1}]$
$H$	Diffusive discretization term	$[kg^{-1}\ s\ m^3]$
<b>Greeks</b>		
$\alpha$	Angle between hole and crossflow	
$\eta$	Adiabatic effectiveness $\frac{(T_\infty - T_{aw})}{(T_\infty - T_c)}$	
$\langle \eta \rangle$	Spanwise averaged effectiveness $\sum_n \frac{(T_\infty - T_{aw})}{(T_\infty - T_c)}$	
$\omega$	Turbulence frequency	$[s^{-1}]$
$\varepsilon$	Turbulence dissipation	$[m^2\ s^{-3}]$
$\mu_{t,eff}$	Eddy viscosity	$[kg\ m^{-1}\ s^{-1}]$
$\rho$	Density	$[kg\ m^{-3}]$
$\gamma$	Anisotropic factor	
$\Gamma$	Blending function	
<b>Subscripts</b>		
0	Uncooled plate	
$aw$	Adiabatic wall	
$\infty$	Crossflow	
$c$	Coolant	
$w$	Wall	
$awt$	Automatic Wall Treatment	
$p$	First near wall node	
$HR$	High Reynolds	
$LR$	Low Reynolds	

## SOLVER

In turbomachinery and heat transfer applications, involved fluid flows may cover a wide range of Mach regimes. In particular, it usually happens that different Mach conditions simultaneously arise in the same domain. Such situation makes the accurate solution of viscous flows governing equations a complex task.

To avoid the known weaknesses of density-based algorithms, another class of methods, proposed originally for viscous incompressible flows [1, 2, 3, 4] and later extended to compressible flows [5, 6, 7, 8, 9, 10, 11] use pressure as the main independent variable also with the concept of the 'retarded density' [12, 13, 14]. Such pressure-based approach is founded on the SIMPLE algorithm (Semi-IMPlicit Pressure Linked Equations) [1]. In this method, continuity equation is converted into an equation for pressure corrector overturning the linkage between pressure and density to extend applicability range up to zero Mach number. The SIMPLE algorithm uses a segregated approach where the equations are solved in sequential steps letting to the iterative process the care of the non-linearity as well as the coupling between equations. To better visualize the cycle of SIMPLE algorithm a flow-chart of the pseudo code is reported

in Fig. 1.

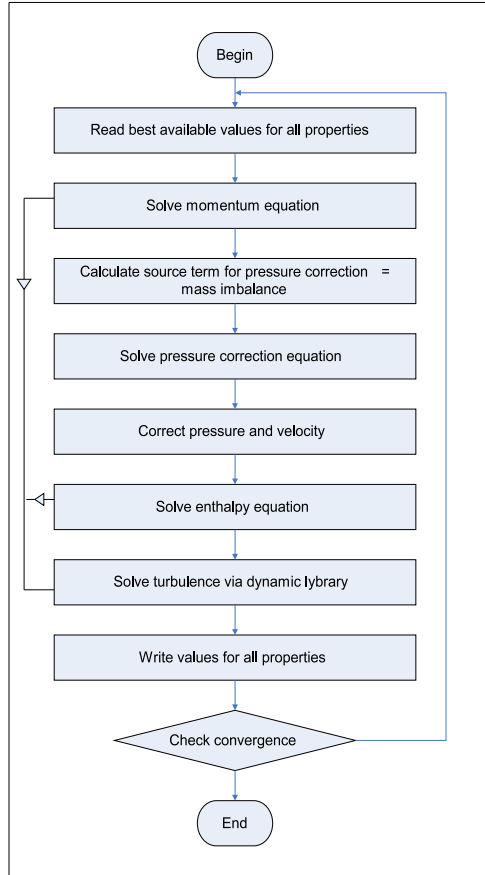


Figure 1. Flow chart of SIMPLE algorithm.

The improvements of this class of methods in contrast with the standard SIMPLE technique lies in a more precise derivation of the equation for the pressure corrector, allowing the possibility of treating at the same time low subsonic, almost incompressible, and high compressible flows.

The pressure correction equation, details can be found in [15, 16, 17, 18], in the compressible form says:

$$\nabla \cdot (C_\rho U p') - \nabla \cdot (\rho H (\nabla p')) = -\nabla \cdot (\rho U). \quad (1)$$

The role of Eq.(1) in the SIMPLE cycle is to enforce mass conservation, it is in fact derived from a combination of momentum conservation and continuity equation. In order to solve Eq.(1), attention should be posed on the fact that the pressure correction equation now assumes a convective-diffusive form instead of

a purely diffusive behavior like the original incompressible formulation. While the other steady-state form transport equations have to be relaxed in order to characterize the inertial physics lost by the elimination of the time derivative, for the pressure correction equation this cannot be done. Usage of usual implicit relaxation techniques on pressure corrector, in fact, corrupt mass conservation on single iteration steps breaking the concept standing behind SIMPLE algorithm. In subsonic cases, standard Neumann conditions at inlet velocity boundary, like in incompressible tests, determine ill-defined problems for Eq.(1). Care must be taken in handling pressure correction boundary condition in order to solve in a well-posed manner such an equation [19]. A combination of Dirichlet and Neumann type condition for the inlet has been tested.

## TURBULENCE MODELS

The correct modeling of turbulent quantities is fundamental in conducting heat transfer simulations, because of the simultaneous importance of well predicting both the near wall behavior and the complex structures of the main flow [20, 21]. Correct predictions of thermal quantities and gradients inside boundary layers are necessary to establish whether or not the cooling systems of gas turbine are efficient. At the same time wall properties are very dependent on the development of the free stream flow.

Use of standard wall function has to be avoided because of the unpredictability of boundary thermal gradient and the failure in predicting transitional, Low Reynolds as well as adverse pressure gradient flows.

First step in modeling turbulence in a more appropriate manner inside the near wall region has been the introduction of the so-called damping functions in the standard  $k - \varepsilon$ . The basic structure of the models is the same for all of them differing in the tuning of the damping functions and some extra sources in dissipation equation, as shown below:

$$\frac{\partial \rho k}{\partial t} + \nabla \cdot (\rho U k) - \nabla \cdot (\mu_{eff} \nabla k) = P_k - \rho \varepsilon, \quad (2)$$

$$\frac{\partial \rho \varepsilon}{\partial t} + \nabla \cdot (\rho U \varepsilon) - \nabla \cdot (\mu_{eff} \nabla \varepsilon) = f_1 P_k \frac{\varepsilon}{k} - f_2 \rho \frac{\varepsilon^2}{k}. \quad (3)$$

Of the many Low Reynolds  $k - \varepsilon$  models proposed in literature in the course of years, the models by Lien and Leschziner [12], Lien [22], Abe *et al* [23], Chien [24], Chen *et al* [25], Hwang and Lin [26] and Lam and Bremhorst [27] have been implemented.

It is however known in literature that in high strain rate regions eddy viscosity models tend to overpredict turbulent kinetic energy: this problem is sometimes referred to as “stagnation point anomaly” [28]. These higher values of  $k$  are due to an overestimate of production term  $P_k$ . To avoid such overprediction

linear dependence between  $P_k$  and  $|S|^2$  should be bounded in regions where  $|S|$  grows. This is achieved with a time scale bound, derived from a “realizability” constraint for Reynolds stress tensor to be definite positive:

$$T_s = \frac{\mu_t}{C_\mu \rho k} = \min \left( \frac{k}{\varepsilon}, \frac{\alpha}{\sqrt{6} C_\mu |S|} \right) \quad (4)$$

This limiter proposed by Durbin [29] has been inserted in all Low Reynolds models above presented as an option to be switched on or off by the user.

Then, in order to match good near wall predictions with suitable modeling of flow structures far from the wall, Two Layer  $k - \varepsilon$  models have been implemented. Such method consists in patching together a one equation model in the near wall layer and a two equation High Reynolds model in the outer layer [30]. Both Wolfstein and Norris&Reynolds closure formulas [22] have been tried without significant discrepancies in the results.

Another failure of numerical computations, already pointed out in previous studies [31, 32], is the low lateral spreading predicted for jets in crossflow. Both film and effusion cooling geometries tend in fact to concentrate the cooling effect on the meanline of the holes. This is due to the assumption of turbulence isotropy that fails in the near-wall region because of the damping of normal to wall fluctuations. To avoid this discrepancy with experimental evidences, Bergeles [33] proposed to algebraically correct the main Reynolds stress, enlarging the product of the stream and span directed fluctuation. The Reynolds Stress tensor is so calculated using a tensorial definition of turbulent viscosity:

$$-\overline{\rho u'_i u'_j} = \mu_{t,ij} \left( \frac{\partial U_i}{\partial x_j} + \frac{\partial U_j}{\partial x_i} - \frac{2}{3} \delta_{ij} \frac{\partial U_k}{\partial x_k} \right), \quad (5)$$

where

$$\mu_{t,ij} = \begin{pmatrix} \mu_t & \gamma \mu_t & \mu_t \\ \gamma \mu_t & \mu_t & \mu_t \\ \mu_t & \mu_t & \mu_t \end{pmatrix}, \quad (6)$$

and  $\gamma$  is an amplification factor ranging from 4.5 in the free-stream region to 60 in the near wall region (the model is applied for  $y^+ > 1.5$ ) [34].

This correction was applied to the Two Layer model changing the turbulent flux in the momentum, energy and turbulence equations.

All previous models require a quite fine grid at walls ( $y^+ \approx 1$ ) but for cases of a certain complexity this results to be a quite

strict constraint. In order to increase grid independence a mixed approach between wall-function and Low Reynolds was added to the  $k - \omega$  SST model. The idea, see [35], is to blend the two approaches via a blending function  $\Gamma$  calculated algebraically from the non dimensional wall distance. Both turbulent production and turbulent specific dissipation are imposed on the first node mixing the effects of the Low Reynolds and the High Reynolds contributions:

$$P_{awt,p} = P_{LR,p} e^{-\Gamma} + P_{HR,p} e^{-\frac{1}{\Gamma}}, \quad (7)$$

$$\omega_{awt,p} = \omega_{LR,p} e^{-\Gamma} + \omega_{HR,p} e^{-\frac{1}{\Gamma}}, \quad (8)$$

where  $\Gamma$  is calculated with an algebraic expression for  $y^+$  defined with  $u_\tau = \max(u_{\tau,LR}, u_{\tau,HR})$ . The same blending is applied to thermal quantities following Kader universal law [36].

## RESULTS

### Generalities

Most of the cases to be presented have already been tested and published in [37] where much more details on the cases can be found. Even if many of the already obtained results are reported to make comparisons, here the focus will be on the new models to be tested: the anisotropic model and the automatic wall treatment for the  $k - \omega$  SST.

Due to the great number of implemented turbulence models, a shortcut has been used to name most of them: the acronyms presented in Tab. 1 will be widely used in substitution of authors' full name.

Table 1. Acronyms for the various turbulence models.

$k - \varepsilon$ Low Reynolds by Abe et al.	AKN
$k - \varepsilon$ Low Reynolds by Chien	CH
$k - \varepsilon$ Low Reynolds by Lien et al.	CLL
$k - \varepsilon$ Low Reynolds by Hwang and Lin	HW
$k - \varepsilon$ Low Reynolds by Lam and Bremhorst	LB
$k - \varepsilon$ Low Reynolds by Lien and Leschziner	LW
$k - \varepsilon$ Low Reynolds by Lien	LNR
Realizability constraint correction	Real
Two Layer	TL
Anisotropic Two Layer	KEA
Automatic Wall Treatment	SSTawt

## Turbulence Models Validation Test

### Flat Plate

First test to be presented is a fully turbulent flow over an adiabatic flat plate. Such simple case was chosen in order to test in detail the near wall behavior of turbulence, that is why a very fine grid was needed. The flow field being modeled is that reported by Wieghardt [39] and later included in the 1968 AFOSR-IFP Stanford Conference [40]. Details about flow conditions are listed in Tab. 2.

Table 2. Flow conditions for flat plate test

Inlet temperature	294.4	K
Inlet Mach number	0.2	
Pressure	101400	Pa
Turbulence kinetic energy - $k$	23.6	$m^2 s^{-2}$
Dissipation - $\varepsilon$	3365	$m^2 s^{-3}$
Comparison axial loc. - $x$	4.6870	m

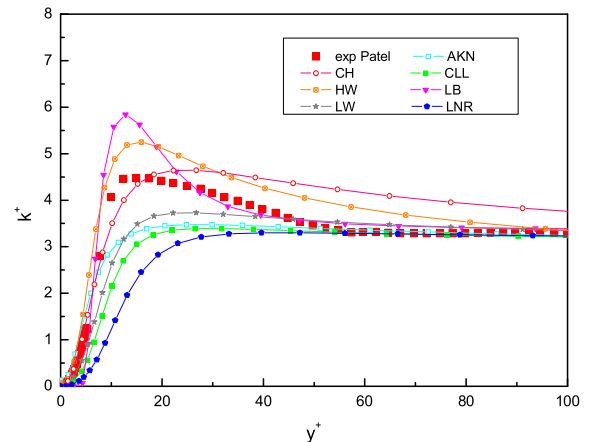
Both the non dimensional  $k$  and  $\varepsilon$  were checked in their behavior against the non dimensional wall distance at an axial location where the flow can be considered fully developed, Fig. 2. The level of agreement with the experimental is fairly good, especially for  $k^+$ , with free stream values matching for almost all models. However the discrepancy between experimental and numerical simulation follows exactly the profiles obtained by other researchers some of which are directly models' authors [41, 24, 26]. Both for a higher guarantee of stability and for the best reliability on matching experimental results further test was conducted only on CLL and AKN.

For the same geometry another case involving heat transfer was set up to validate mesh independence of the  $k - \omega$ SST with the automatic wall treatment. Three different grids with increasing first node distance from the wall were tested ( $y_p^+ = 0.1$ ;  $y_p^+ = 9$ ;  $y_p^+ = 35$ ). The results are reported in terms of Stanton number and tested against Incropera [42], see Fig.3. Even if the three profiles are still not coincident the mesh dependence is decreasing as the flow develops and moreover the agreement is improved a lot from standard wall function approach.

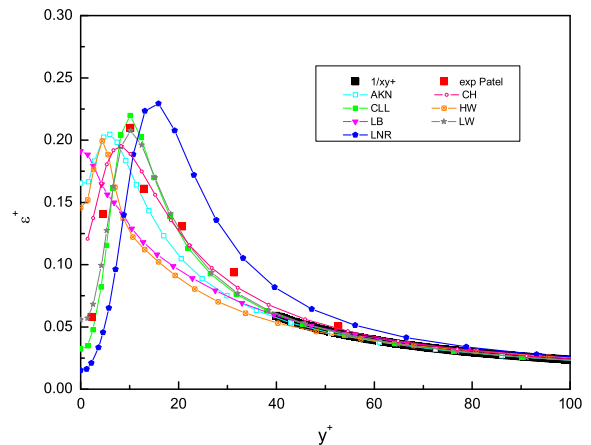
### Heat Transfer tests

#### Impingement Cooling

As already known in literature, impinging jets flows are a specific class of flows for which the modeling of turbulence results determinant in obtaining acceptable agreement with experimental data. Especially for flows involving heat transfer in fact, the flow conditions in the area around the stagnation point result



(a)  $k^+$  profile



(b)  $\varepsilon^+$  profile

Figure 2. Turbulence quantities profiles.

pretty dependent on the turbulence model used. The numerical estimation of heat transfer coefficient, for example, can lead to errors of about 100% in the evaluation of the peak, choosing one or another model. This class of flows is so suitable for deeply testing new turbulence models.

Two different impinging geometries were tested: first of all a 2-D normal impinging jet of air has been performed following a test case by ERCOFTAC and after a five row array of holes reproducing experimental results obtained during the European project LOPOCOTEP.

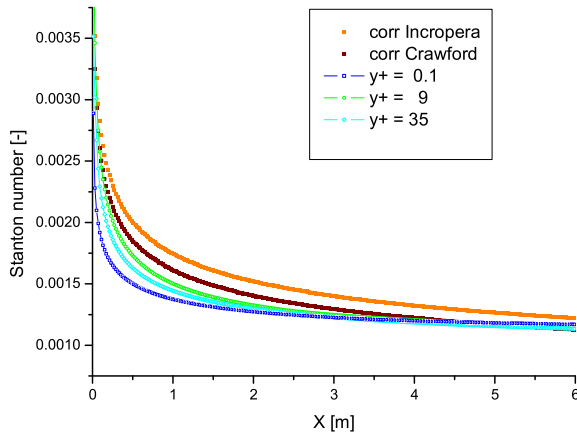


Figure 3. Stanton number profile.

### ERCOFTAC C25 Axial-symmetric Impingement

This case is a turbulent incompressible flow of air impinging onto a flat plate, modeled after [43]. The impact surface is heated and kept at constant heat flux of  $\dot{q} = 200 \text{ W/m}^2$ , all other walls were treated as adiabatic walls. From the experiments, the Nusselt number distribution for various jet Reynolds numbers is known. For validation purpose, a Reynolds number of 23,000 and a distance of  $L/D = 2$  were chosen. The far-field boundaries are modeled as mixed inflow/outflow pressure boundaries.

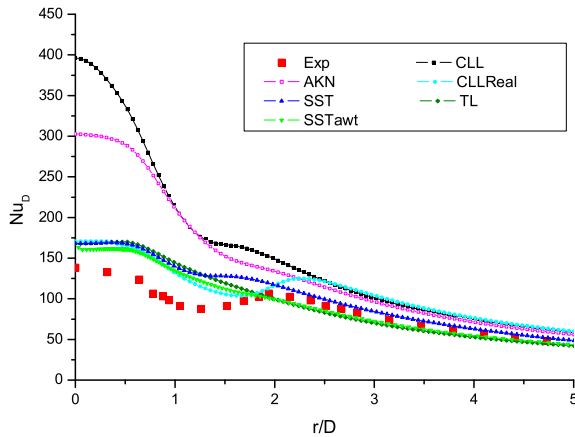


Figure 4. Nusselt number distribution along radius.

Fig. 4 shows how the models without realizability constraint

fail and dramatically overpredict the peak in the heat transfer coefficient (error of almost 200%) in agreement with the original idea of such limiter [44].

In addition to what already noticed in [37], it is possible to compare the behavior of the SSTawt model with the other models. When the same Low Reynolds mesh is used its predictions are obviously collapsing on the standard SST model and agreement with the best performing models is good.

**5-Holes Impingement cooling** This case is simulating typical design conditions for impingement cooling of a gas turbine. The case was performed following the set up of an experiment done at the Energy Engineering Department of the University of Florence for the European project LOPOCOTEP (LOW POLLUTANT COMBUSTOR TEChnical Programme). Coolant is injected from a plenum through a perforated plate and impacts over a flat plate at uniform heat flux reproducing the behavior of the first 3 – 2 rows (the array of holes is staggered) for a total of 5 jets. For further details refer to [45].

Main flow parameters are reported in Tab. 3.

Table 3. Flow conditions for 5-hole impingement test

Inlet Temperature	308.2	<i>K</i>
Outlet Pressure	85101	<i>Pa</i>
Inlet Turbulence level - Tu	$\leq 0.5\%$	%
$Re_j$	7600	
Inlet Velocity	0.28956	<i>m/s</i>
Wall Heat flux	3000	<i>W/m}^2</i>

Simulations have been validated in terms of heat transfer coefficient, see Fig. 5 and Fig. 6, calculated with respect to inlet static temperature, almost coincident for such low Mach number with inlet total temperature. Adiabatic simulations have been conducted too but on a single hole configuration of the same case, in order to check whether this approximation could be done or not.

Both experimental and numerical data are sampled onto the two different lines connecting symmetry planes and then merged together in the zone where a relative minimum is localized.

Even if obtained results are in good agreement with experimental data far from the stagnation point, it should be noticed that predictions for the peak value are quite different from measured data. Higher discrepancies on the even peaks are probably due to errors in the experimental measurements [45]. Comparing the two models, Two Layer predicts peak values a 10% better of the SST giving basically identical results outside the stagnation points area. In any case, it should be considered that temperature gradients are quite small. A better agreement is expected for higher values of wall heat flux.

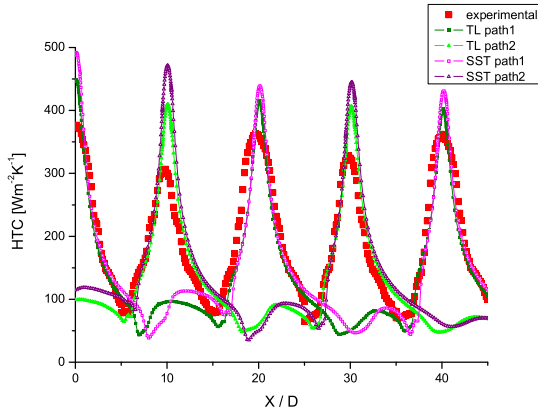


Figure 5. Heat transfer coefficient along center lines.

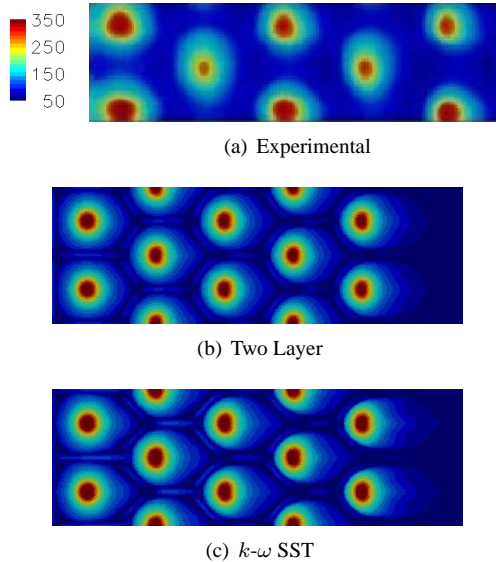


Figure 6. Heat transfer coefficient [ $W m^{-2} K^{-1}$ ] distribution on impinging wall.

### Film and effusion cooling

This section is presenting results for jets in crossflow aimed at representing both film and effusion cooling. The main difference in these two methods of cooling stands actually just in which is the principal cooling effect of the cold flow injected in the hot gases. In film cooling the heat absorbed in the small hole is negligible and wall is protected with a film of coolant over the external surface. For effusion cooling viceversa the less effective film protection is compensated by a higher heat removed in the holes.

The numerical prediction of the mixing between coolant and cross flow still represents one of the most difficult task in CFD analysis, even in adiabatic conditions [46]. The difficulties are mainly related to the well known deficiency of standard eddy viscosity turbulence models in the accurate prediction of lateral jet spreading, essentially due to the isotropy assumption for turbulent stresses [47, 48, 49]. The performances of the KEA model were so tested against standard EVM in terms of averaged and local adiabatic effectiveness.

Two different test-cases were studied: the well known single hole experiment by Sinha [50] and an experimental multi-hole geometry aimed at cooling turbine endwalls [51].

**Sinha test** Experimental data and geometries are based on tests made by Sinha *et al.*[50]; local and spanwise averaged effectiveness are compared with calculated values. The geometry is a flat plate with a single row of holes, while flow conditions are listed in table 4.

Table 4. Flow conditions for Sinha test

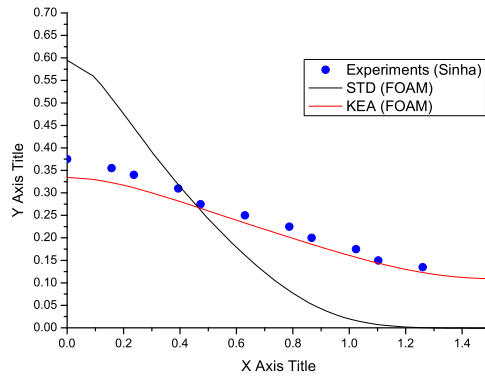
Cross flow temperature	300	$K$
Coolant temperature	153	$K$
Pressure	$10^5$	$Pa$
Density ratio - DR	2.0	
Blowing-rate - M	0.5	
Momentum ratio - I	0.125	
Turbulence level - Tu	$\leq 0.2$	%
Cross flow velocity	20	$m/s$
$Re_c$	15700	

The performances of standard turbulence models (STD model in Figs.7(a) and 7(b) were analyzed in comparison with the anisotropic model (KEA) in terms of laterally-averaged and local span-wise and centerline effectiveness.

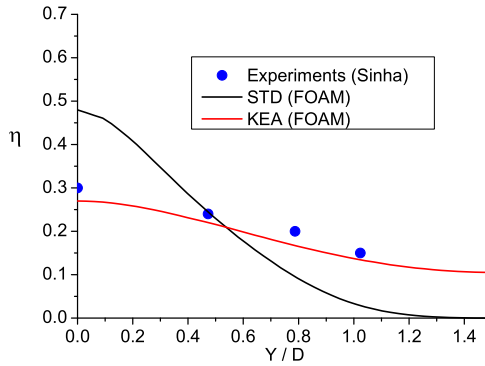
Local lateral effectiveness 10 and 15 diameters downstream is shown in Fig. 7, local centerline and laterally averaged effectiveness is also presented in Fig. 8. Finally a map of wall effectiveness is reported in Fig. 9.

The improvements obtained using the anisotropic model are remarkable. The experimental lateral profiles of effectiveness are perfectly reproduced both at 10 and 15 diameter downstream while all the other isotropic models were failing such predictions dramatically. The centerline values also tend to be much closer to experiments especially when the distance from the hole is increasing. It is clear how the eddy viscosity model predicts a too coherent jet Fig. 9, thus severely underestimating lateral cooling performances. However this error is smoothed in the laterally-averaged parameters and as expected the anisotropic factor just distribute in different way the coolant over the plate





(a) 10D



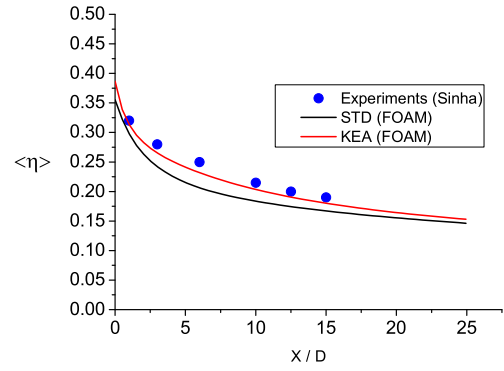
(b) 15D

Figure 7. Spanwise distribution of film cooling effectiveness at various sections.

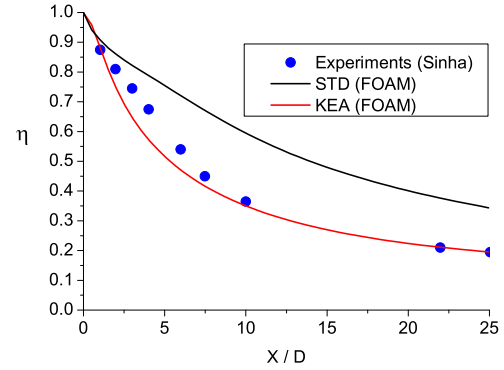
not influencing that much the averaged effectiveness. This consideration allows the use of isotropic models when the averaged parameters are considered but as expected confirm how, the local values of wall temperature cannot be considered reliable.

**6-Holes effusion cooling** The geometry of this case is a six holes flat plate interposed in between a plenum and a channel at lower pressure. A summary of flow conditions can be found in Tab. 5.

Results are reported in terms of spanwise averaged adiabatic effectiveness, see Fig. 10. Together with experimental data, correlative approach predictions using L'Ecuyer and Soechting correlation with Sellers superposition criterion have been reported [51]. It is in fact quite difficult to reproduce exactly such experimental profiles that are better used as a reference mean value for  $\eta$ . In agreement to what already noticed in the previous case, the



(a) Laterally averaged



(b) Center line

Figure 8. Comparison between laterally averaged and local center line film cooling effectiveness.

Table 5. Flow conditions for 6-holes effusion test

Cross flow temperature	323	$K$
Coolant temperature	298	$K$
Pressure	$7.0 \cdot 10^{-4}$	$Pa$
Density ratio - DR	1.103	
Blowing-rate - M	0.2	

laterally averaged effectiveness is not that much influenced by the anisotropic factor, see Fig.10.

All models in fact qualitatively well reproduce the correlative decay of the spanwise averaged effectiveness downstream the holes. By looking at the two-dimensional effectiveness map in Fig. 11 however it's evident how the lateral diffusion of coolant is more correct in the anisotropic case than in the other two. For the lack of experimental data this analysis could only be done qualitatively.

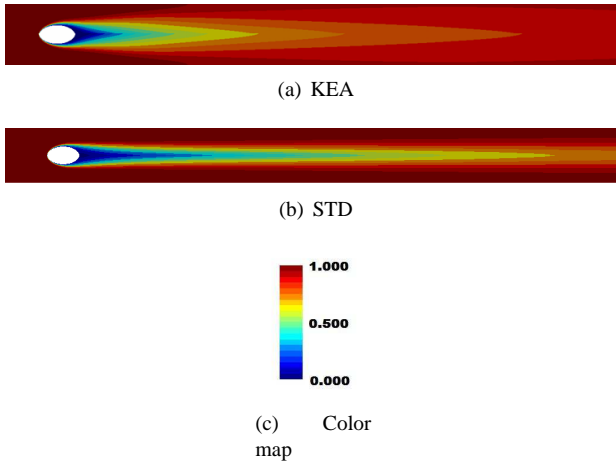


Figure 9. Effectiveness distribution over the wall.

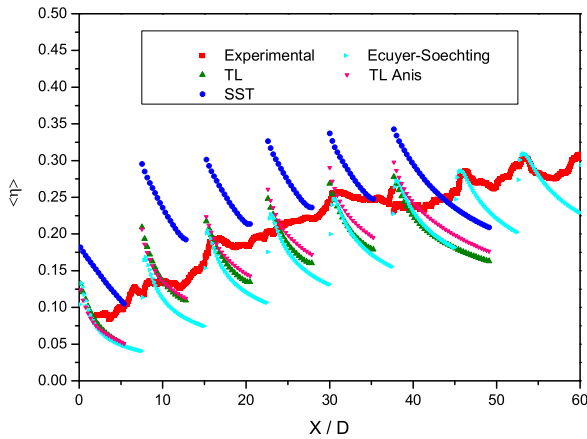


Figure 10. Spanwise averaged adiabatic effectiveness.

## CONCLUSIONS

OpenFOAM has been improved to predict heat transfer phenomena in gas turbine. Many different tests were performed representing the state of the art for the cooling systems in turbomachinery applications. Validation of a pressure correction algorithm and various turbulence models have been made by comparison with experimental data on typical heat transfer geometries. Massive parallel calculation have also been tested for the multirow configuration simulations both for impingement and effusion cases by the use of LAM/MPI library <http://www.lam-mpi.org>.

The combination of the new built-in OpenFOAM libraries is able to reproduce the flow conditions with good accuracy for all

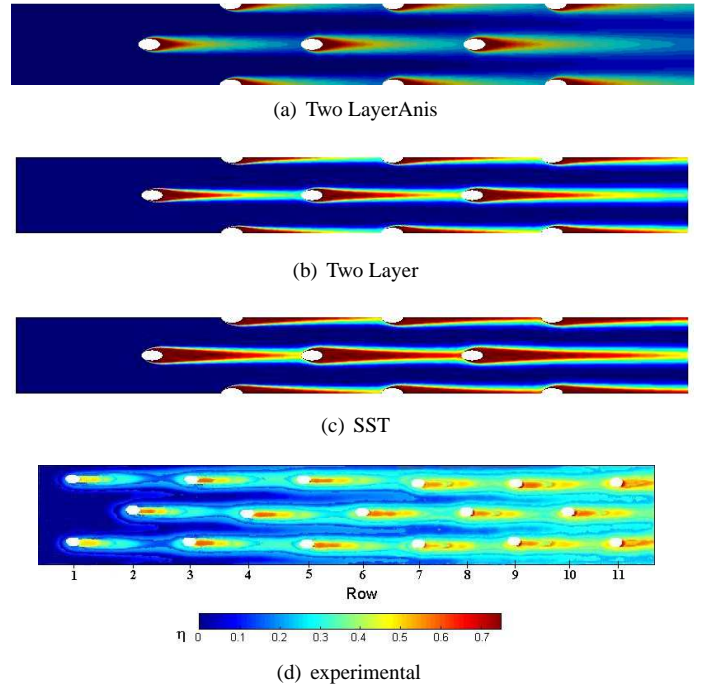


Figure 11. Comparison between laterally averaged and local center line film cooling effectiveness.

the geometries studied. Good agreement with experimental data and with the common commercial software has been reached for impingement and effusion cooling configurations.

The used object oriented language results to be very flexible for implementing new turbulence models, solver algorithms, boundary condition types and physical models.

Future work will be concentrated on expanding the capability of the code to simulate fluid-structure interaction, with main focus in conjugate heat transfer analysis. An even more fundamental step will be to expand the capability of the code to handle periodic boundaries, in particular it is necessary to implement a new non-conformal type of cyclic patch.

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